

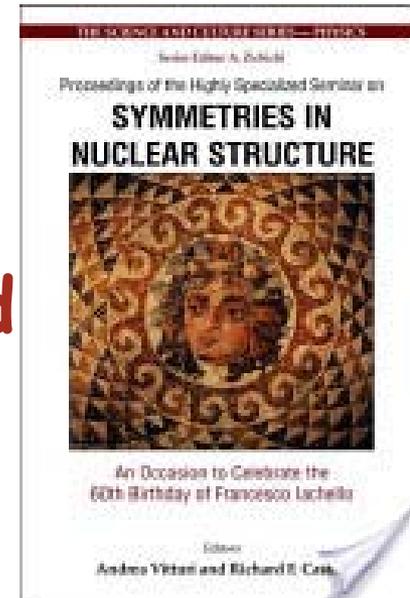
"The pursuit of truth and beauty is a sphere of activity in which we are permitted to remain children all our lives."

Albert Einstein



Beauty in Physics □ Theory and Experiment

Hacienda Cocoyoc, Morelos,
May 14-18, 2012





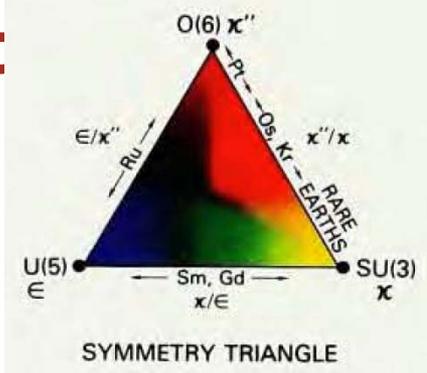
My personal Journey

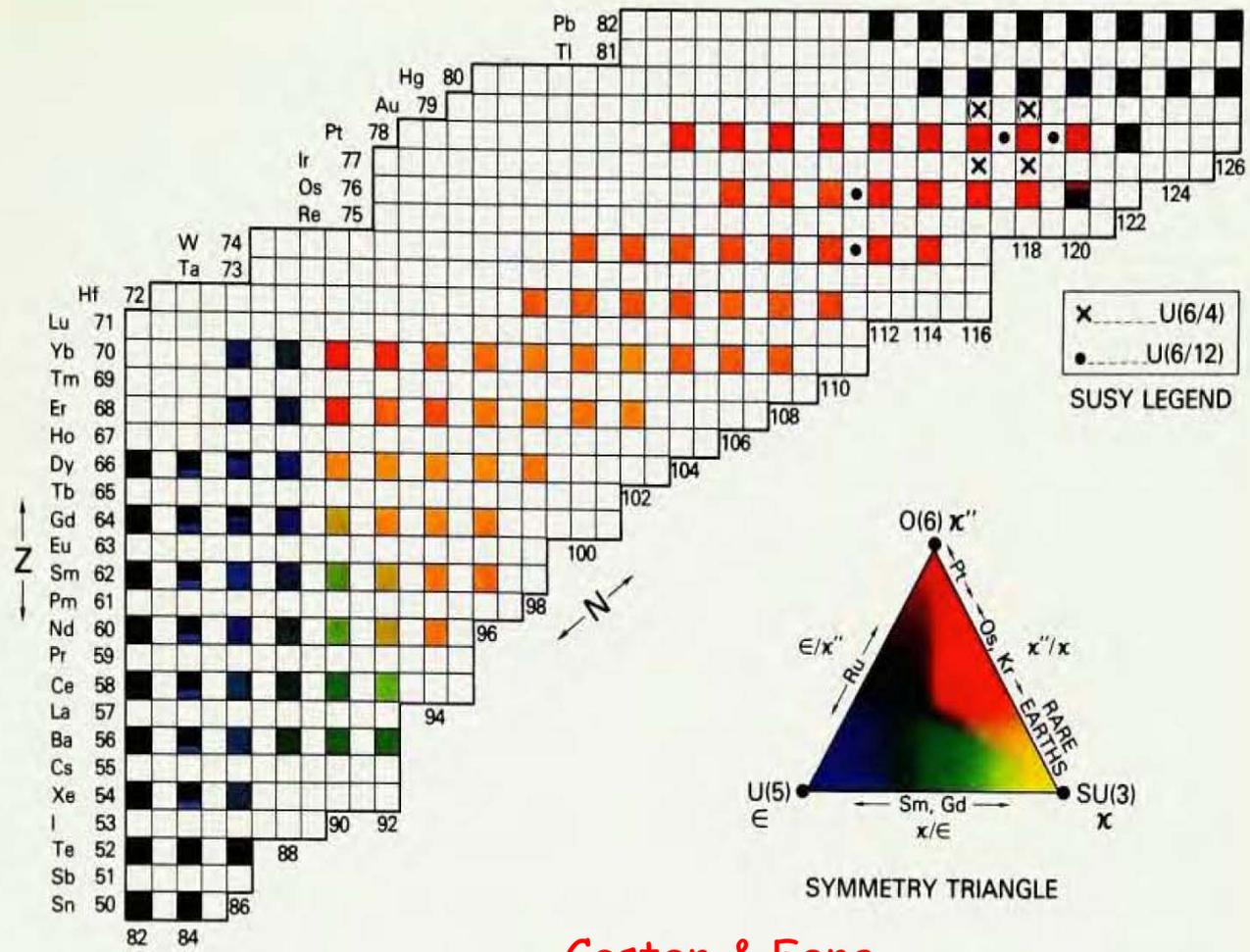
Beauty in Physics □ Theory and Experiment



Beauty in Physics □ Theory and Experiment

Hacienda Cocoyoc, Morelos,
May 14-18, 2012





Casten & Feng
 Physics Today 37, 26 (1984)

Beauty in Physics – Theory and Experiment

Hacienda Cocoyoc, Morelos,
 May 14-18, 2013

First Observation of a Near-Harmonic Vibrational Nucleus

A. Arahamian

Clark University, Worcester, Massachusetts 01610, and
Lawrence Livermore National Laboratory, Livermore, California 94550

D. S. Brenner

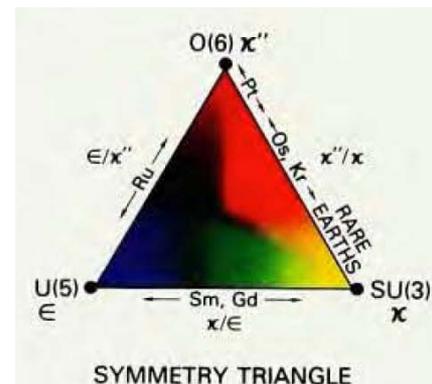
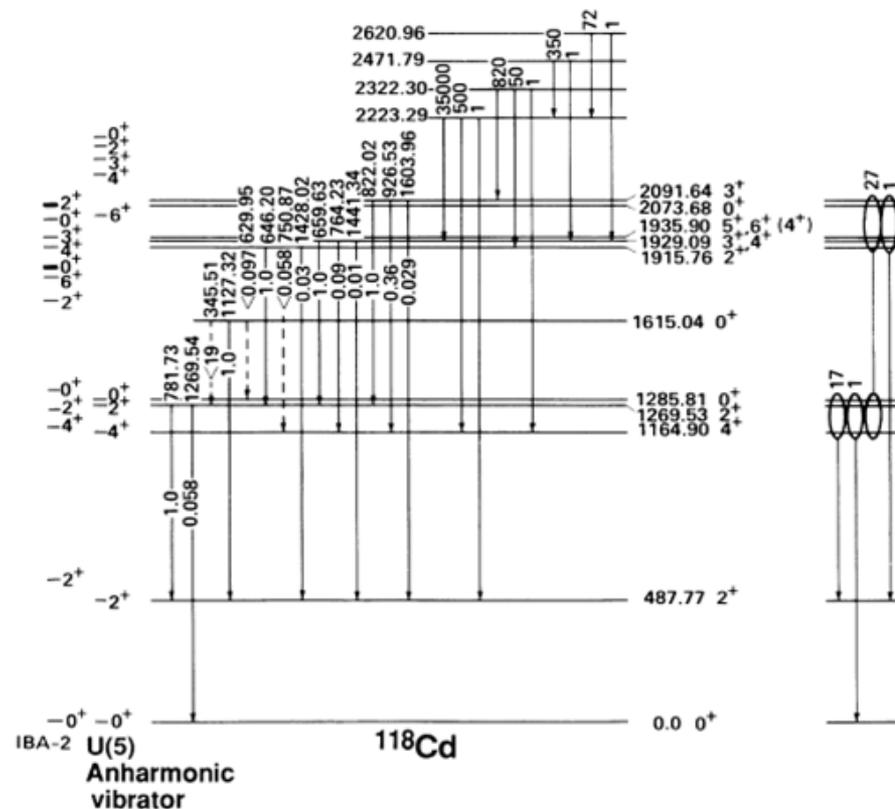
Clark University, Worcester, Massachusetts 01610

and

R. F. Casten, R. L. Gill, and A. Piotrowski^(a)

Brookhaven National Laboratory, Upton, New York 11973

(Received 4 May 1987)



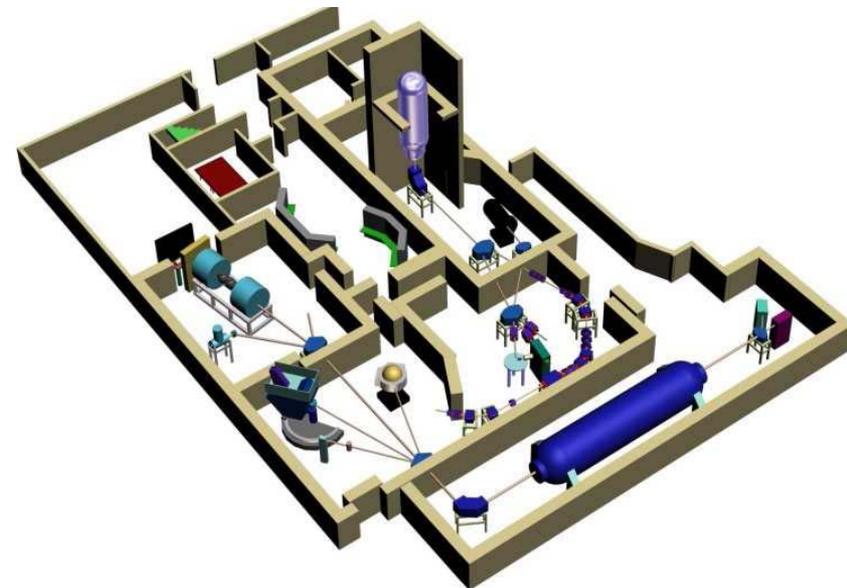
SYMMETRY TRIANGLE



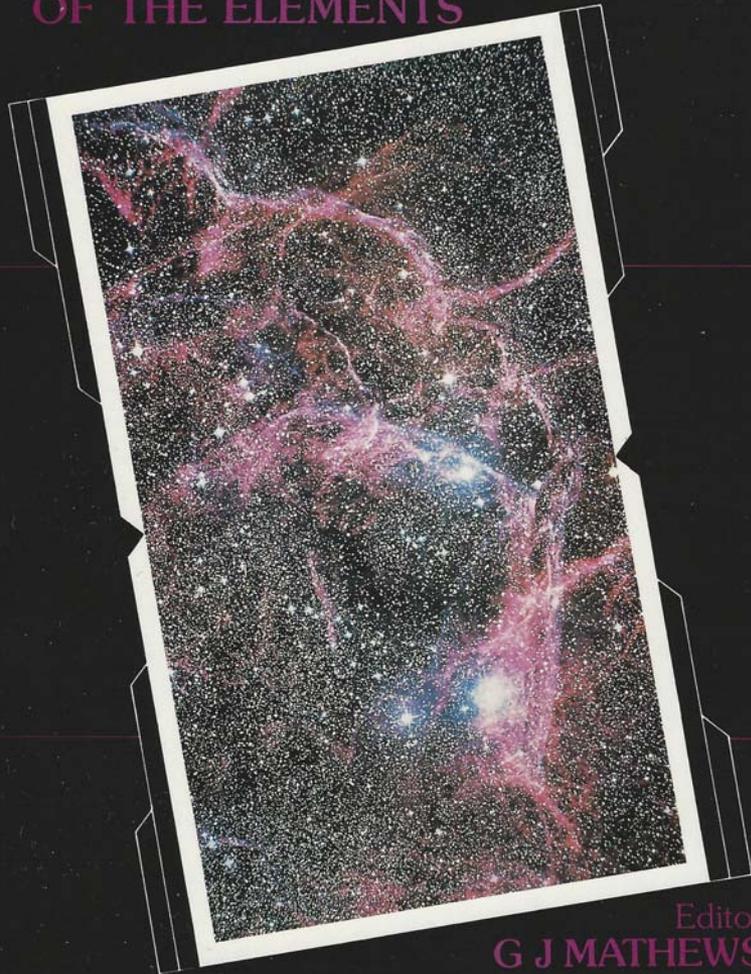
UNIVERSITY OF NOTRE DAME



Institute for Structure and Nuclear Astrophysics



ORIGIN AND DISTRIBUTION OF THE ELEMENTS



Editor
G J MATHEWS

World Scientific

1988

Nuclear Properties Along the r-Process Path

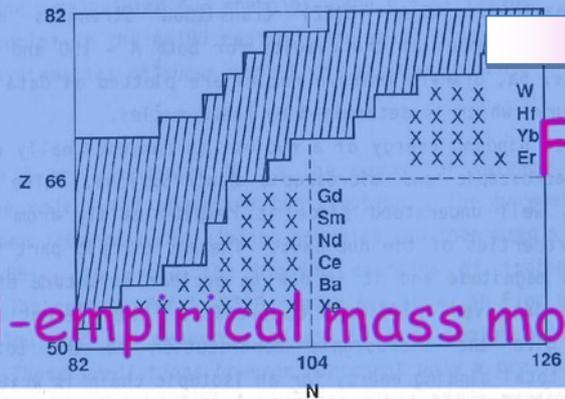
A. APRAHAMIAN
Lawrence Livermore National Laboratory
Livermore, California 94550
USA

Effective Boson Number

ABSTRACT

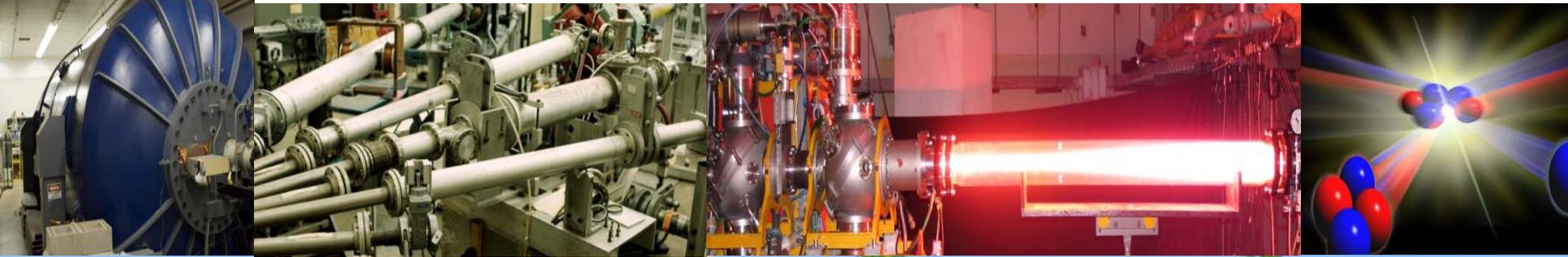
The uniformity of different nuclear regions as a function of the number of valence protons and neutrons (counted relative to the nearest closed shell) has been exploited for the parameterization of calculations for nuclei far from stability within the IBA model. Predictions are given for low lying levels, E2 transition rates, and binding energies for nuclei in the r-process path in the $A = 150$ and $A = 100$ mass regions.

nuclei that have been calculated.



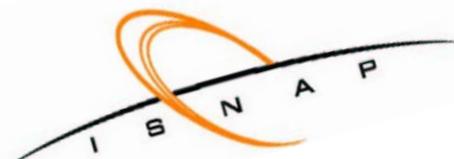
Semi-empirical mass model

Fig. 4 The relevant portion of the N-Z plane. The shaded parts indicate known nuclei. The x's show the calculated nuclei.





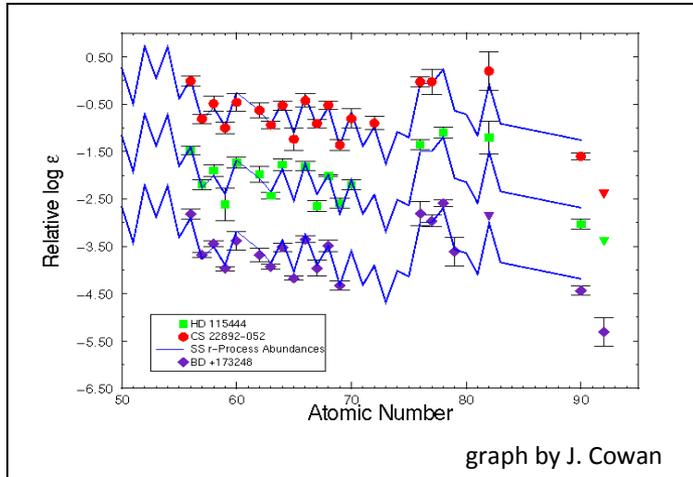
Sensitivities of the r-process to ...masses, β -decay rates, cross-sections nuclear structure



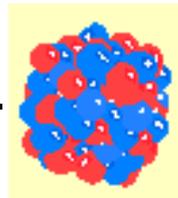
Institute for Structure & Nuclear Astrophysics
University of Notre Dame, Notre Dame, IN (USA)

The r-process problem

New precision observations of r-process elements



Nuclear Physics



Missing link

r-process models

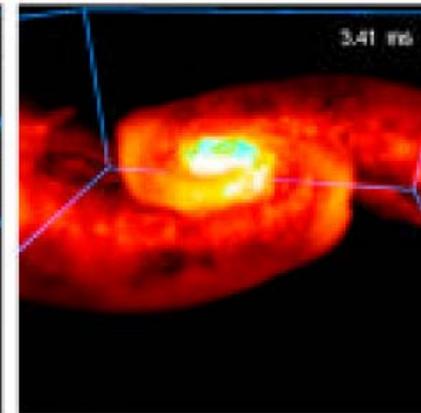
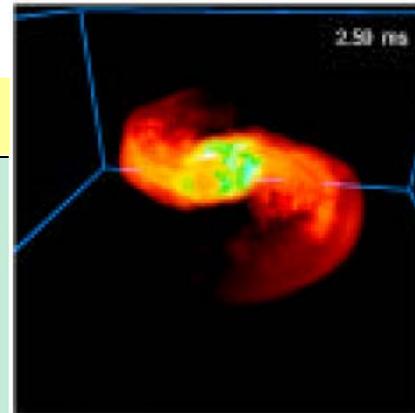
Supernova ?

- Neutrino wind ?
- Jets ?
- Explosive burning ?
- Prompt Explosions ?

GRB ?

Image: Burrows et al. 1995

Neutron star mergers ?

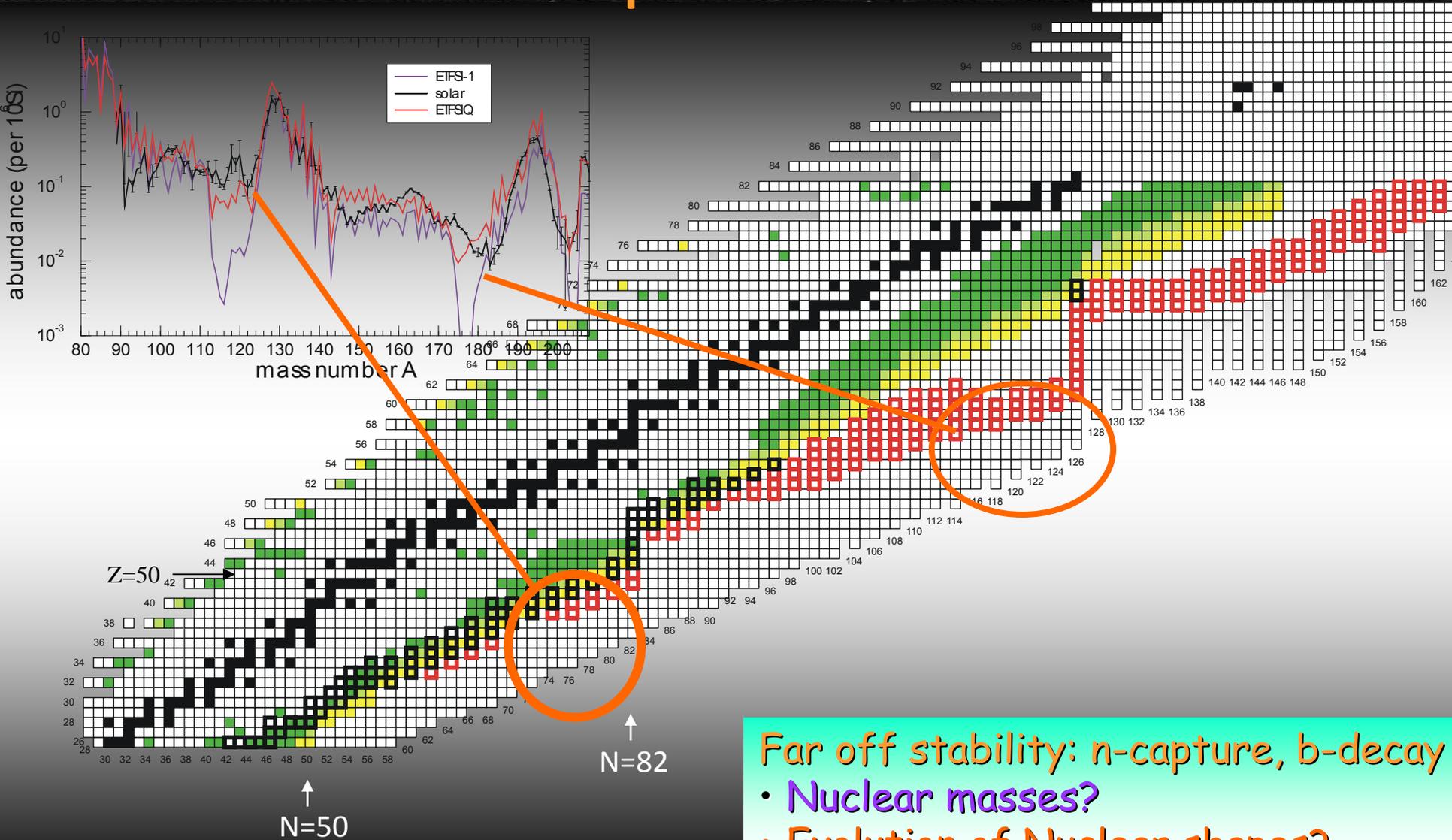


SDSS-2 Nuclear Physics driven observations

Need nuclear physics:

- With abundance observations the only experimental constraint of r-process environment
- Disentangle contributions from various s- and r-processes to observed abundances
- Use r-process as probe for extreme environment

r-process



Far off stability: n-capture, β -decay

- Nuclear masses?
- Evolution of Nuclear shapes?



Masses
 β -decay rates
n- capture

Major Shells and evolution of shells...

Experimental & Theoretical Challenges



Available online at www.sciencedirect.com

SCIENCE @ DIRECT*

Progress in Particle and Nuclear Physics 54 (2005) 535–613

Progress in
Particle and
Nuclear Physics

www.elsevier.com/locate/ppnp

Review

Nuclear structure aspects in nuclear astrophysics

A. Aprahamian^a, K. Langanke^b, M. Wiescher^{a,*}

^a*Department of Physics and the Joint Institute for Nuclear Astrophysics, University of Notre Dame, Notre Dame, IN 46556, USA*

How do you decide which nuclei to measure???

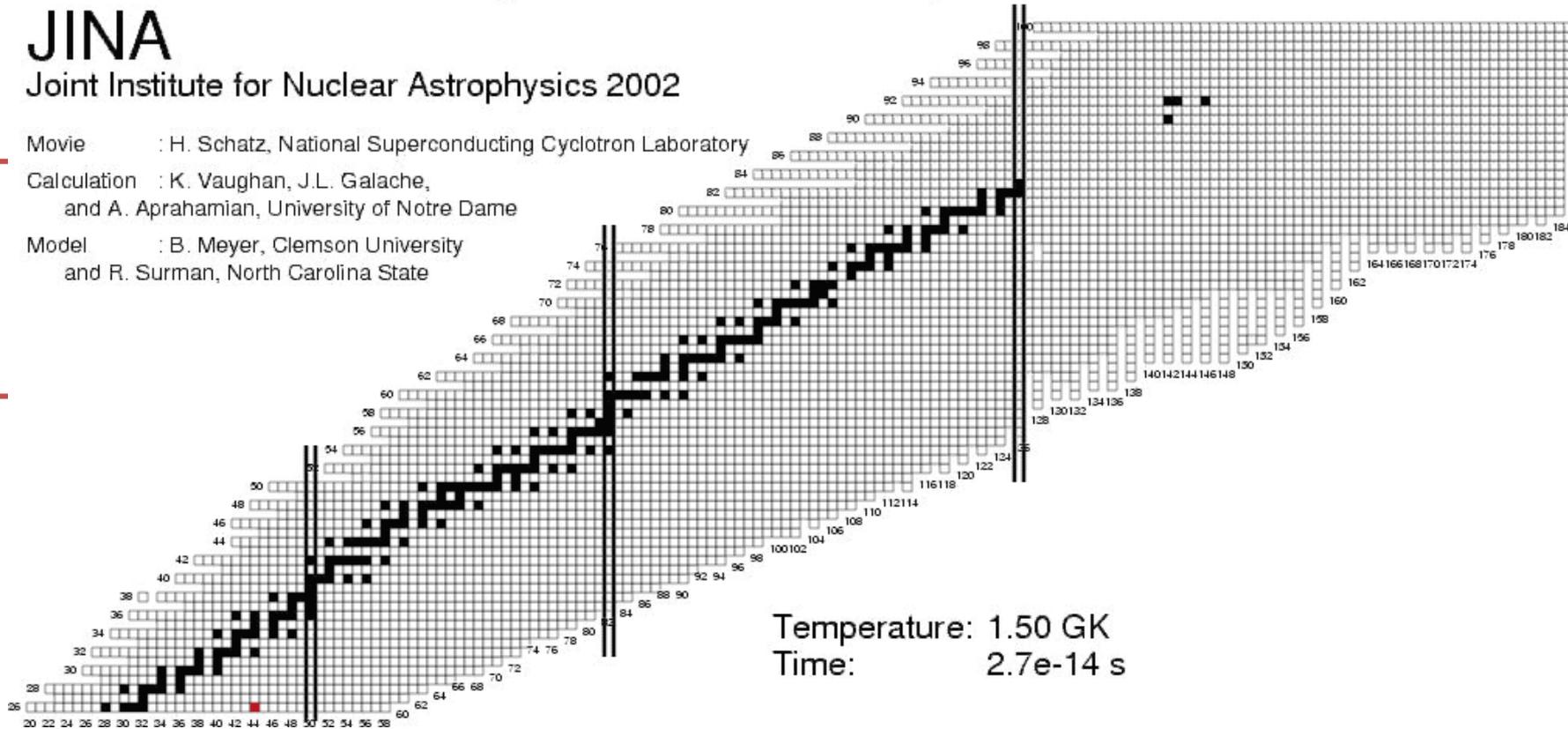
Nucleosynthesis in the r-process

JINA

Joint Institute for Nuclear Astrophysics 2002

- Pt — Movie : H. Schatz, National Superconducting Cyclotron Laboratory
Calculation : K. Vaughan, J.L. Galache,
and A. Aprahamian, University of Notre Dame
Model : B. Meyer, Clemson University
and R. Surman, North Carolina State

Xe —



Masses
beta-decay half-lives

First experiment: r-process in the Ni region

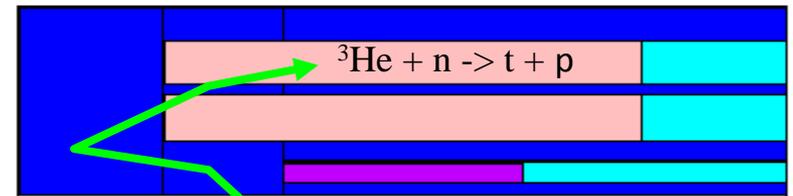
Hosmer et al. PRL 94, 112501 (2005)



Measure:

- β -decay half-lives
- Branchings for β -delayed n-emission

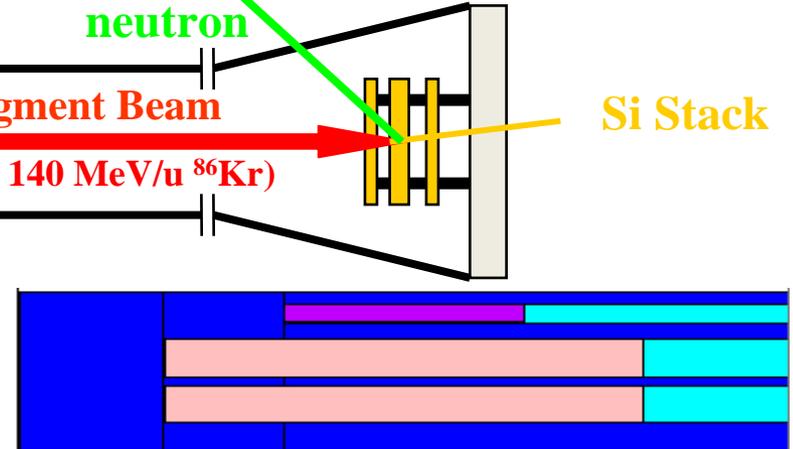
Neutron detector NERO



neutron

Fast Fragment Beam
(fragment. 140 MeV/u ${}^{86}\text{Kr}$)

Si Stack

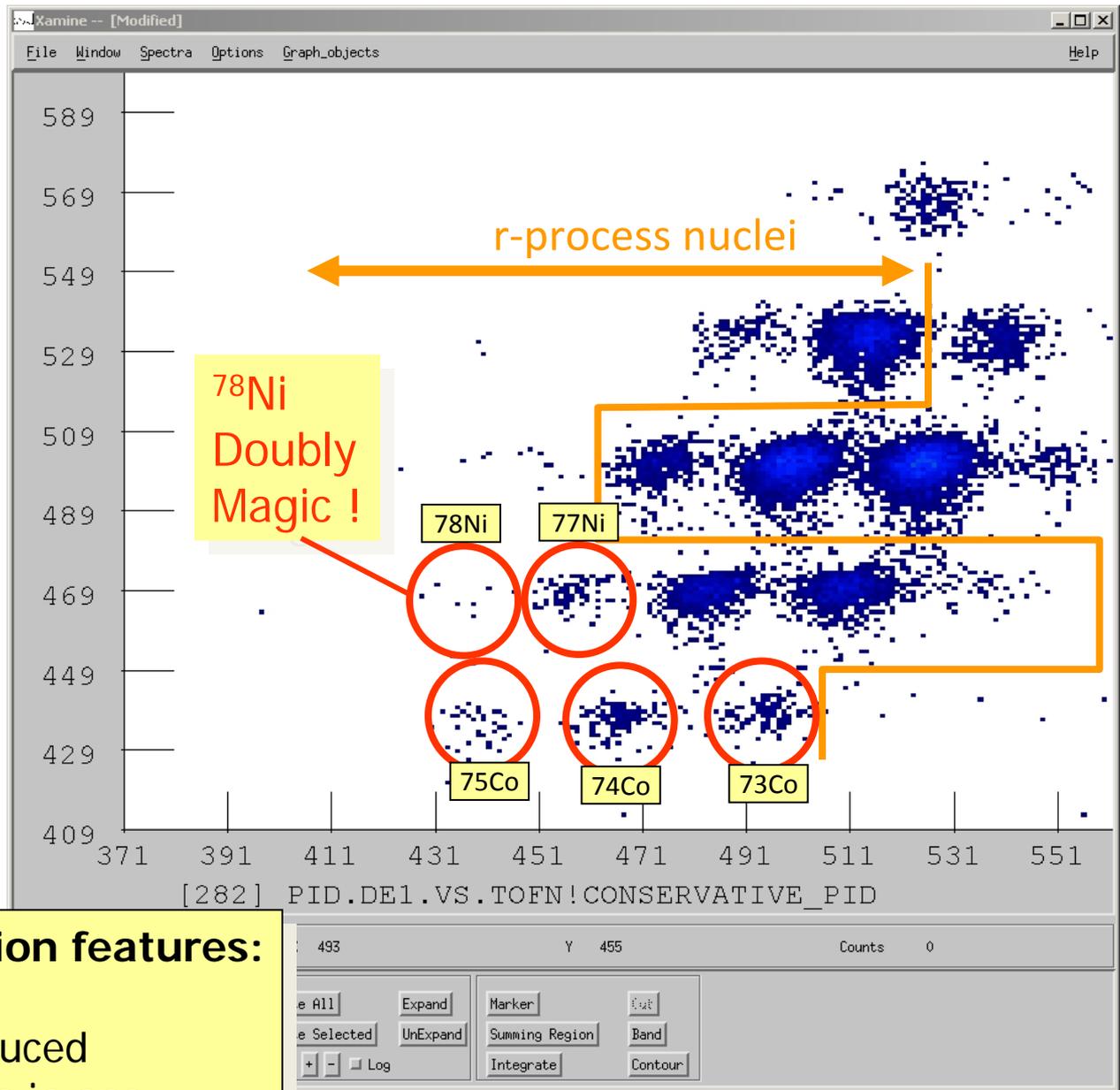


Detect:

- Particle type (TOF, dE, p)
- Implantation time and location
- β -emission time and location
- Neutron- β coincidences

Particle Identification:

Energy loss in Si $\sim Z$

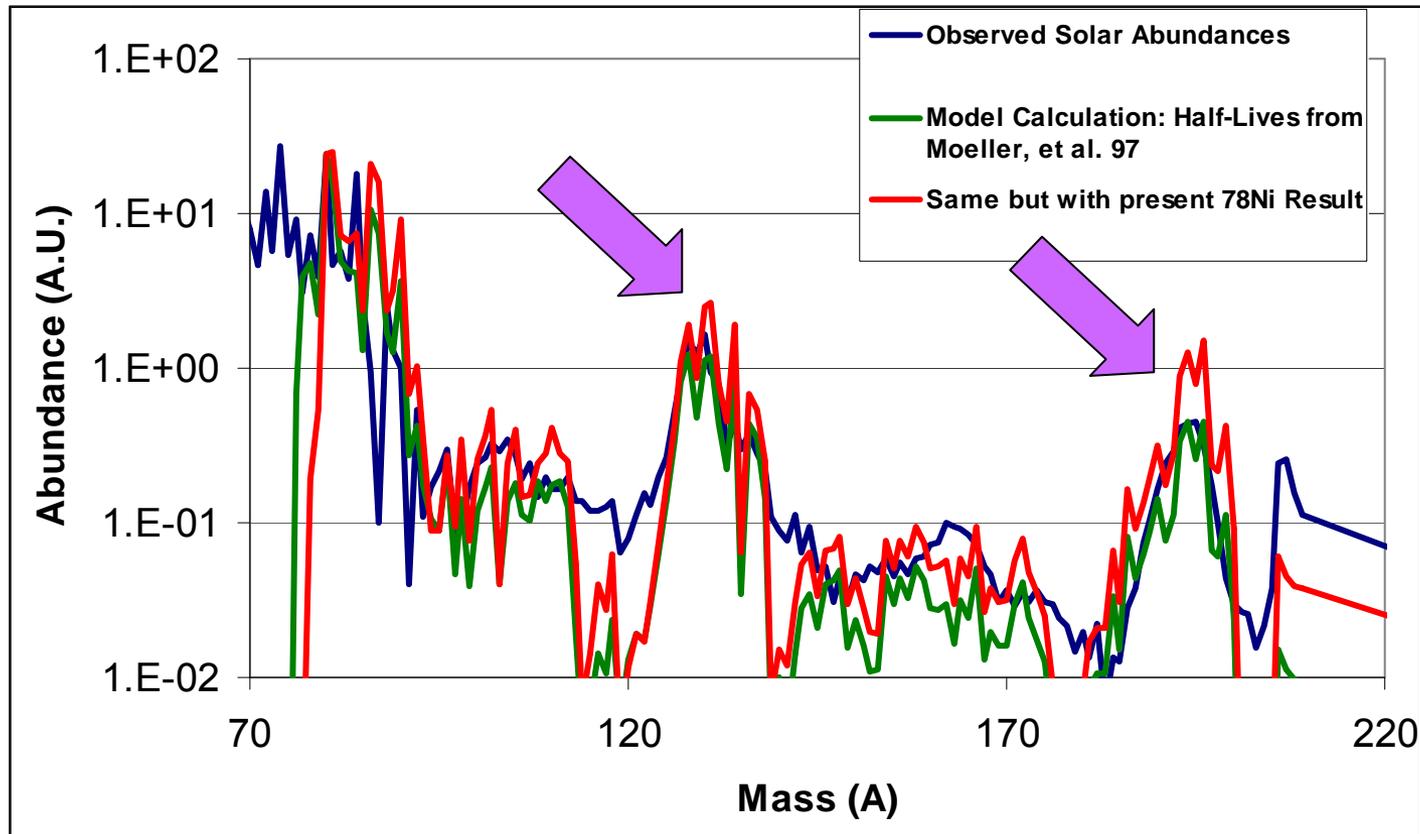


RIB from fragmentation features:

- no decay losses
- any beam can be produced
- multiple measurements in one
- high sensitivity

Time of flight $\sim m/q$

Impact of ^{78}Ni half-life on r-process models



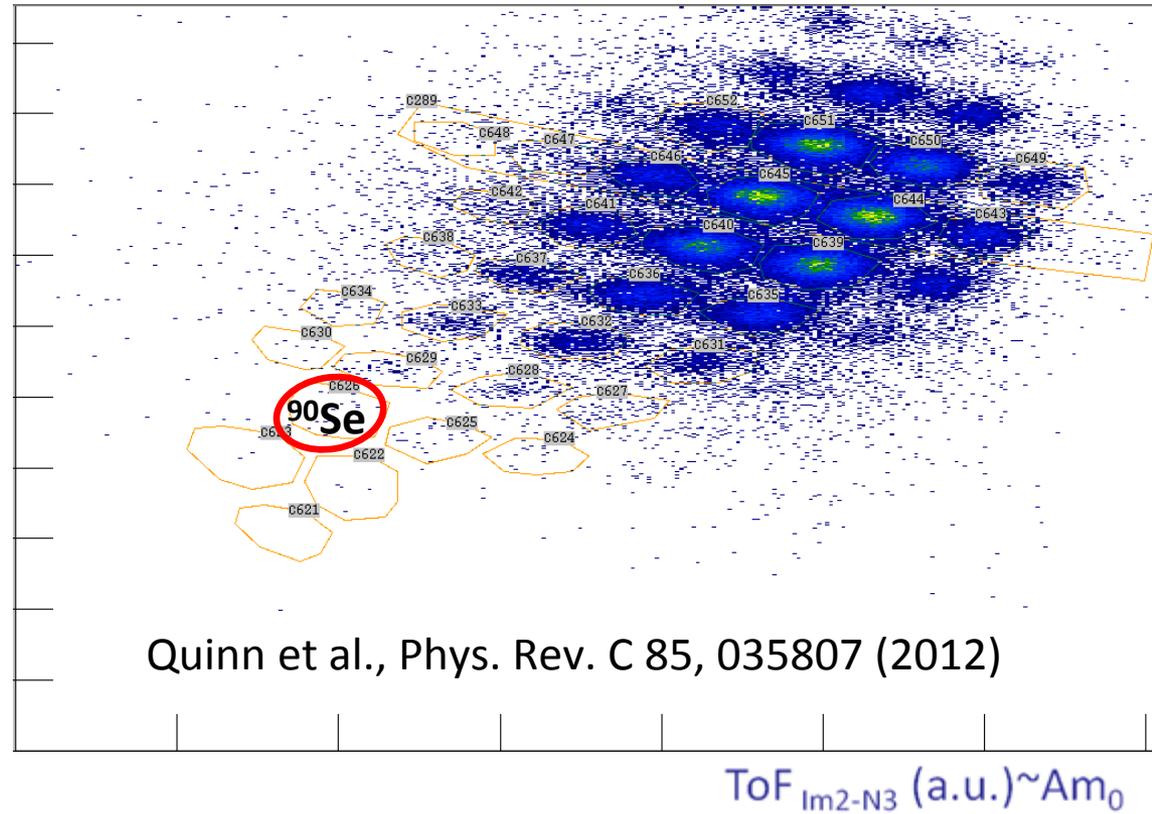
→ need to readjust r-process model parameters

→ Can obtain Experimental constraints for r-process models from observations and solid nuclear physics

N=56 subshell with Z=34???

Fragmentation of 120 MeV/u
 ^{136}Xe beam

ΔE_{PINO} (a.u.) $\sim Z^2$

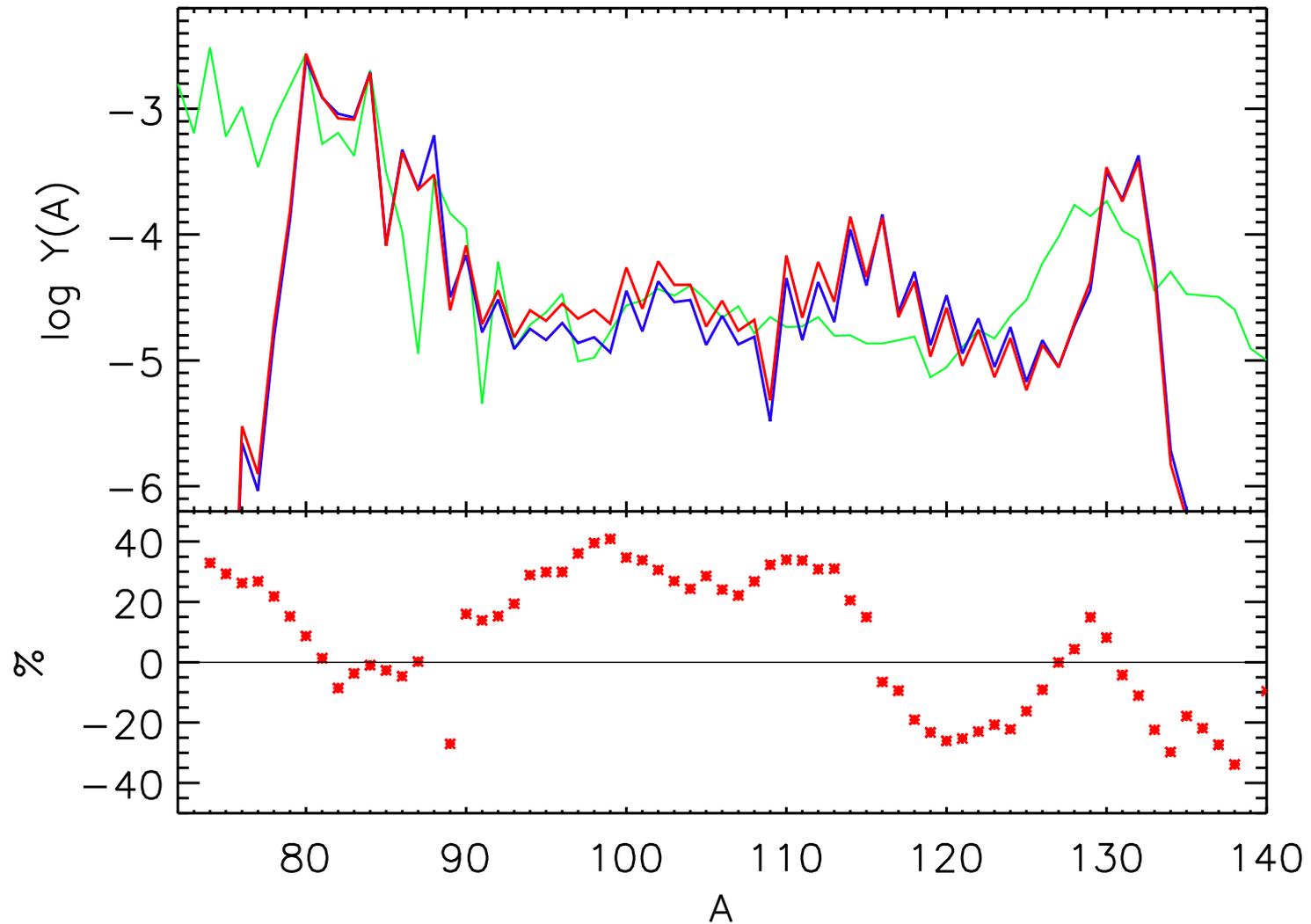


Implantations

Maximum Likelihood Method (ms)

^{87}As	27	12	$1450(550)_{-1250}^{+3900}$
^{88}As	16	8	$200(10)_{-90}^{+200}$
^{88}Se	144	74	$650(35)_{-140}^{+175}$
^{89}Se	180	90	$345(25)_{-80}^{+95}$
^{90}Se	70	30	$195(10)_{-65}^{+95}$

Impact of ^{90}Se half-life on r-process models



r-process sensitivities...masses

More quantitative approach to choosing to measure nuclei that would have the greatest impact on

What?

Brad Meyer code modified by R. Surman
various mass models-

FRDM, Duflo-Zuker, ETFSIQ, HFB-21, F-spin

Method:

Adjusted the separation energy of each nucleus $\pm 25\%$
(**3010 nuclei twice...**)

Calculated the max and fractional change from final abundances

What did we find?

Some consistent set of nuclei that are the most important to measure

So, What did we do?

Simulations.... Varied astrophysical conditions
varied seed nuclei
varied mass models

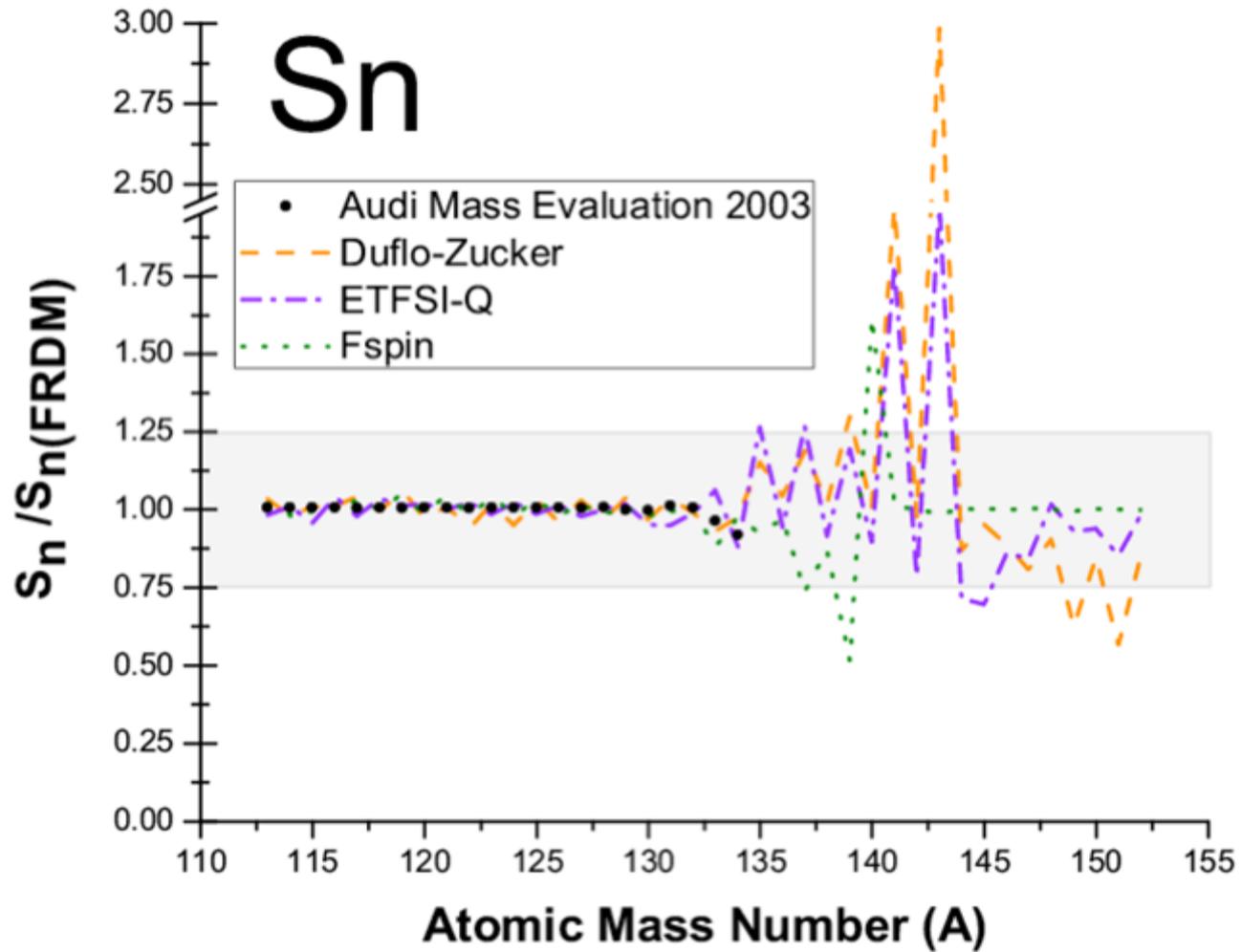
Input initial astrophysical conditions

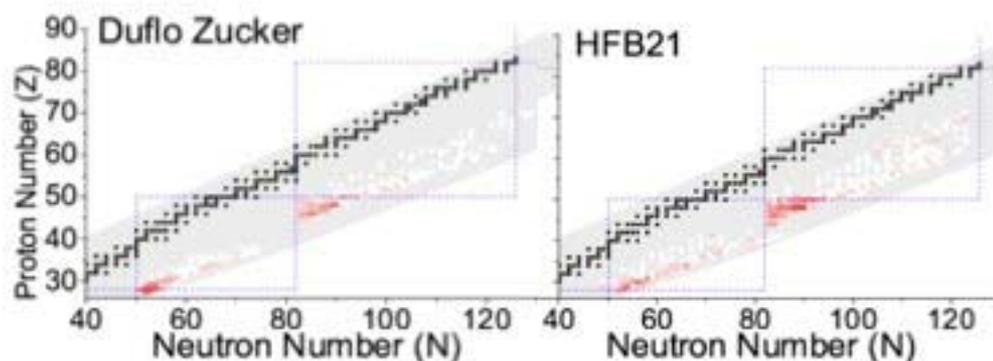
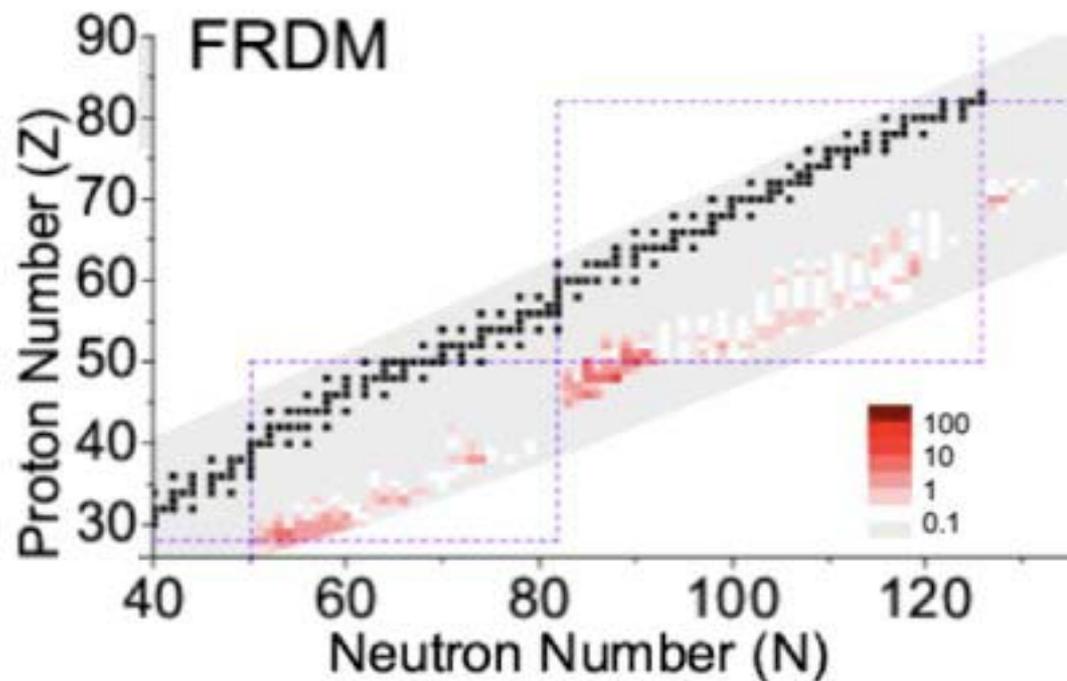
Temperature/density
neutron/seed ratios
Freeze-out times

Input nuclear physics

masses
n-capture rates
beta decay half-lives
(fission recycling, alpha recycling, neutrino interactions off)

Why 25%





$$\Delta Y_{\pm 25\%}(N, Z) = \sum_A |Y(A) - Y(A, \pm \Delta S_n(N, Z))|.$$

ΔY for FRDM

Nucleus	
¹³⁶ Cd	20.2
¹⁴⁰ Sn	12.1
¹³⁵ Cd	8.80
⁸³ Cu	8.42
¹³⁹ Sn	8.19
¹⁴² Sb	5.64
¹³⁵ Sn	5.44
¹³³ Cd	5.38
¹⁴⁰ Sb	5.25
¹³⁴ Cd	5.23
⁸² Cu	4.14
¹³⁴ In	4.14
¹³¹ Pd	3.29
¹³⁷ Sn	2.94
¹⁴¹ Sn	2.91
⁸³ Zn	2.89
⁸⁵ Zn	2.71
⁸⁵ Cu	2.66
¹³⁰ Pd	2.39
¹³² Pd	2.39

ΔY for ETFSI-Q

Nucleus	
¹⁴⁰ Sn	20.1
¹³⁶ Cd	19.0
¹⁴² Sn	17.3
¹³⁷ Cd	15.3
⁷⁹ Ni	12.5
⁸⁰ Ni	12.0
¹³⁵ Cd	11.5
¹³⁴ Cd	11.5
¹³⁸ Cd	8.57
¹³² Pd	7.66
¹³⁰ Pd	7.34
¹³² In	7.33
¹²⁹ Pd	5.12
¹³⁹ Sn	4.63
¹³¹ Pd	4.37
¹³⁸ In	3.98
¹³⁹ In	3.95
⁸⁶ Zn	3.21
¹⁴¹ Sn	2.92
⁸⁵ Zn	2.86

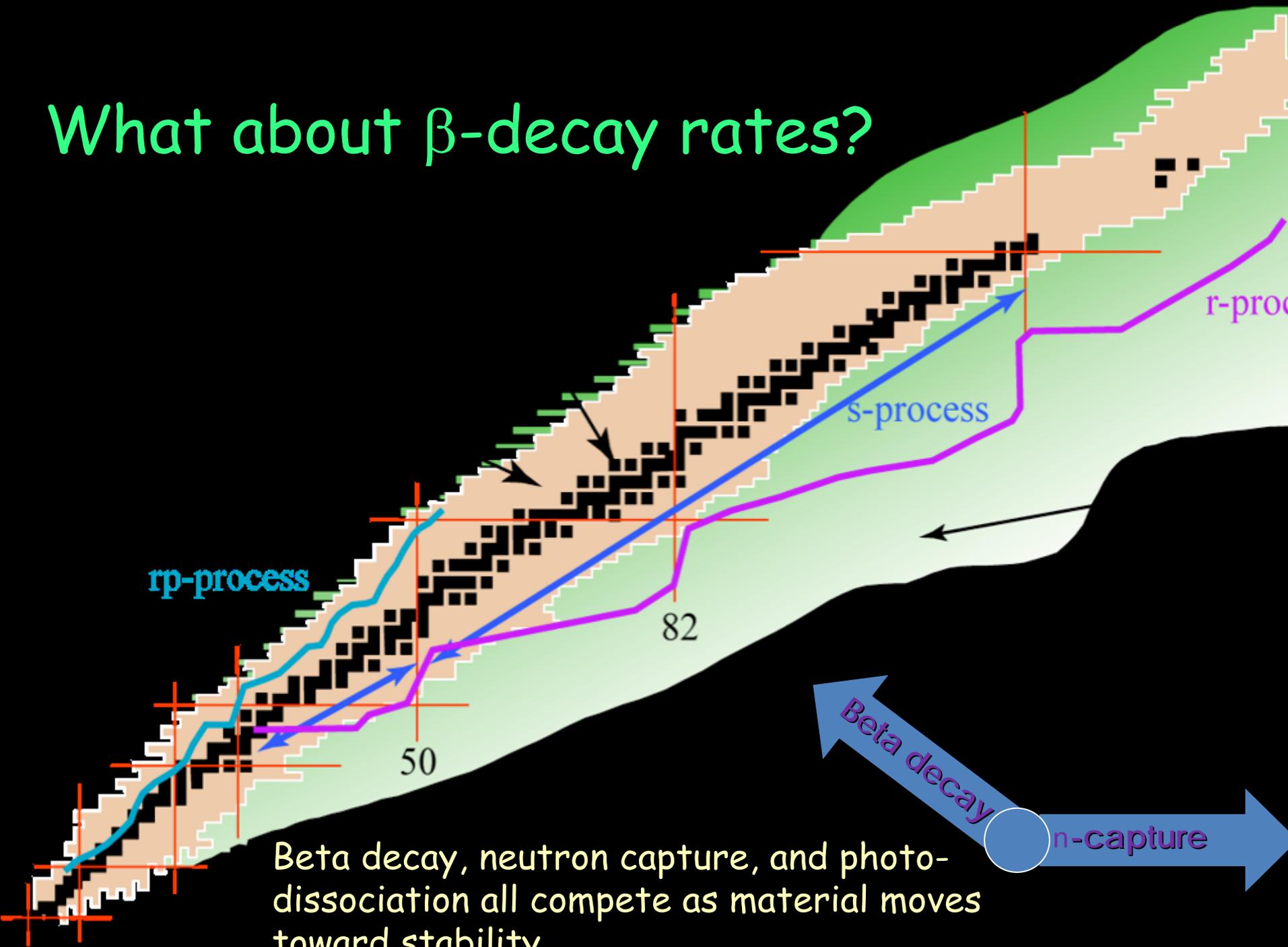
ΔY for DZ

Nucleus	
⁸⁰ Ni	13.63
⁷⁹ Ni	9.96
¹³⁸ Cd	7.08
¹³⁷ Cd	5.49
⁸³ Cu	4.27
¹³¹ Pd	3.54
⁸² Cu	3.36
¹³² Pd	3.12
¹³⁶ Cd	3.00
¹³⁰ Pd	2.97
⁸⁶ Zn	2.84
¹²⁹ Pd	1.88
⁸⁵ Zn	1.81
¹³⁴ Ag	1.49
¹⁴² Sn	1.42
¹³⁵ Ag	1.39
¹³⁵ Cd	1.36
¹³³ Cd	1.10
¹⁴¹ Sn	1.08
¹⁴⁴ Sn	1.07

- The same isotopes are present in each evaluation:

- Sn, Sb, and In,
- Cd,
- Pd,
- Cu, Zn, and Ni.

What about β -decay rates?



Beta decay, neutron capture, and photo-dissociation all compete as material moves toward stability

So, What are we doing?

Simulations..... Varied astrophysical conditions
varied seed nuclei
varied mass models
varied beta-decay rates

Input initial astrophysical conditions

Temperature/density
neutron/seed ratios
Freeze-out times

Input nuclear physics

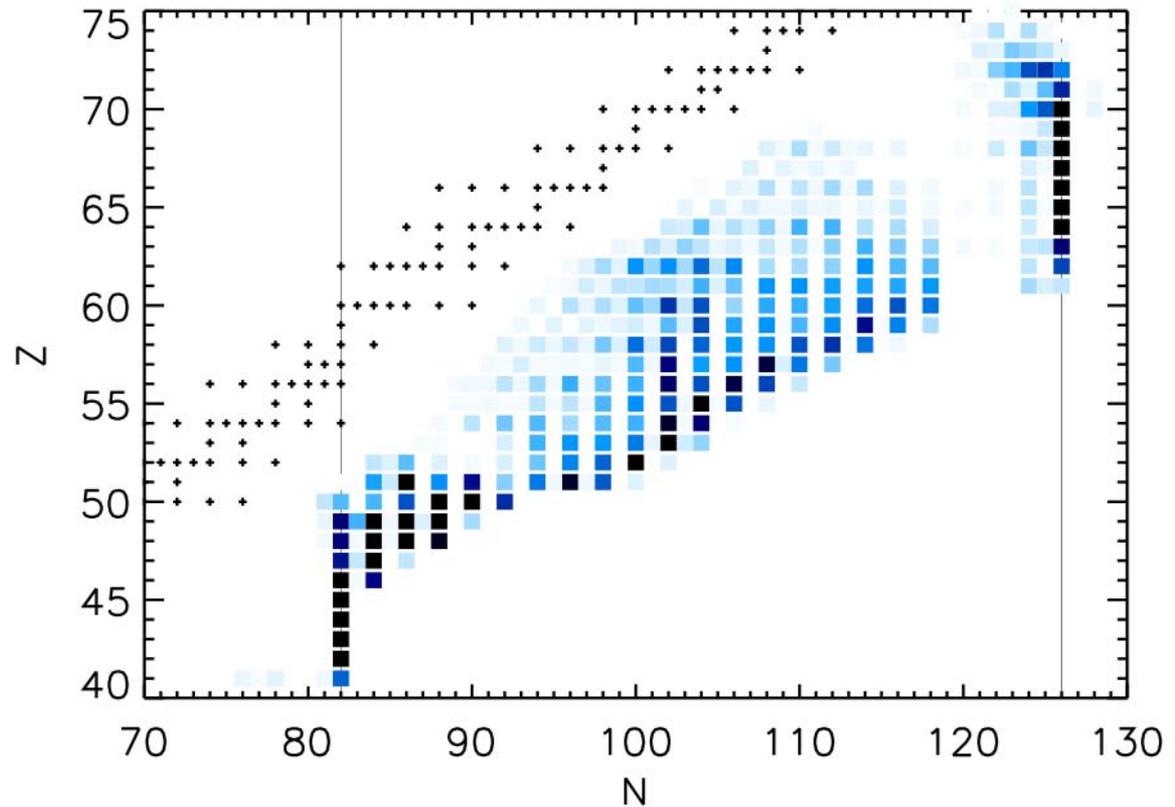
masses
n-capture rates
beta decay half-lives
(fission recycling, alpha recycling, neutrino interactions off)

r-process sensitivities...beta-decay rates

J. Cass, G. Passucci, R. Surman, A. Aprahamian

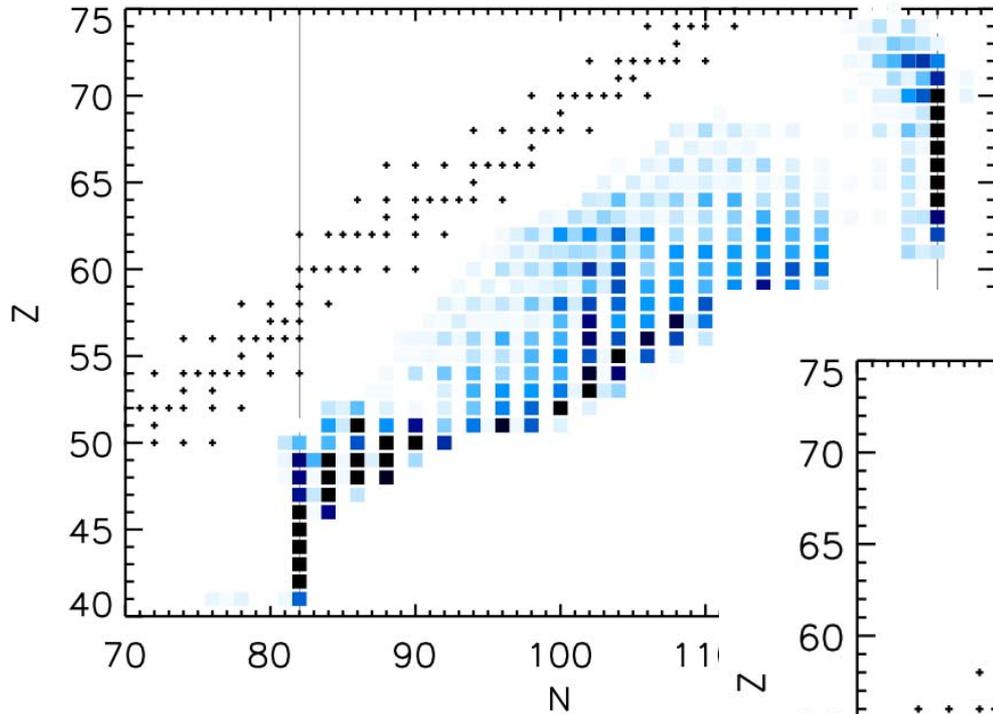
To start...

Vary one beta decay rate by an order of magnitude, rerun the simulation, and compare the final abundance pattern to the baseline

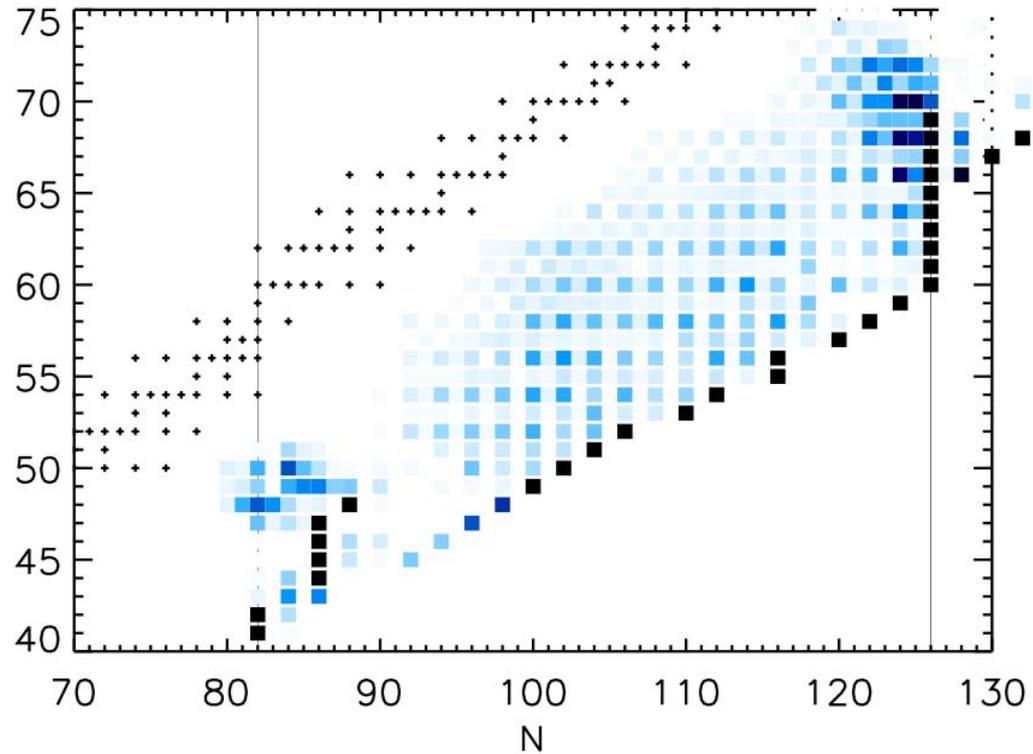


White to black = 0-10% change in the final abundance patterns

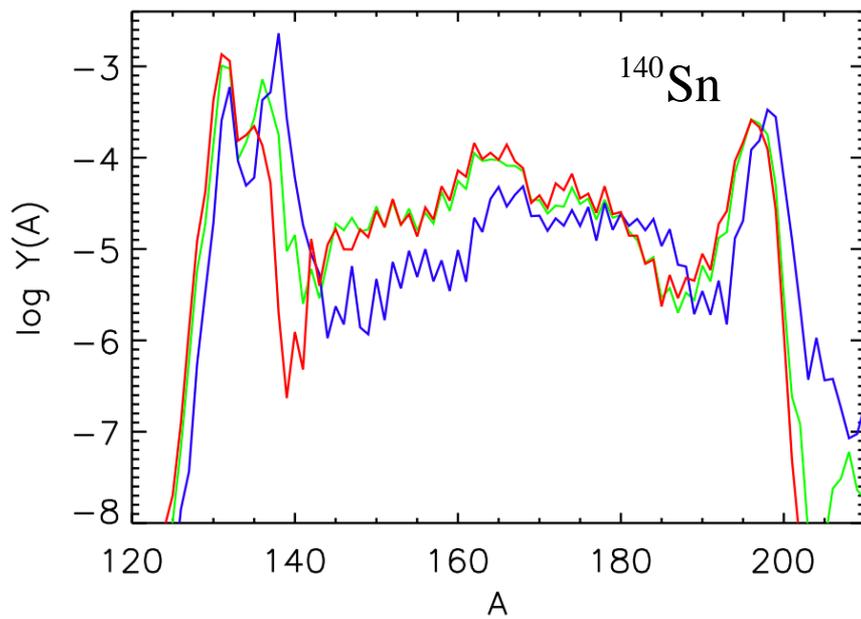
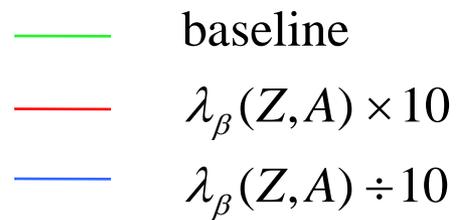
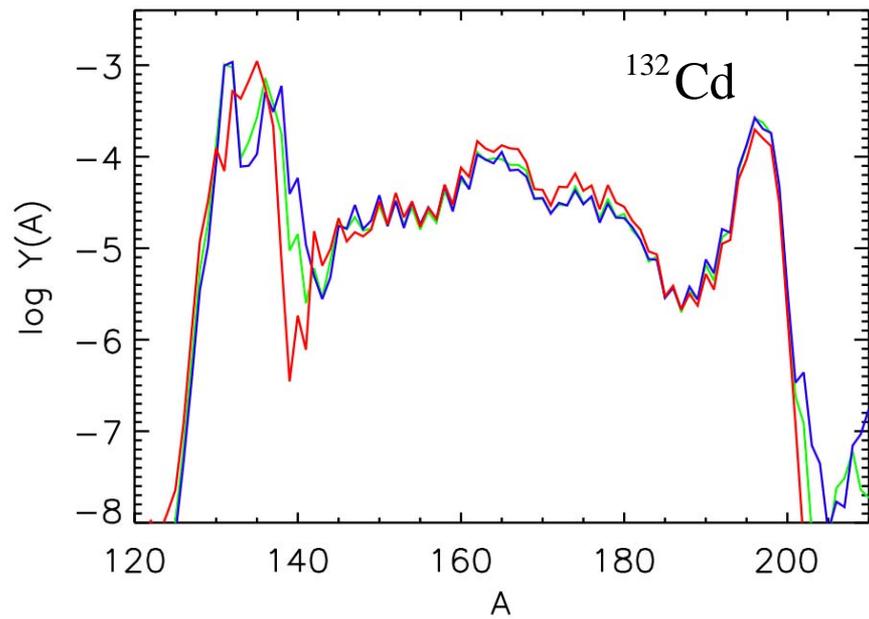
Beta decay rate sensitivity study



hot r-process



cold r-process



conclusions

We have carried out the first quantitative/comprehensive sensitivity study of an r-process simulation to masses, beta decay rates, neutron capture cross sections.

- we varied mass models
- we varied decay rates
- consistent set of nuclei that we

Sensitivity Study Masses

Samuel Brett

Ian Bentley

Nancy Paul

Rebecca Surman

A²

Sensitivity Study β -decay rates

Julie Cass

Giuseppe Passucci

Rebecca Surman

A²



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Alfredo Estrade

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Giuseppe Lorusso

Milan Matos

Fernando Montes

Mainz

Stefan Hennrich

Karl-Ludwig Kratz

Bernd Pfeiffer

Ruben Kessler

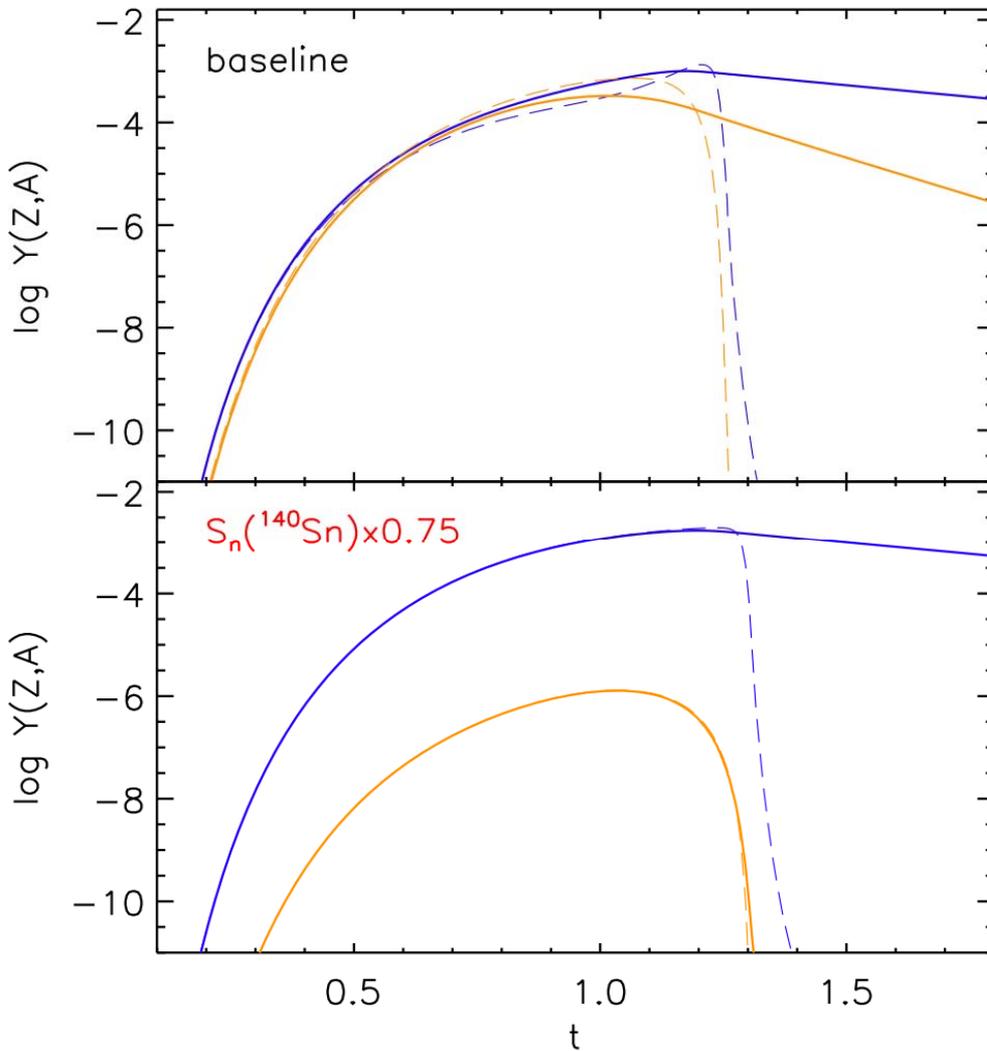
Florian Schertz

Univ. of Maryland

W. Walters



The role of neutron separation energies in a hot r -process



- $Y(50,138)$, abundance of ^{138}Sn
- $Y(50,140)$, abundance of ^{140}Sn
- - - $Y_{\text{equilibrium}}(50,138)$
- - - $Y_{\text{equilibrium}}(50,140)$

While in equilibrium, the relative abundances along an isotopic chain are given by a Saha equation:

$$\frac{Y_{\text{equilibrium}}(Z, A+1)}{Y_{\text{equilibrium}}(Z, A)} = \frac{G(Z, A+1)}{2G(Z, A)} n_n \left(\frac{2\pi\hbar^2 N_A}{m_n kT} \right)^{3/2} \exp\left[\frac{S_n(Z, A+1)}{kT} \right]$$

ΔY for FRDM

Nucleus	ΔY
¹³⁶ Cd	20.2
¹⁴⁰ Sn	12.1
¹³⁵ Cd	8.80
⁸³ Cu	8.42
¹³⁹ Sn	8.19
¹⁴² Sb	5.64
¹³⁵ Sn	5.44
¹³³ Cd	5.38
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¹³⁴ Cd	5.23
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¹³⁴ In	4.14
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⁸⁶ Zn	3.21
¹⁴¹ Sn	2.92
⁸⁵ Zn	2.86

ΔY for DZ

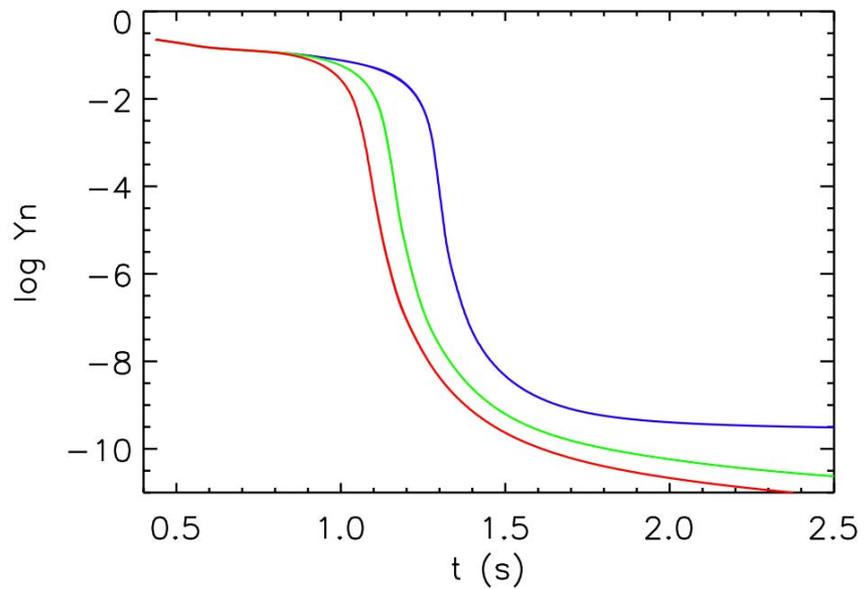
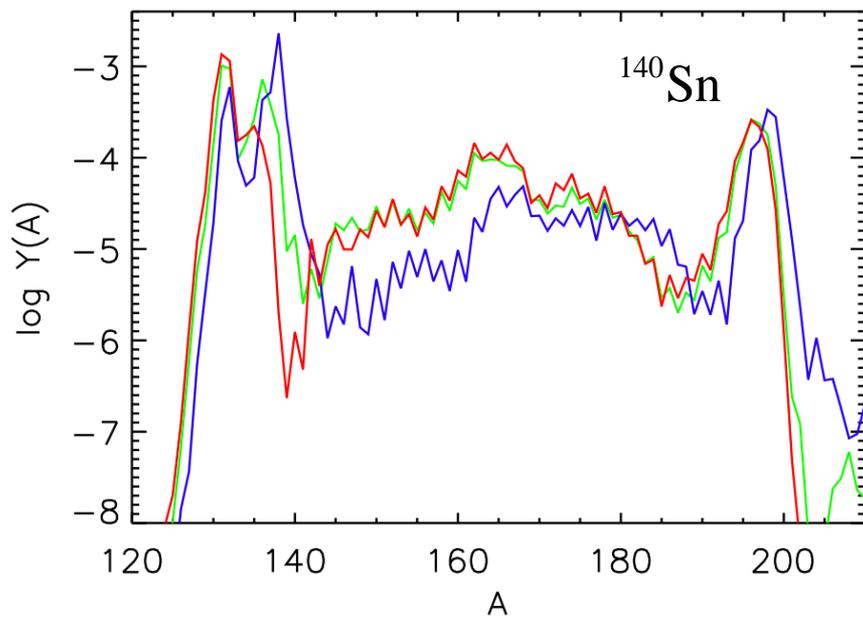
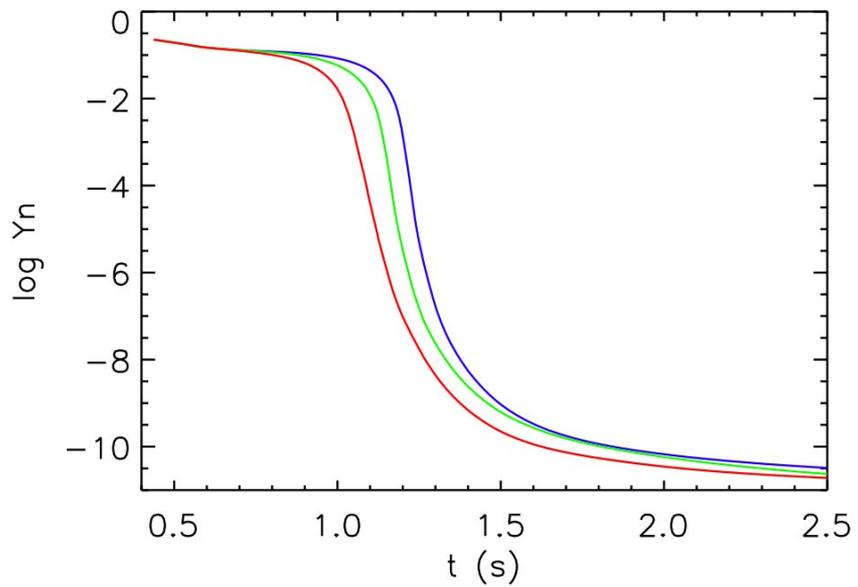
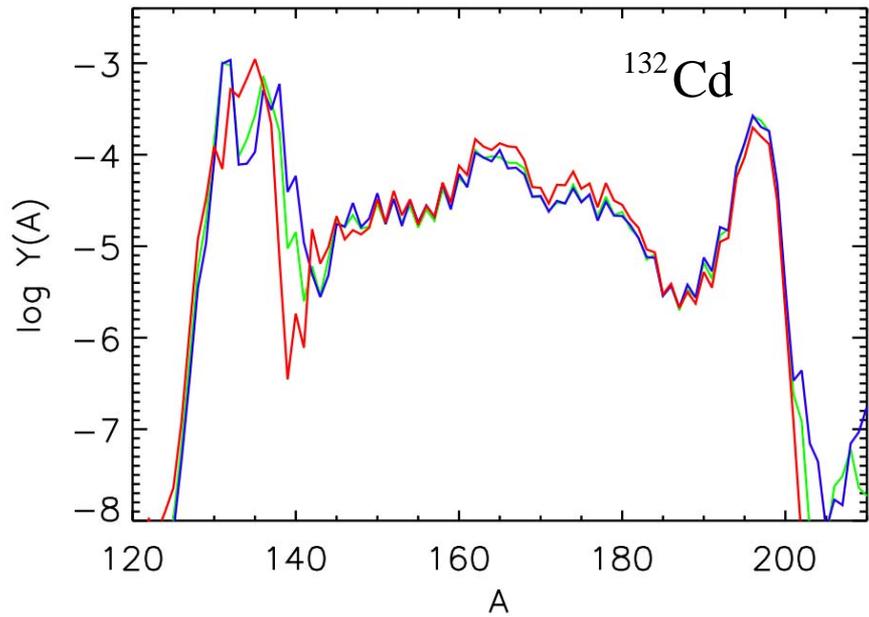
Nucleus	ΔY
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- Pd,
- Cu, Zn, and Ni.

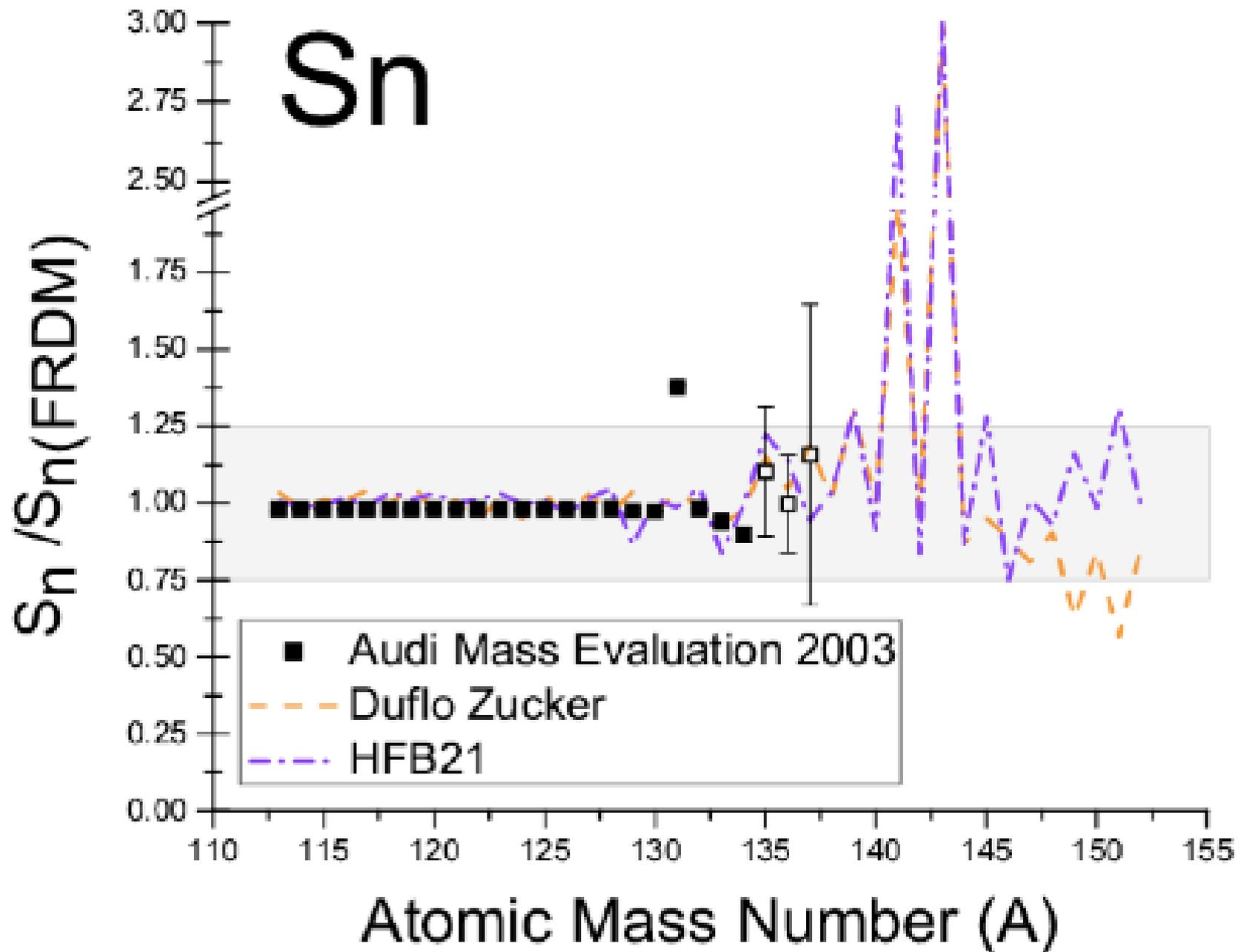
CARIBU possibilities

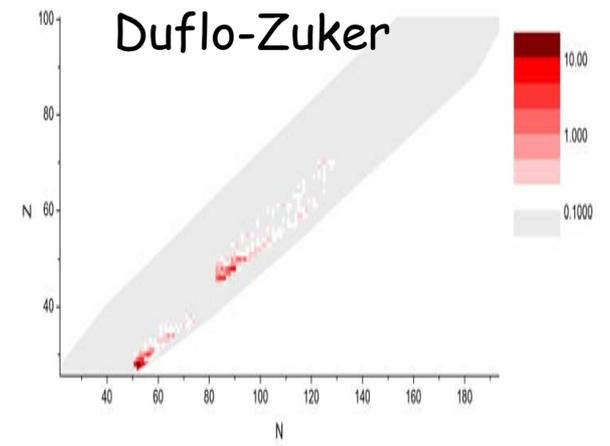
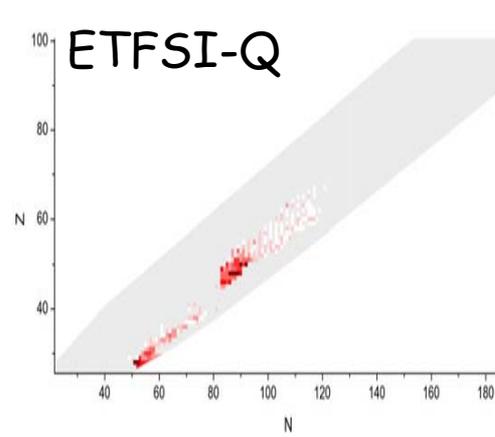
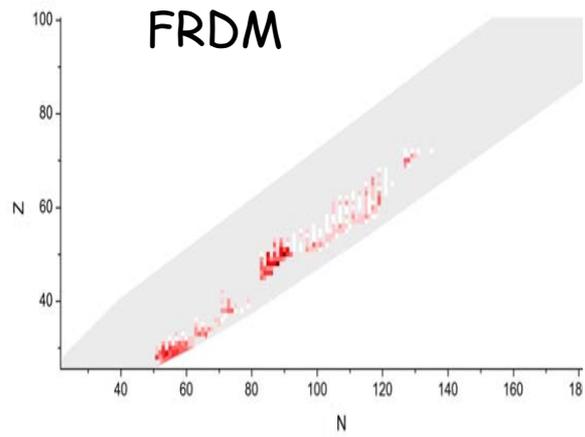
¹³⁰ In	10 ⁴	900
¹³³⁻¹³⁴ Sn	10 ⁴	10 ³
¹²⁸⁻¹³⁶ Sb		
¹¹³⁻¹¹⁹ Pd		
¹²⁰⁻¹²¹ Ag		



Why 25%

Sn





$$\Delta Y_{\pm 25\%}(N, Z) = \sum_A |Y(A) - Y(A, \pm \Delta S_n(N, Z))|.$$

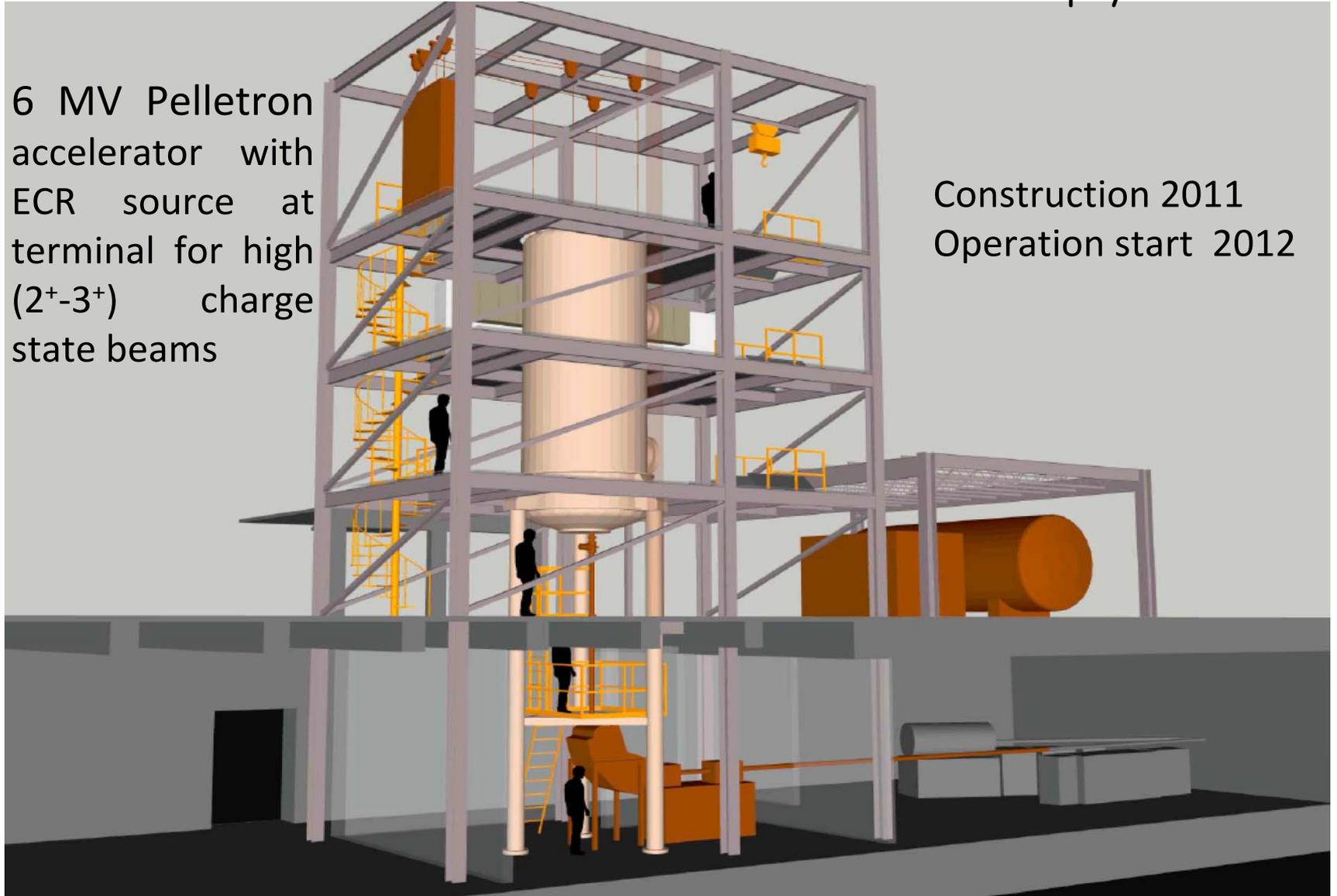
Absolute differences

Heavy Ion Accelerator at Notre Dame

Sta. ANA: Stable beam Accelerator for Nuclear Astrophysics

6 MV Pelletron
accelerator with
ECR source at
terminal for high
(2^+ - 3^+) charge
state beams

Construction 2011
Operation start 2012

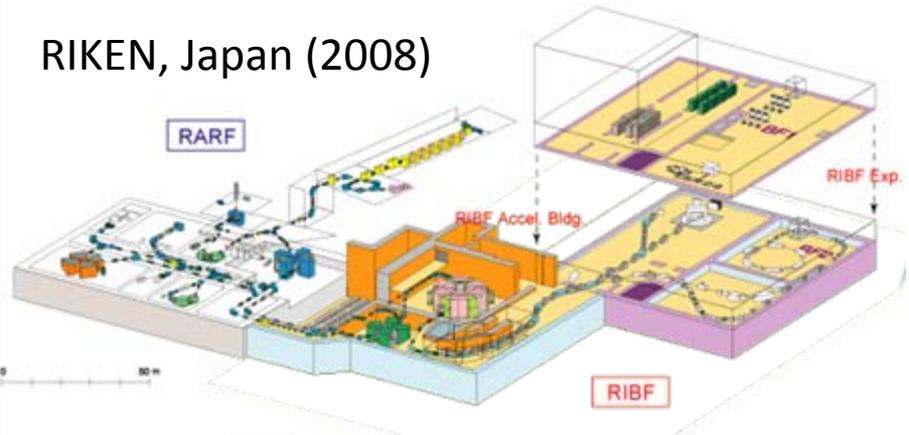


Delivery of Sta. ANA

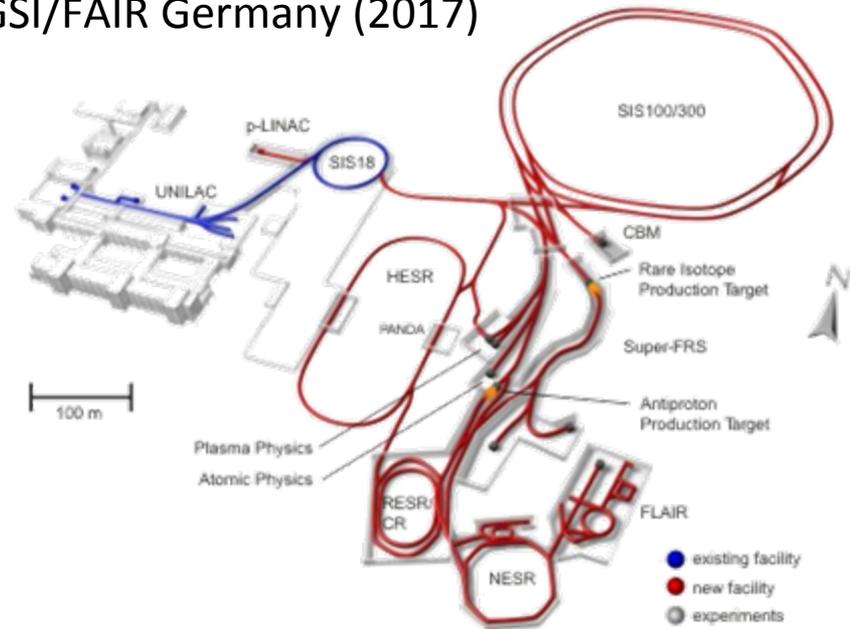




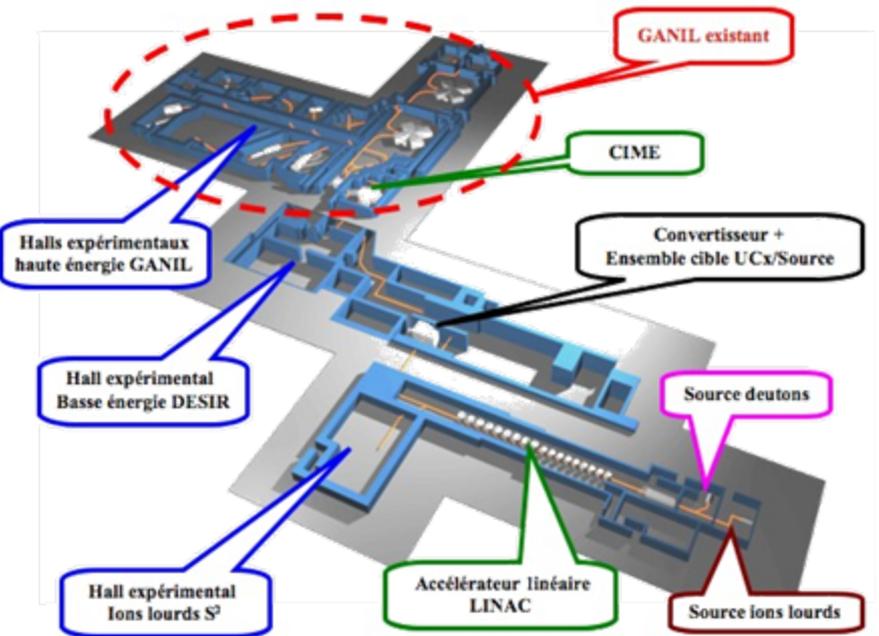
RIKEN, Japan (2008)



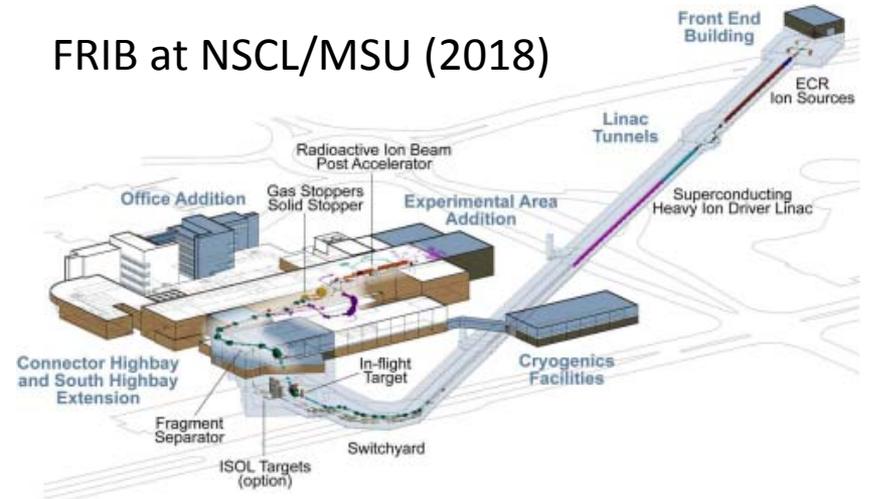
GSI/FAIR Germany (2017)



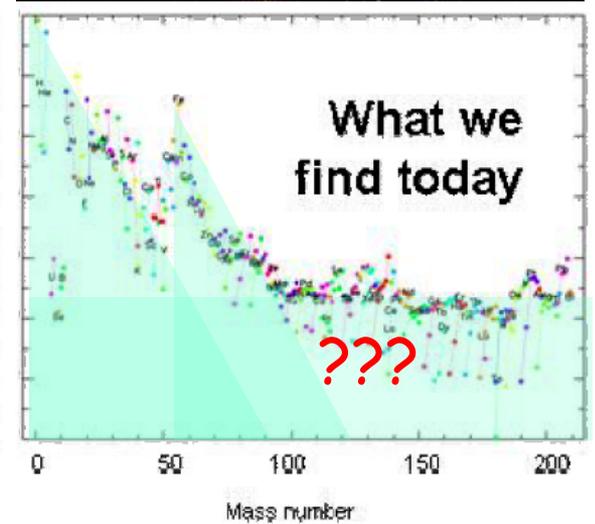
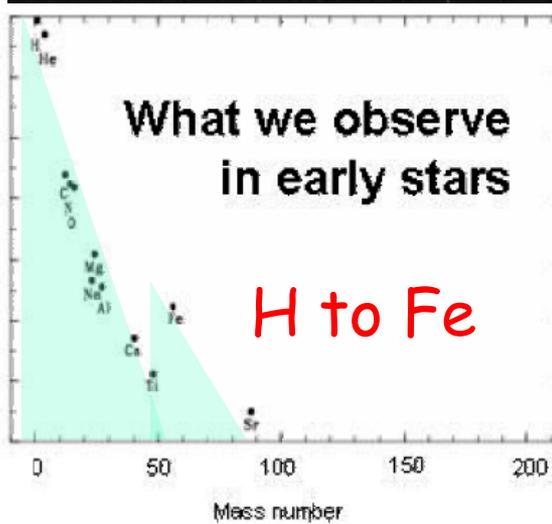
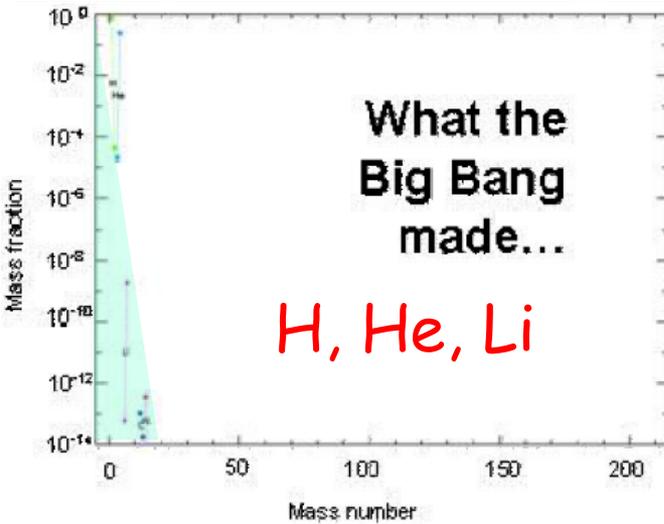
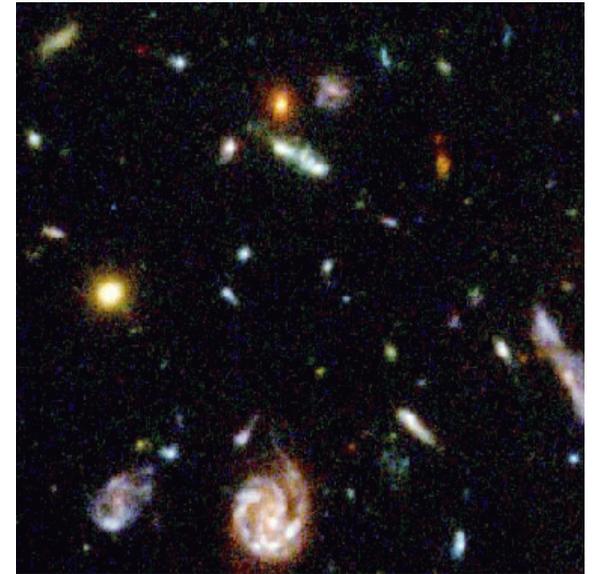
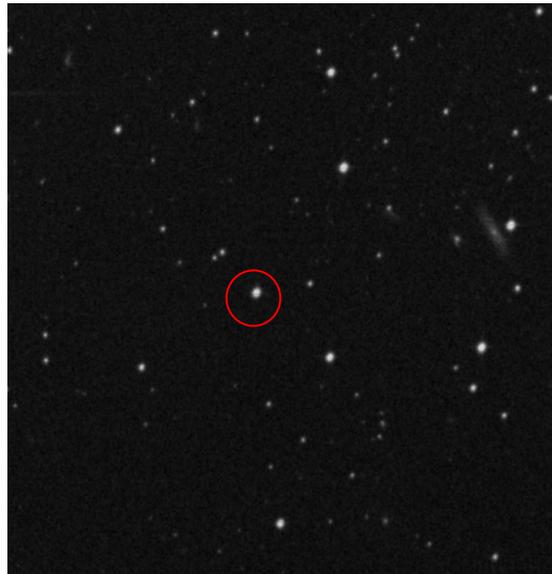
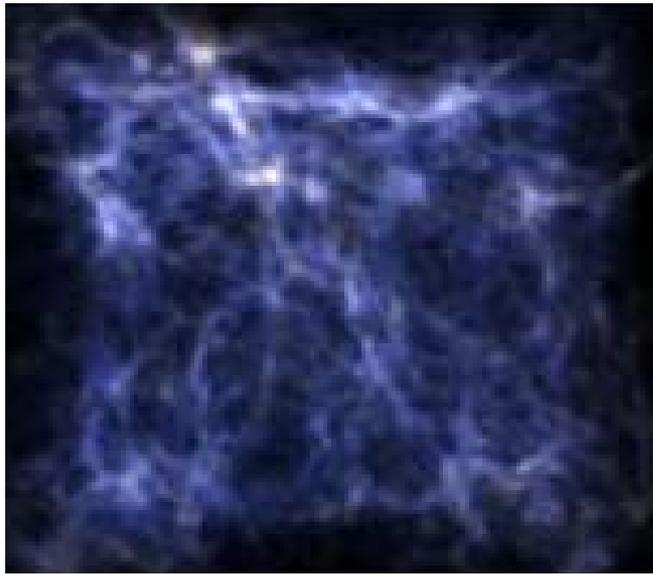
GANIL, France (2013)



FRIB at NSCL/MSU (2018)



Elemental history of the universe

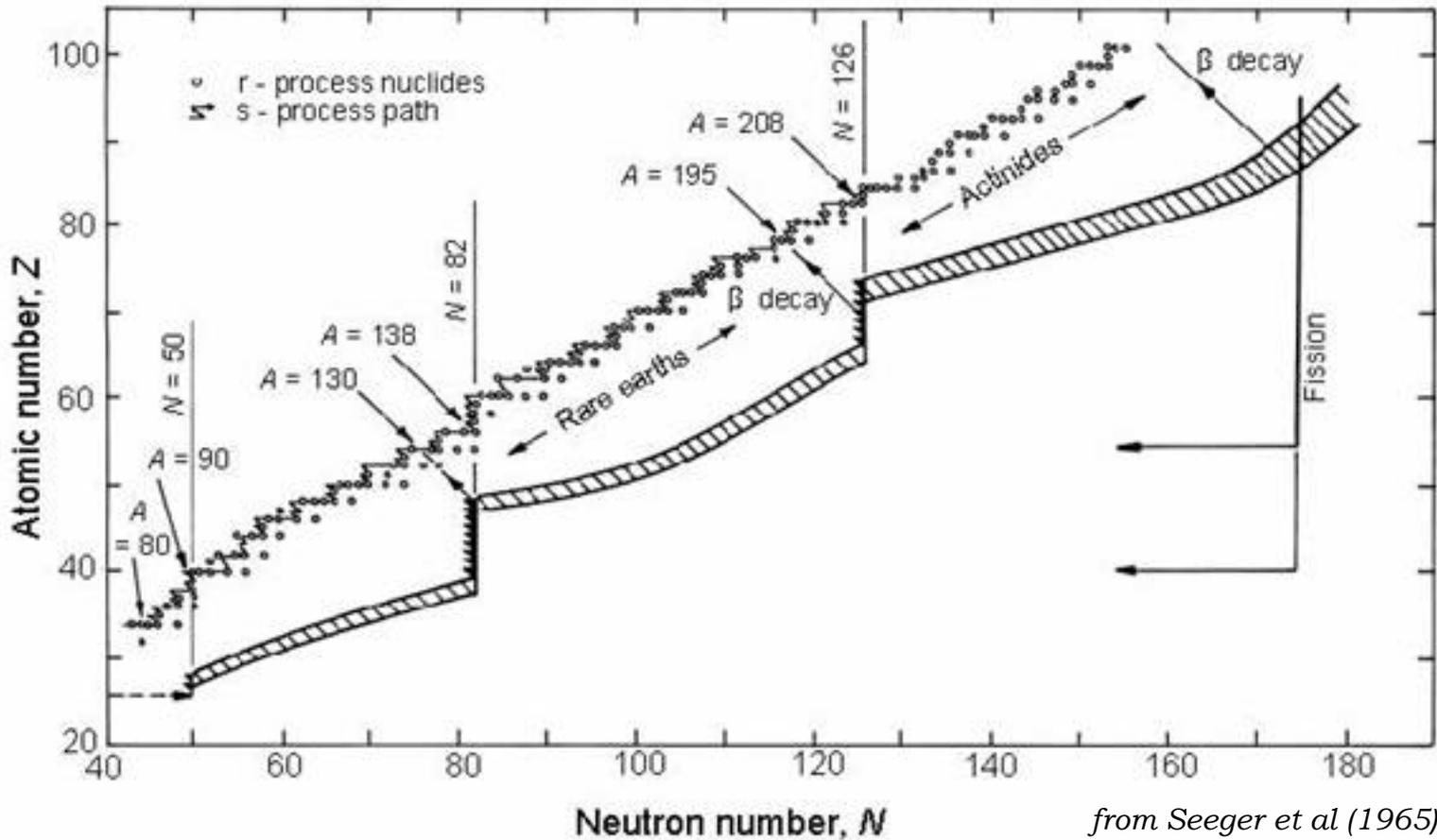


(The primordial abundance pattern)
Brian Fields (2002)

(The abundance pattern in the oldest
observed stars He1017 & HH1327)
Anna Frebel (2006)

(The solar abundance pattern)
Grevesse & Noels (1995)

Hot r -process: (n,γ) - (γ,n) equilibrium



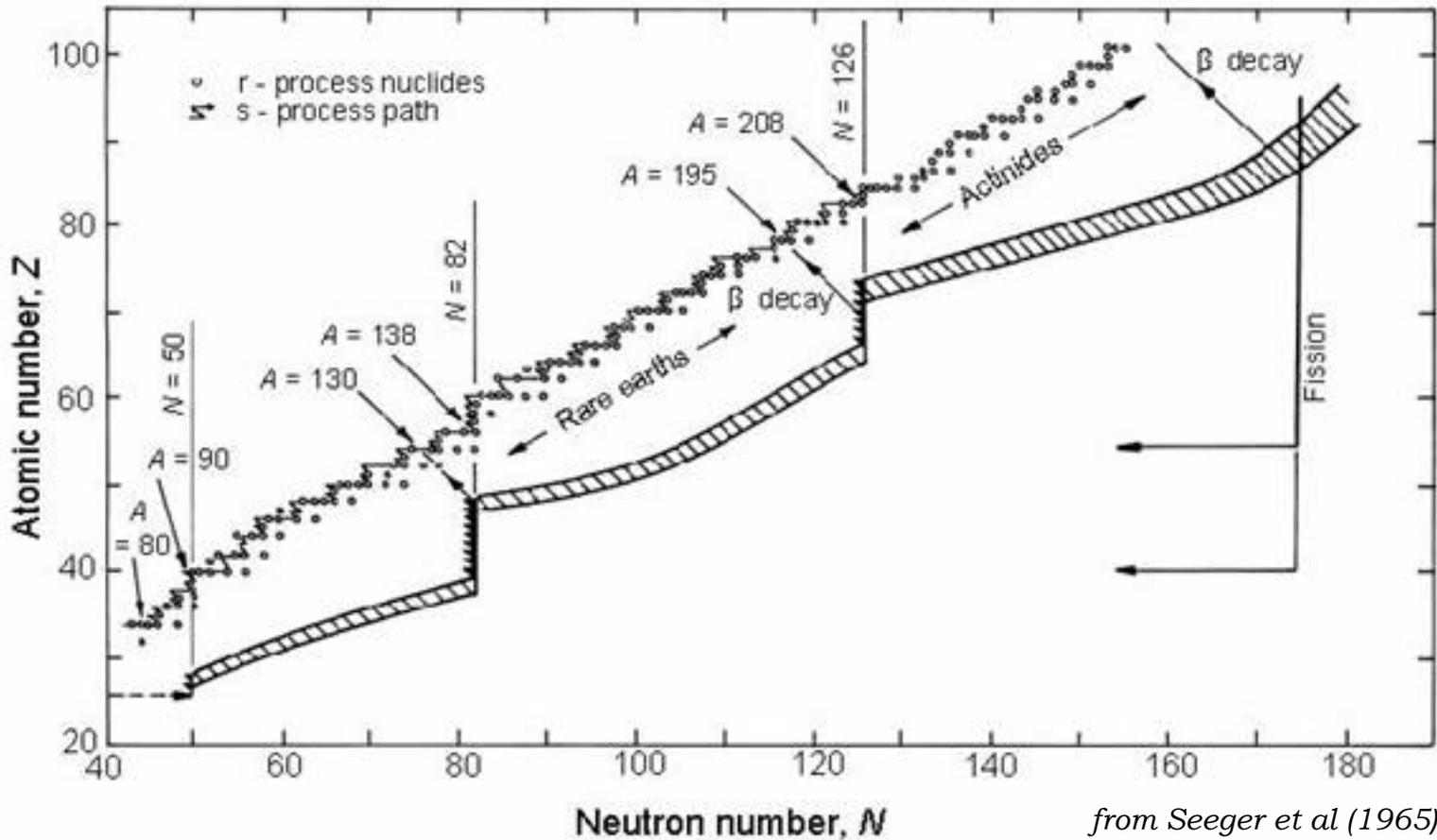
$$S_n(Z, A_{path}) \sim -kT \ln \left\{ \frac{n_n}{2} \left(\frac{2\pi\hbar^2}{m_n kT} \right)^{3/2} \right\}$$

$$S_n(Z, A) = B.E.(Z, A) - B.E.(Z, A - 1)$$

n_n neutron number density

T temperature

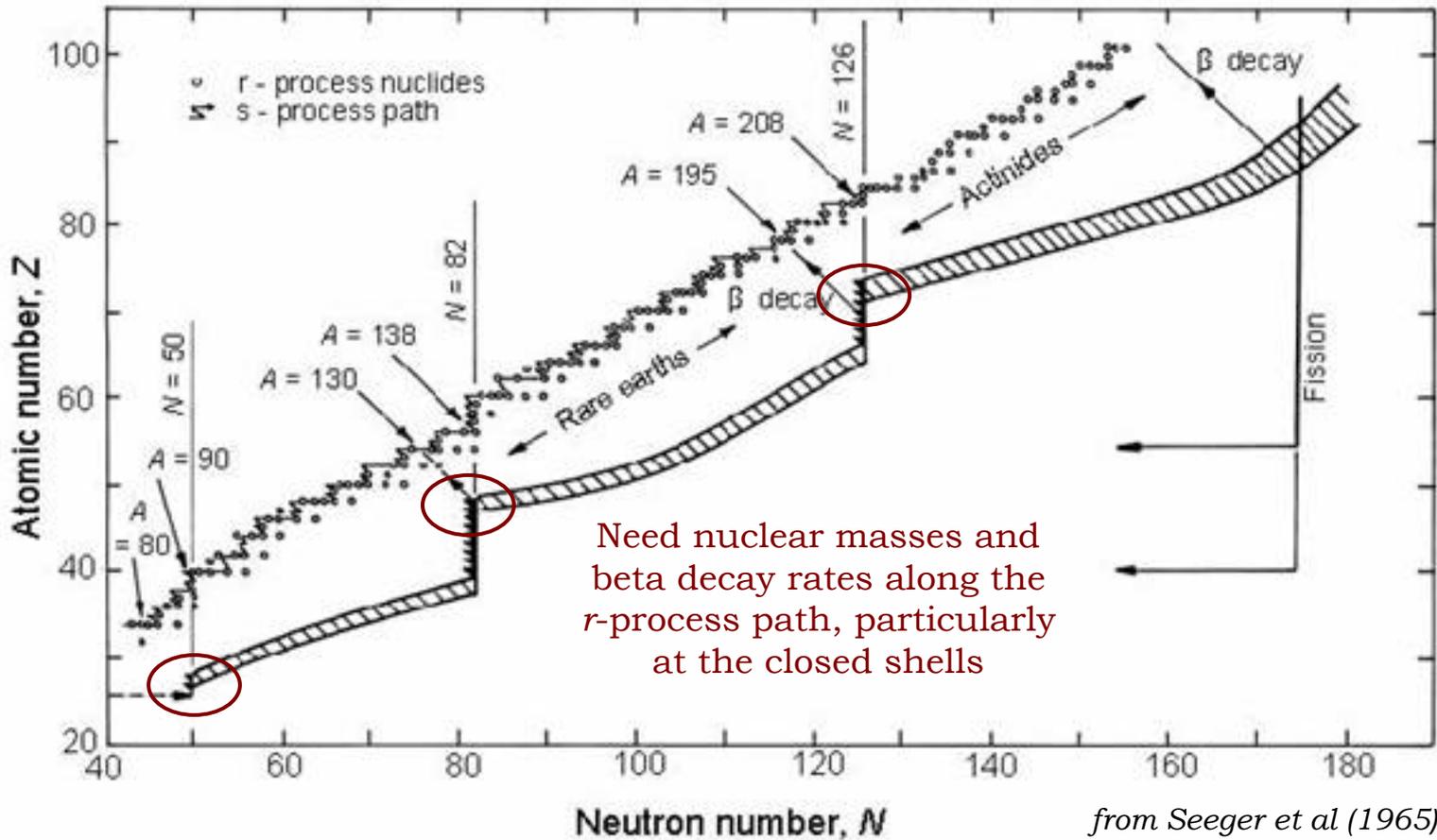
Hot r -process: (n,γ) - (γ,n) equilibrium



$$S_n(Z, A_{path}) \sim -kT \ln \left\{ \frac{n_n}{2} \left(\frac{2\pi\hbar^2}{m_n kT} \right)^{3/2} \right\}$$

$$\lambda_\beta(Z, A_{path}) Y(Z, A_{path}) \sim \text{constant}$$

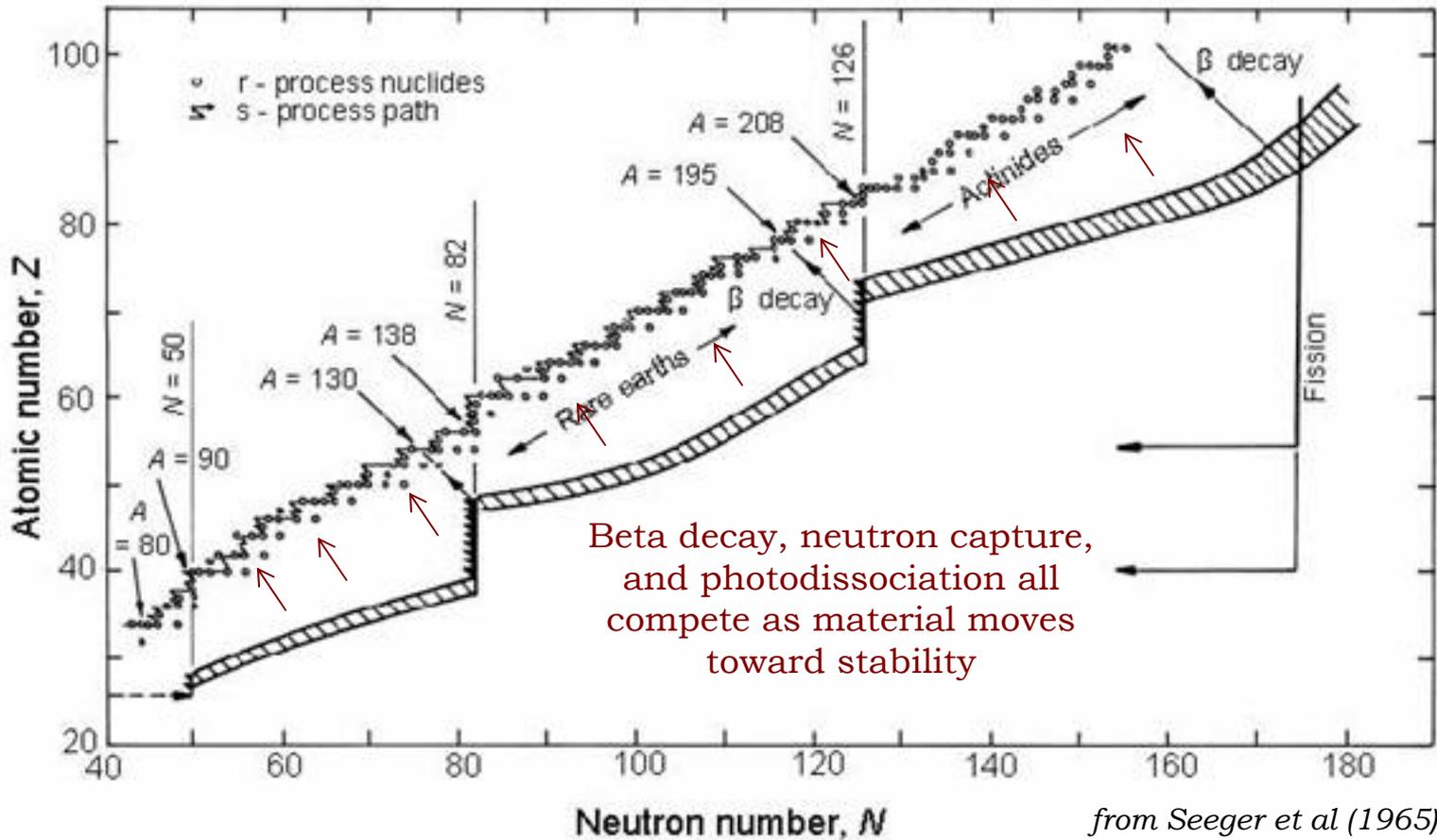
Hot r -process: (n,γ) - (γ,n) equilibrium



$$S_n(Z, A_{path}) \sim -kT \ln \left\{ \frac{n_n}{2} \left(\frac{2\pi\hbar^2}{m_n kT} \right)^{3/2} \right\}$$

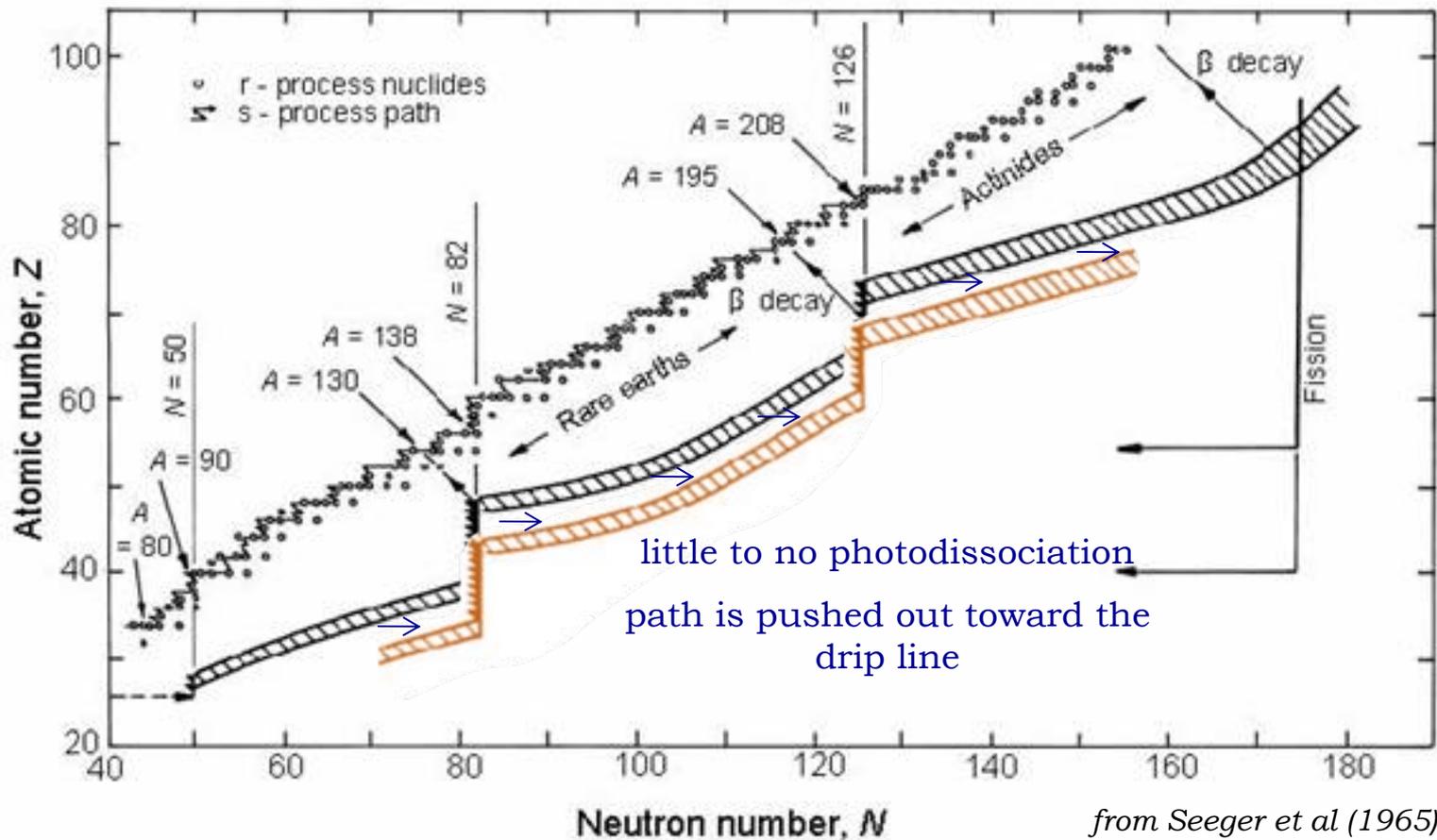
$$\lambda_\beta(Z, A_{path}) Y(Z, A_{path}) \sim \text{constant}$$

Hot r -process: freezeout from (n,γ) - (γ,n) equilibrium



Individual neutron capture and photodissociation rates become important in shaping the final abundance pattern.

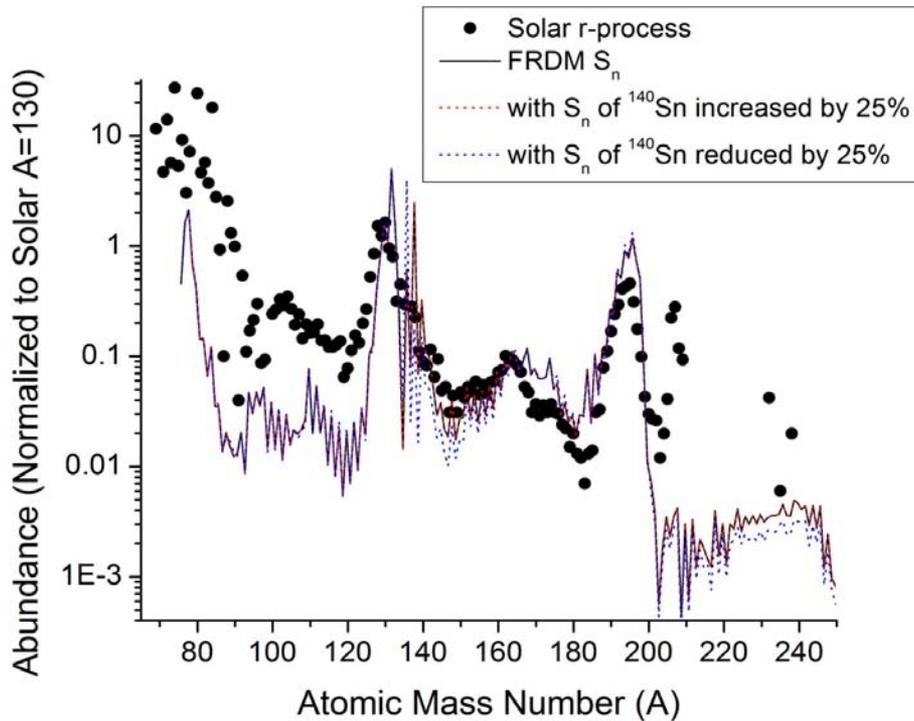
Cold r -process: equilibrium between (n,γ) and β decay



Interplay between beta decay, neutron capture, and beta-delayed neutron emission sets the final abundance pattern.

Neutron separation energy sensitivity study

S. Brett, I. Bentley, N. Paul, A. Aprahamian



plot by I. Bentley

Start with a baseline simulation

(here, the H-event conditions from Qian et al were used)

Vary one separation energy by 25% and rerun the simulation

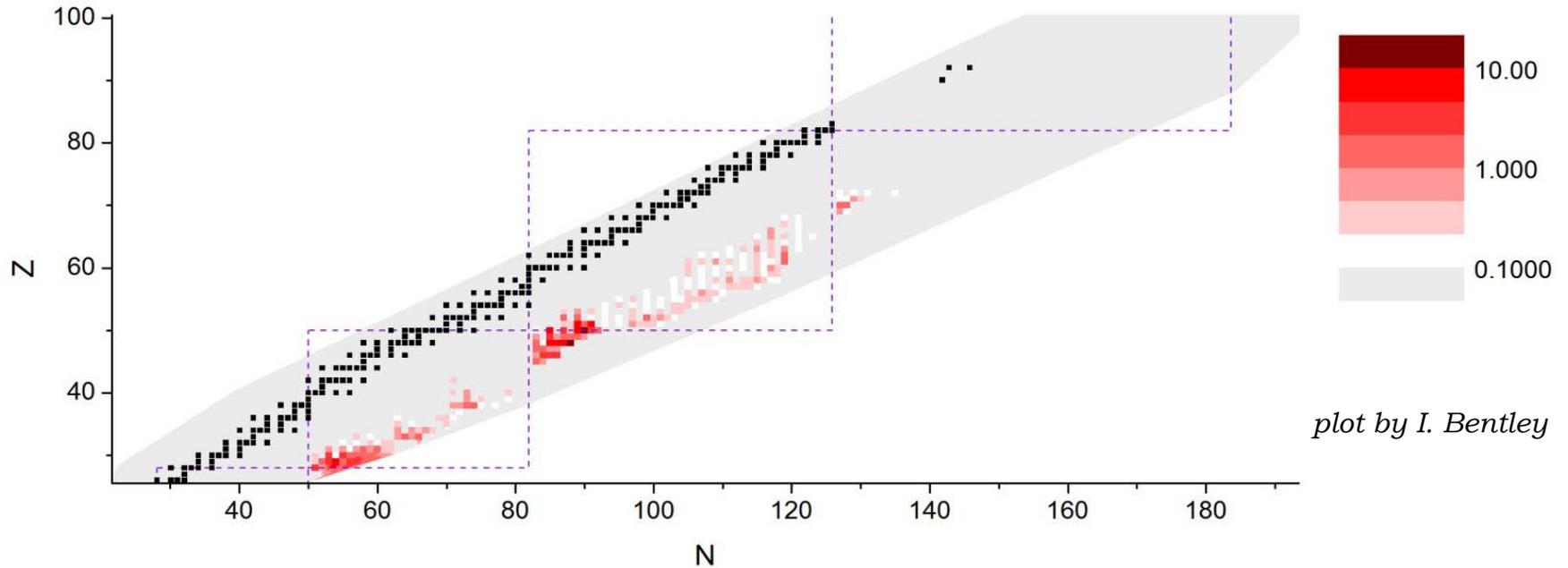
Repeat 6957 times

(twice for each heavy nucleus in the network)

$$\Delta Y_{S_n(Z_i, A_i) \pm 25\%} = \sum_A \left[Y_{baseline}(A) - Y_{S_n(Z_i, A_i) \pm 25\%}(A) \right]$$

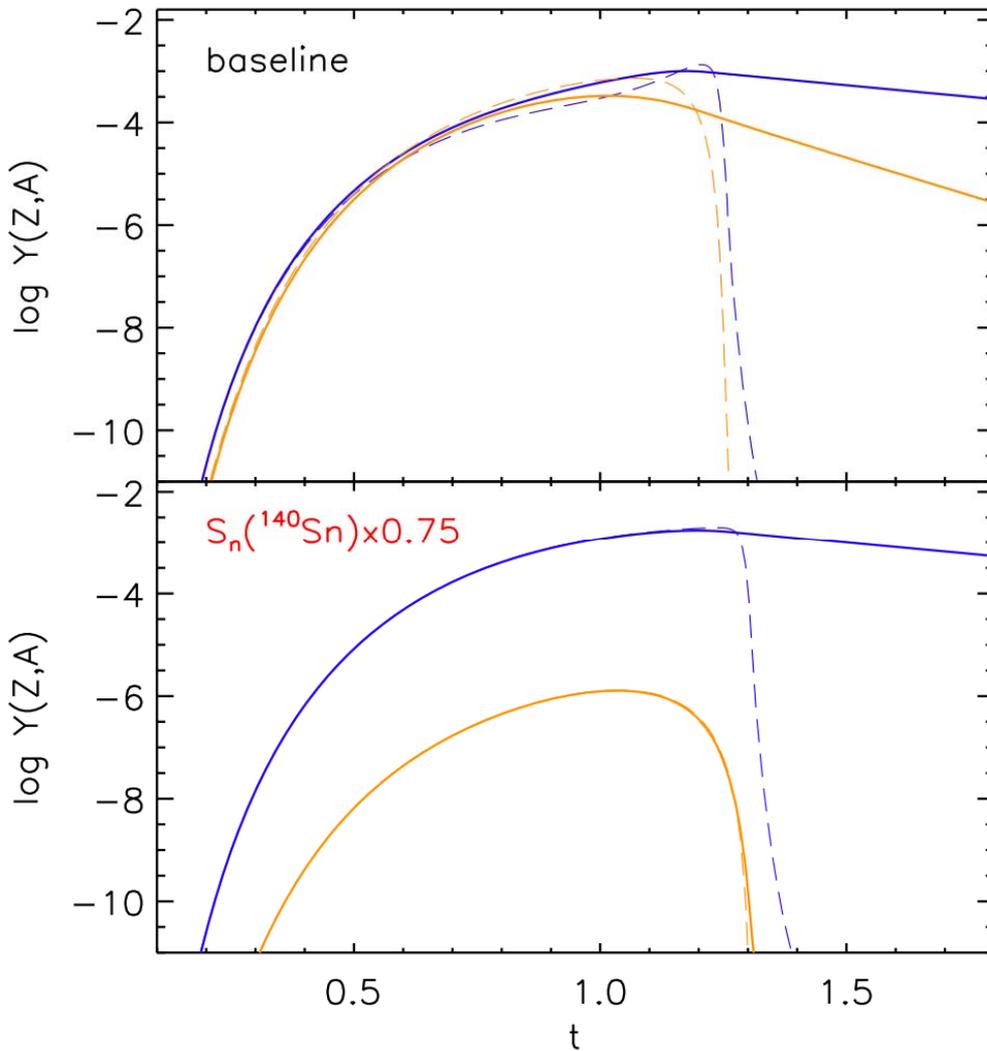
Neutron separation energy sensitivity study

S. Brett, I. Bentley, N. Paul, A. Aprahamian



$$\Delta Y_{S_n(Z_i, A_i) \pm 25\%} = \sum_A [Y_{baseline}(A) - Y_{S_n(Z_i, A_i) \pm 25\%}(A)]$$

The role of neutron separation energies in a hot r -process

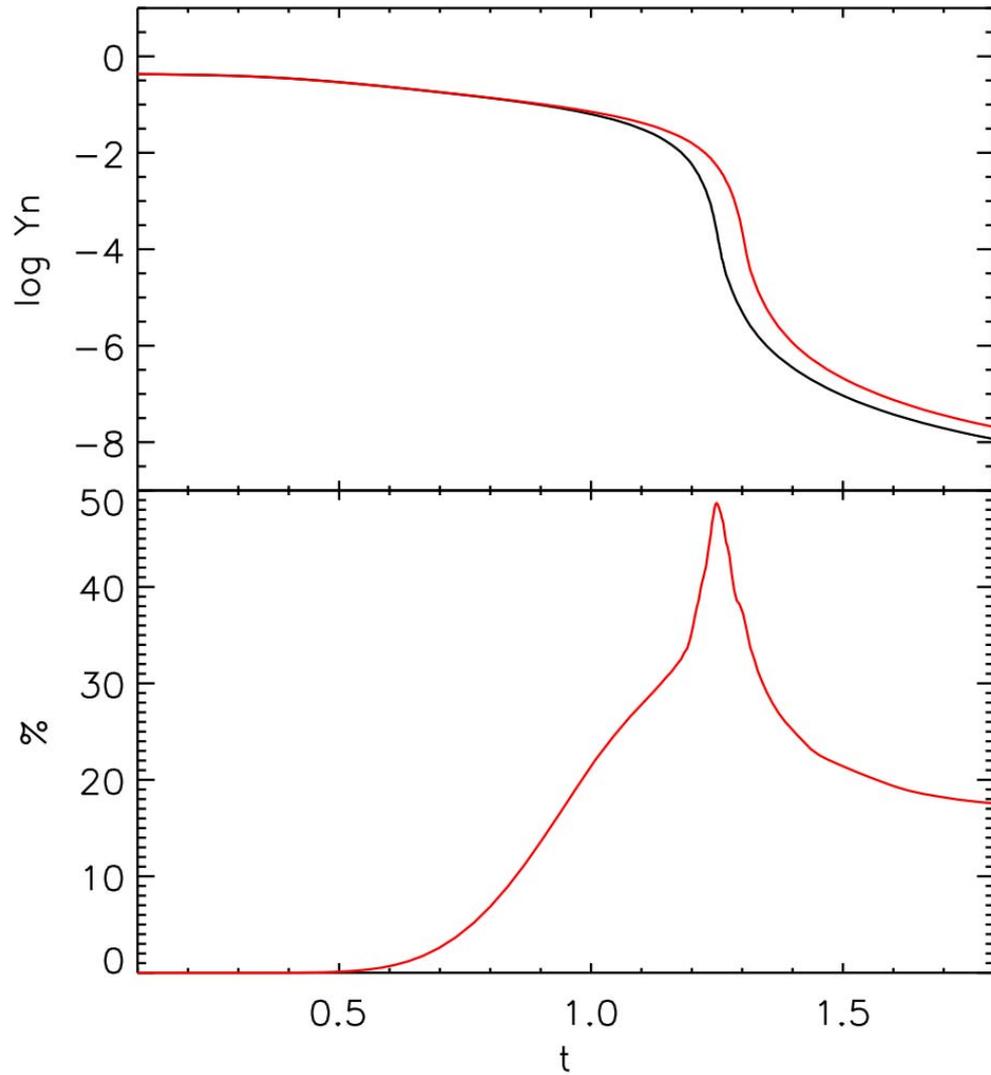


- $Y(50,138)$, abundance of ^{138}Sn
- $Y(50,140)$, abundance of ^{140}Sn
- - - $Y_{\text{equilibrium}}(50,138)$
- - - $Y_{\text{equilibrium}}(50,140)$

While in equilibrium, the relative abundances along an isotopic chain are given by a Saha equation:

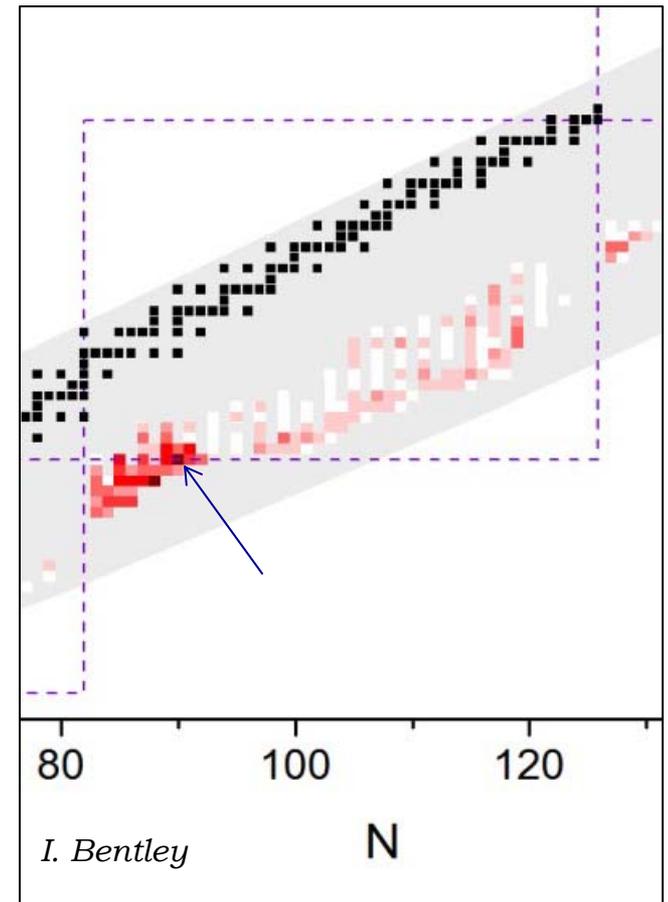
$$\frac{Y_{\text{equilibrium}}(Z, A+1)}{Y_{\text{equilibrium}}(Z, A)} = \frac{G(Z, A+1)}{2G(Z, A)} n_n \left(\frac{2\pi\hbar^2 N_A}{m_n kT} \right)^{3/2} \exp\left[\frac{S_n(Z, A+1)}{kT} \right]$$

The role of neutron separation energies in a hot r -process



plots by R. Surman

— Baseline simulation
— Simulation with $S_n(50,140)$ reduced by 25%



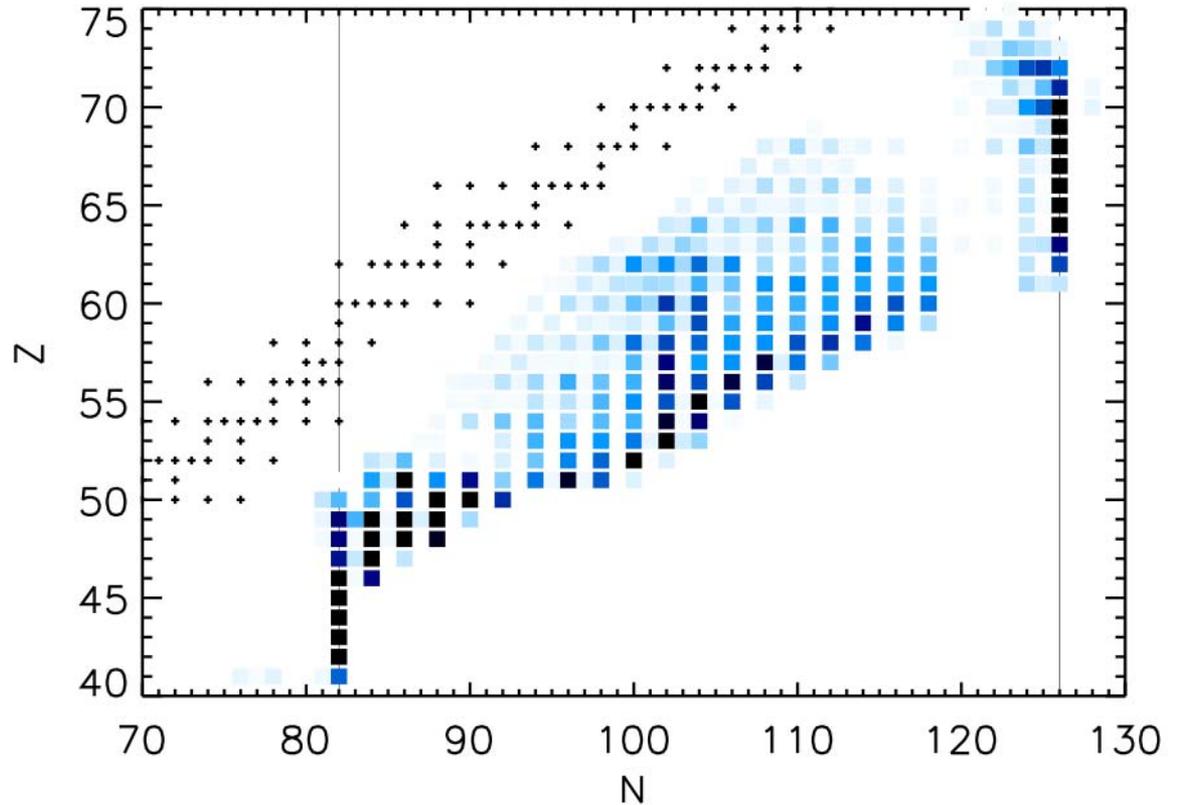
I. Bentley

N

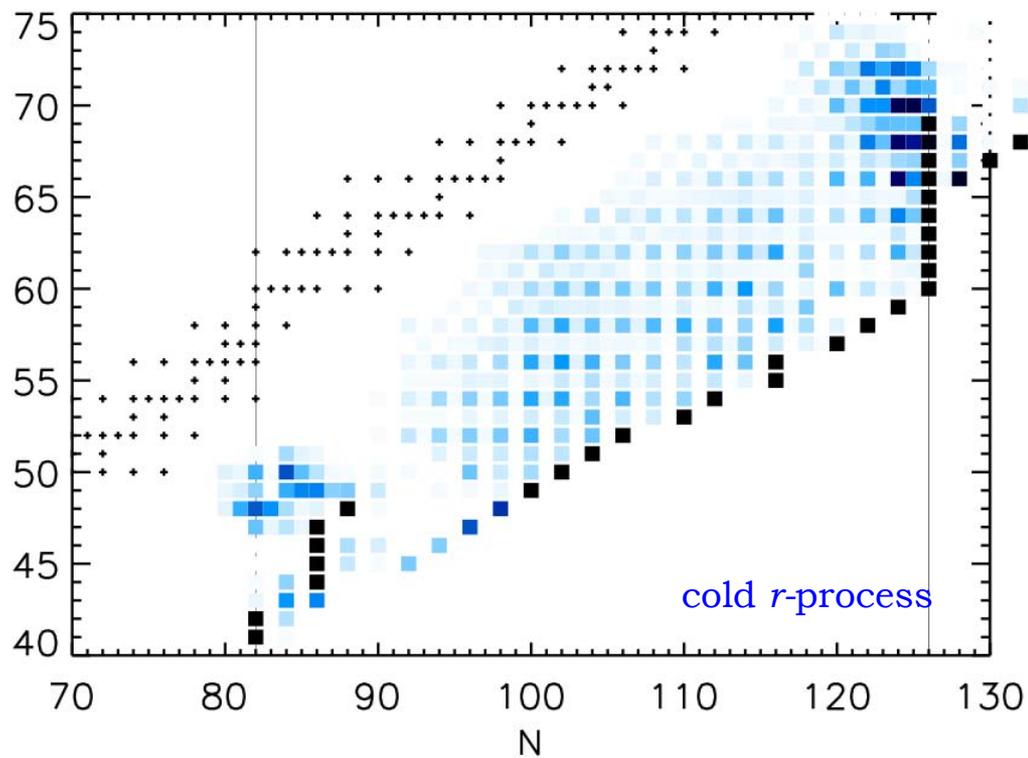
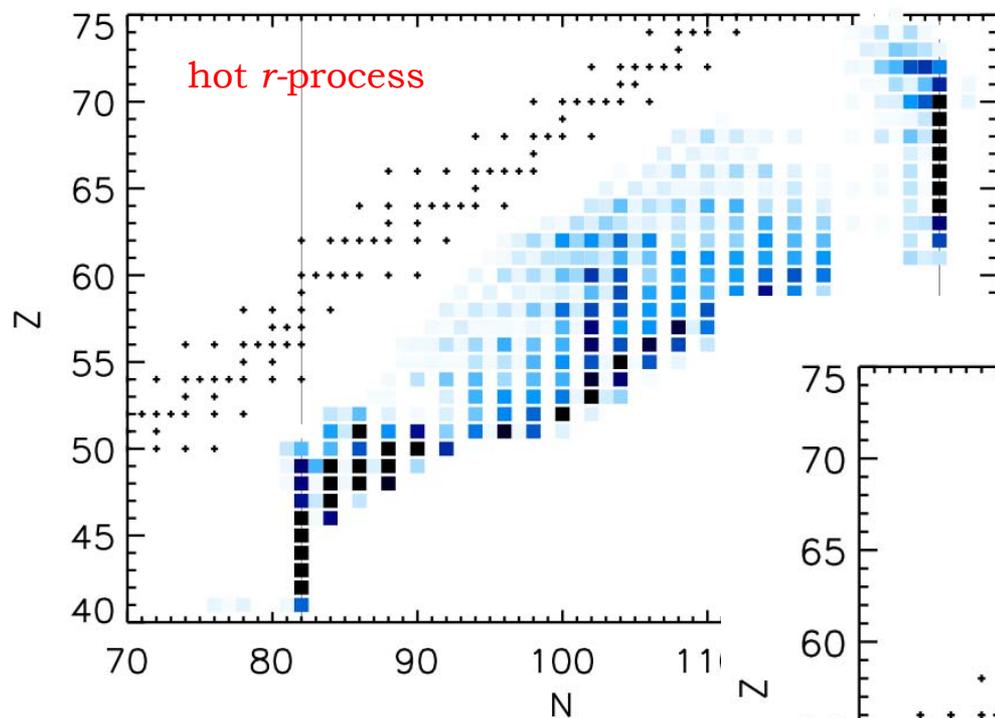
Beta decay rate sensitivity study

J. Cass, G. Passucci, R. Surman, A. Aprahamian

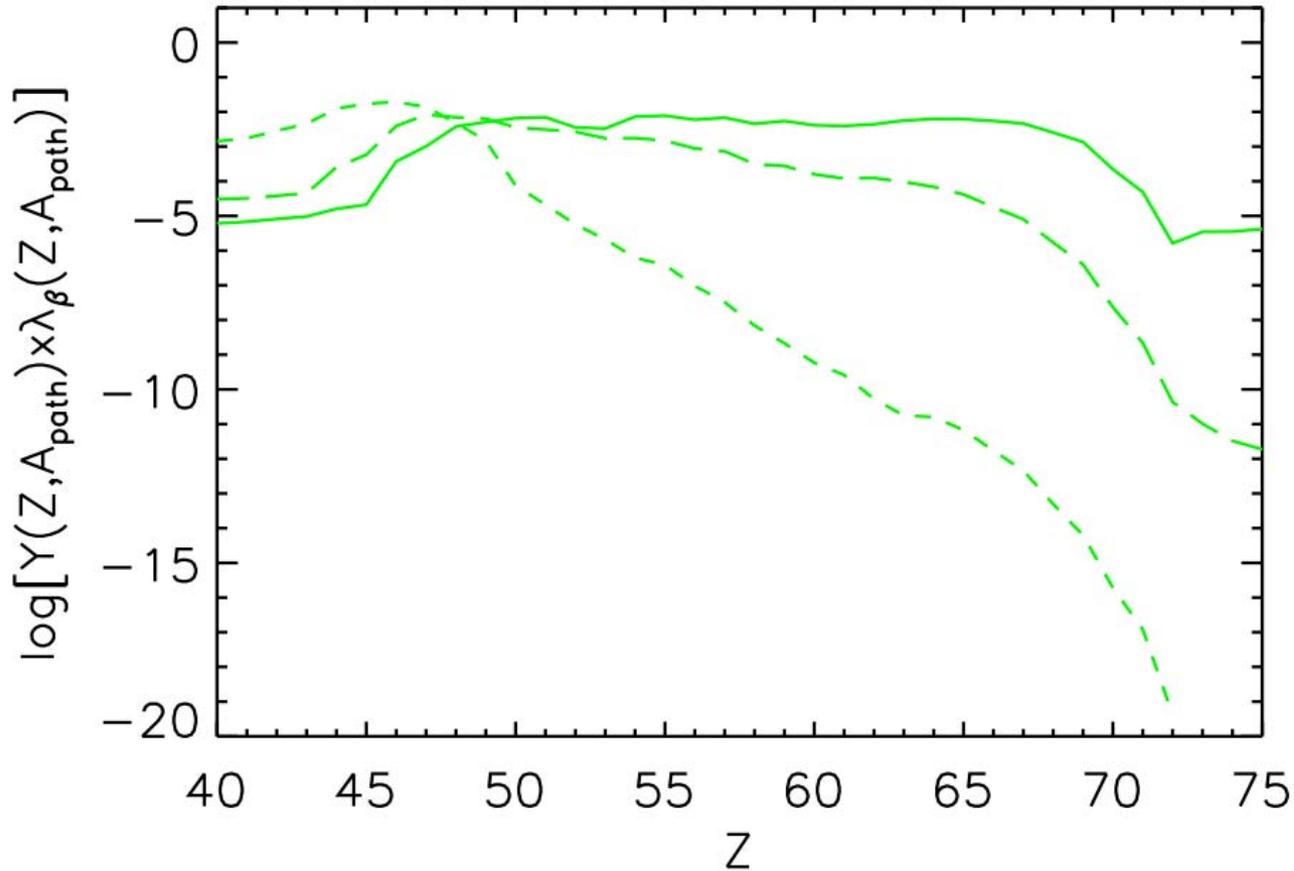
To start, proceed as in neutron separation energy study:
Vary one beta decay rate by an order of magnitude, rerun the simulation, and compare the final abundance pattern to the baseline



Beta decay rate sensitivity study



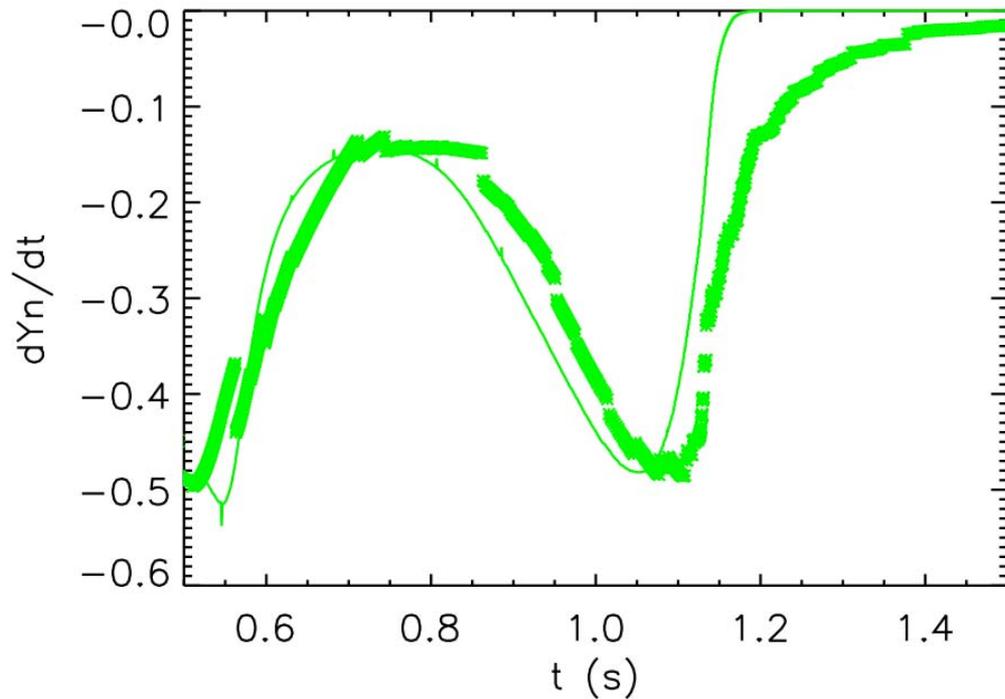
The role of beta decay rates in a hot r -process



Steady beta flow in the baseline simulation

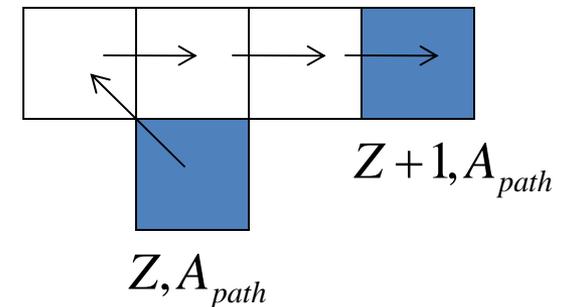
$$\lambda_{\beta}(Z, A_{\text{path}})Y(Z, A_{\text{path}}) \sim \text{constant}$$

The role of beta decay rates in a hot r -process



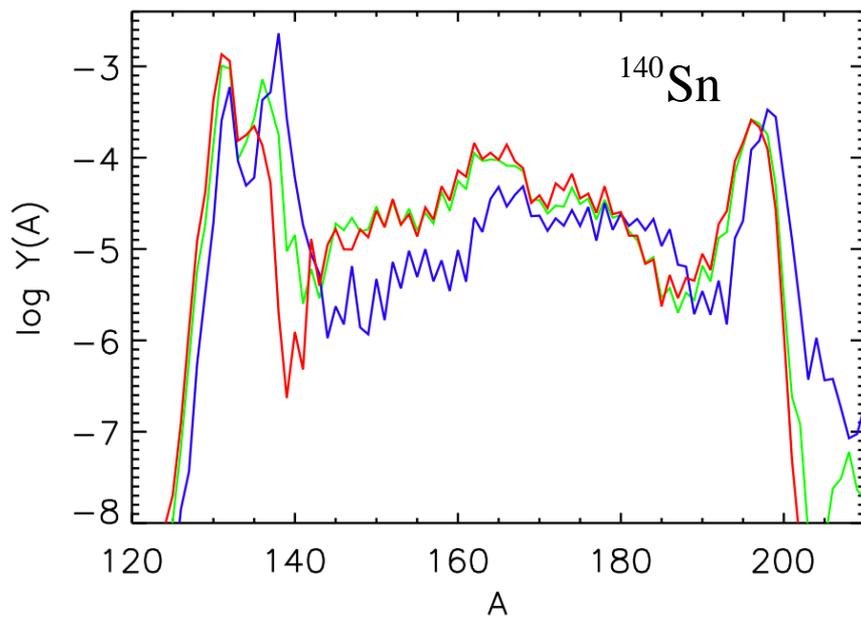
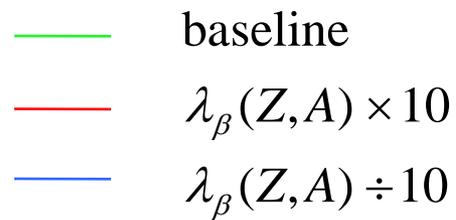
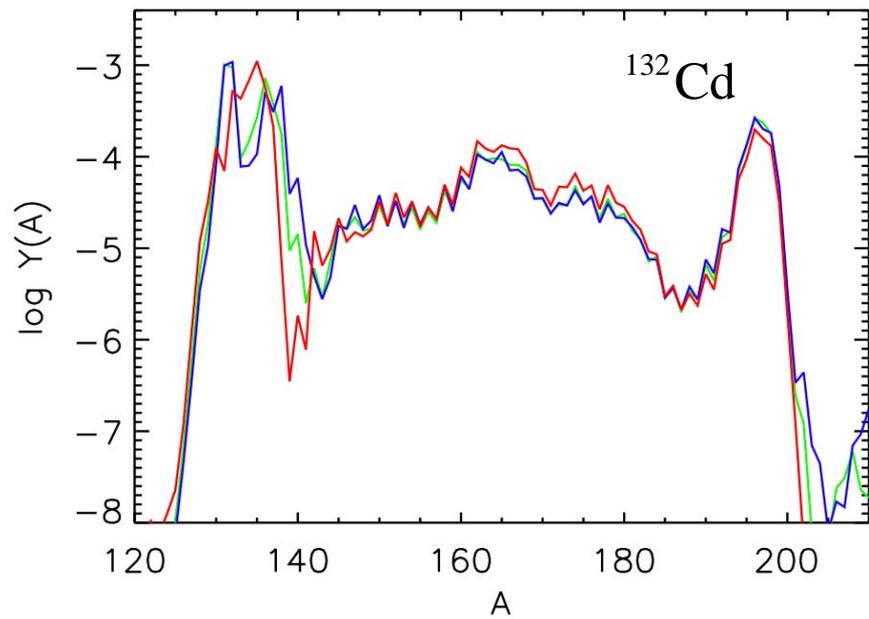
$$\frac{dY_n}{dt} - \sum_Z \lambda_\beta(Z, A_{path}) Y(Z, A_{path}) N'$$

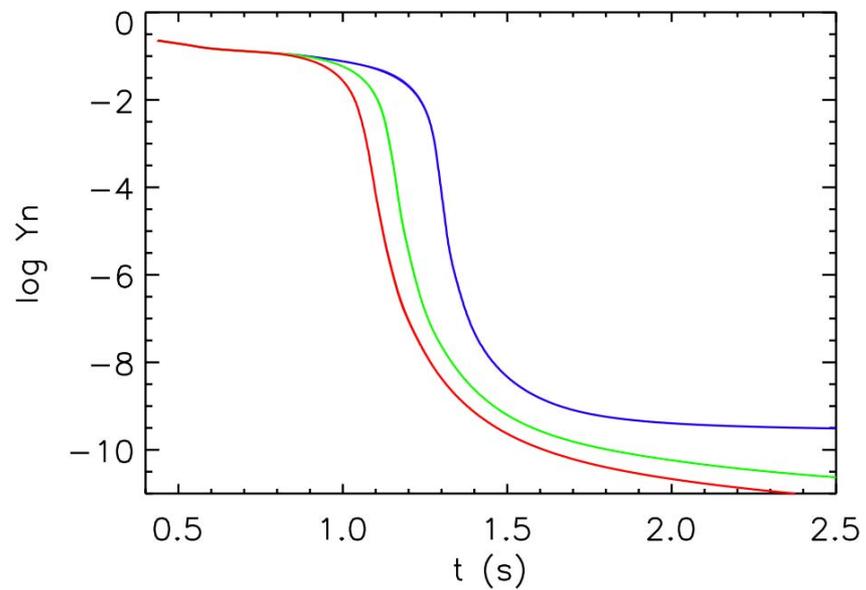
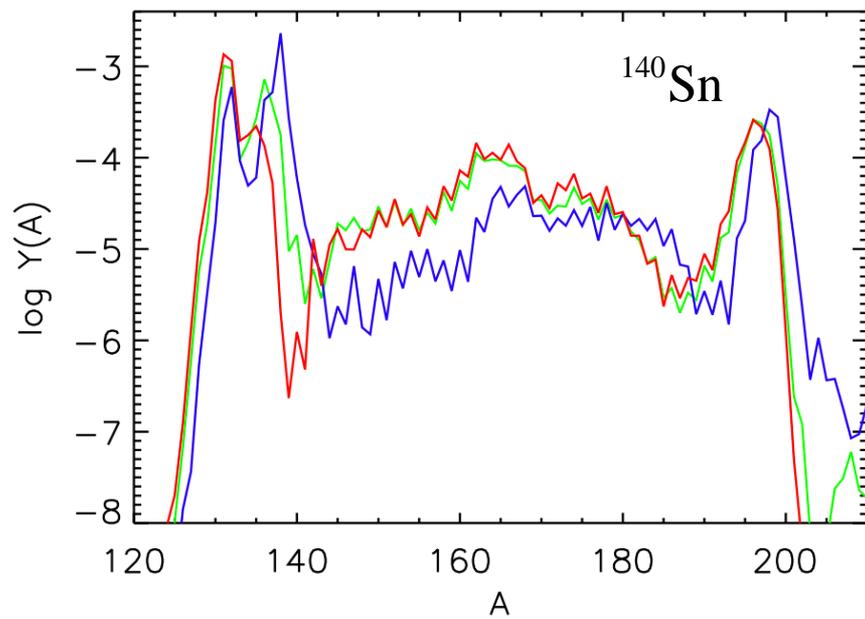
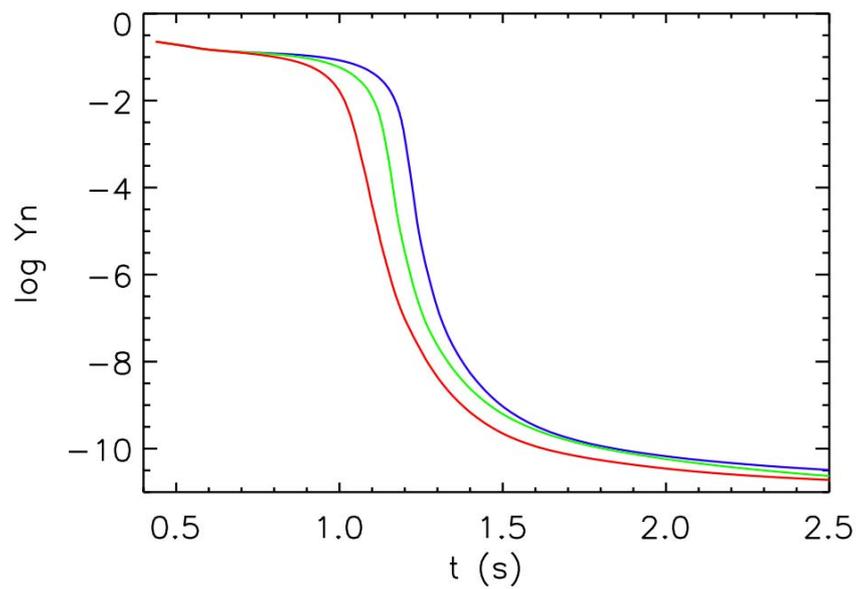
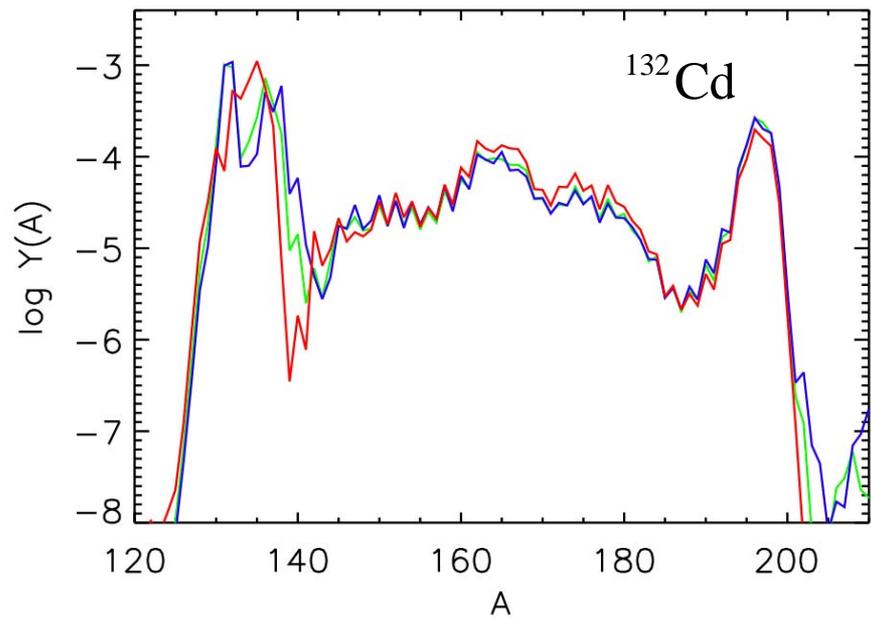
N' neutron captures



$$\frac{dY_n}{dt} \approx \sum_Z \lambda_\beta(Z, A_{path}) Y(Z, A_{path}) N'$$

where N' is the number of neutrons required to return to the path at $Z + 1$ following decay





Input Parameters for the Neutrino-less H-event from Qian et. al

Description	Value
Seed Nucleus	^{90}Se
$N_{neutron}/N_{seed}$	86
*Seed Nucleus	^{70}Fe
* $N_{neutron}/N_{seed}$	67
Initial Density ($\rho_5 = 10^5 \text{ g/cm}^3$)	0.0034
Initial Temperature ($T_9 = 10^9 \text{ K}$)	1.5
Freeze-out Time	0.86s

* ^{90}Se was replaced with ^{70}Fe in order to allow for the dependence on the masses of nuclei between $70 \geq A \geq 90$ to be investigated. This was done in such a way that the electron fraction remains constant ($Y_e = .19$).

ΔY for FRDM

Nucleus	ΔY
¹³⁶ Cd	20.2
¹⁴⁰ Sn	12.1
¹³⁵ Cd	8.80
⁸³ Cu	8.42
¹³⁹ Sn	8.19
¹⁴² Sb	5.64
¹³⁵ Sn	5.44
¹³³ Cd	5.38
¹⁴⁰ Sb	5.25
¹³⁴ Cd	5.23
⁸² Cu	4.14
¹³⁴ In	4.14
¹³¹ Pd	3.29
¹³⁷ Sn	2.94
¹⁴¹ Sn	2.91
⁸³ Zn	2.89
⁸⁵ Zn	2.71
⁸⁵ Cu	2.66
¹³⁰ Pd	2.39
¹³² Pd	2.39

ΔY for ETFSI-Q

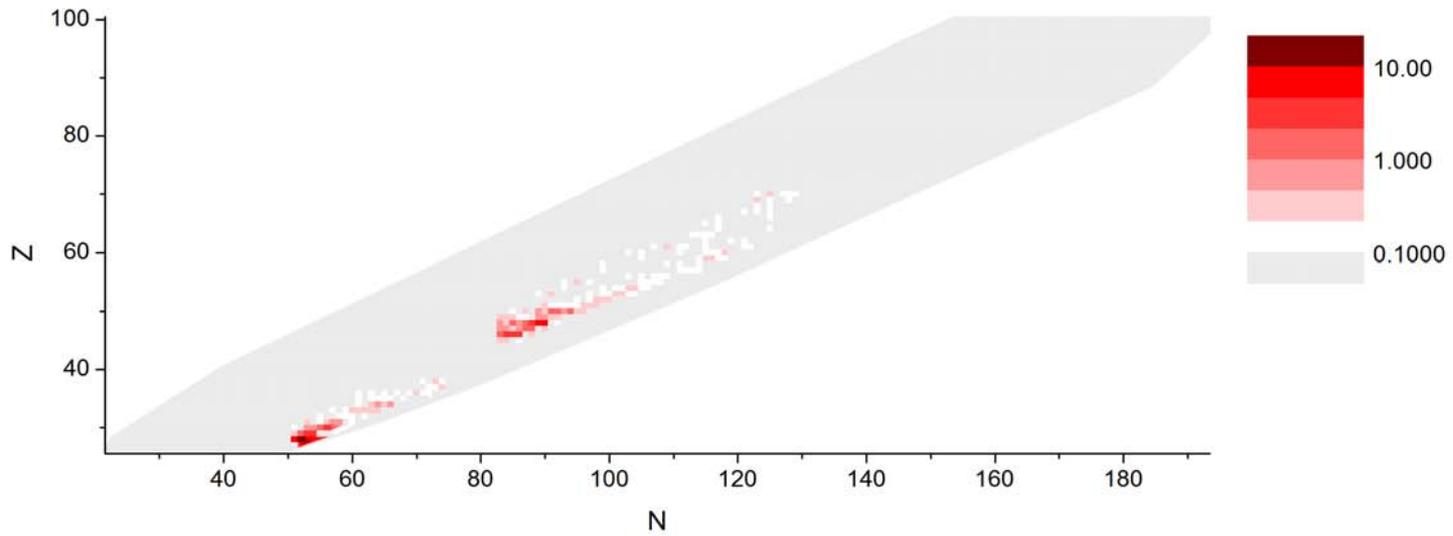
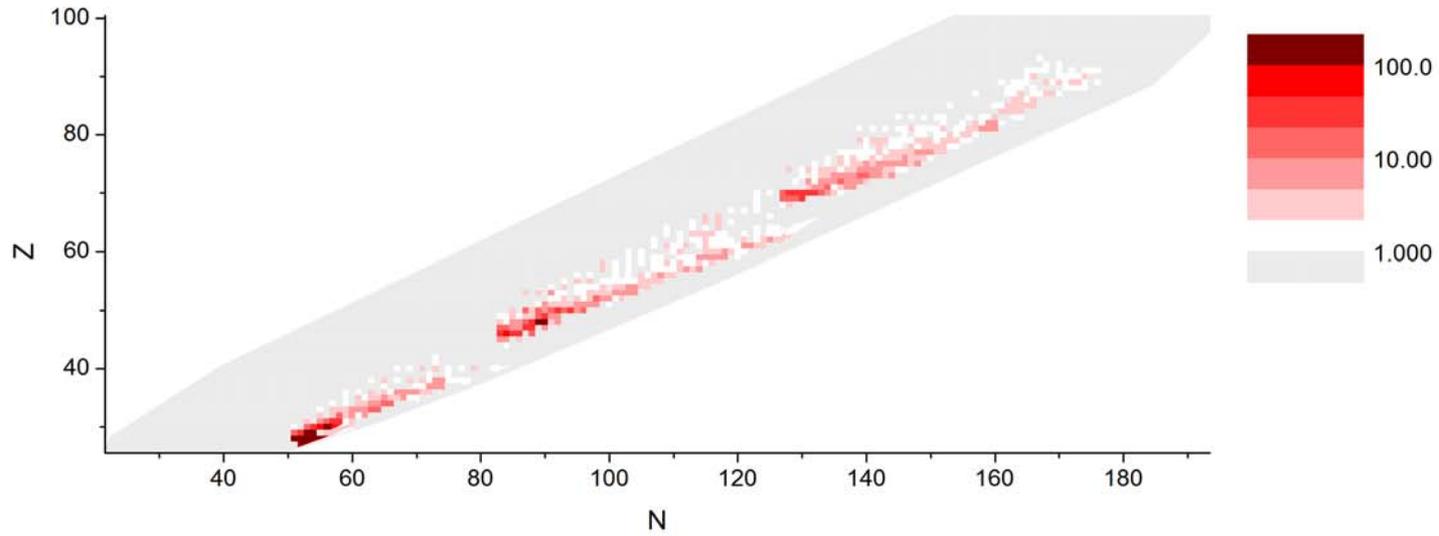
Nucleus	ΔY
¹⁴⁰ Sn	20.1
¹³⁶ Cd	19.0
¹⁴² Sn	17.3
¹³⁷ Cd	15.3
⁷⁹ Ni	12.5
⁸⁰ Ni	12.0
¹³⁵ Cd	11.5
¹³⁴ Cd	11.5
¹³⁸ Cd	8.57
¹³² Pd	7.66
¹³⁰ Pd	7.34
¹³² In	7.33
¹²⁹ Pd	5.12
¹³⁹ Sn	4.63
¹³¹ Pd	4.37
¹³⁸ In	3.98
¹³⁹ In	3.95
⁸⁶ Zn	3.21
¹⁴¹ Sn	2.92
⁸⁵ Zn	2.86

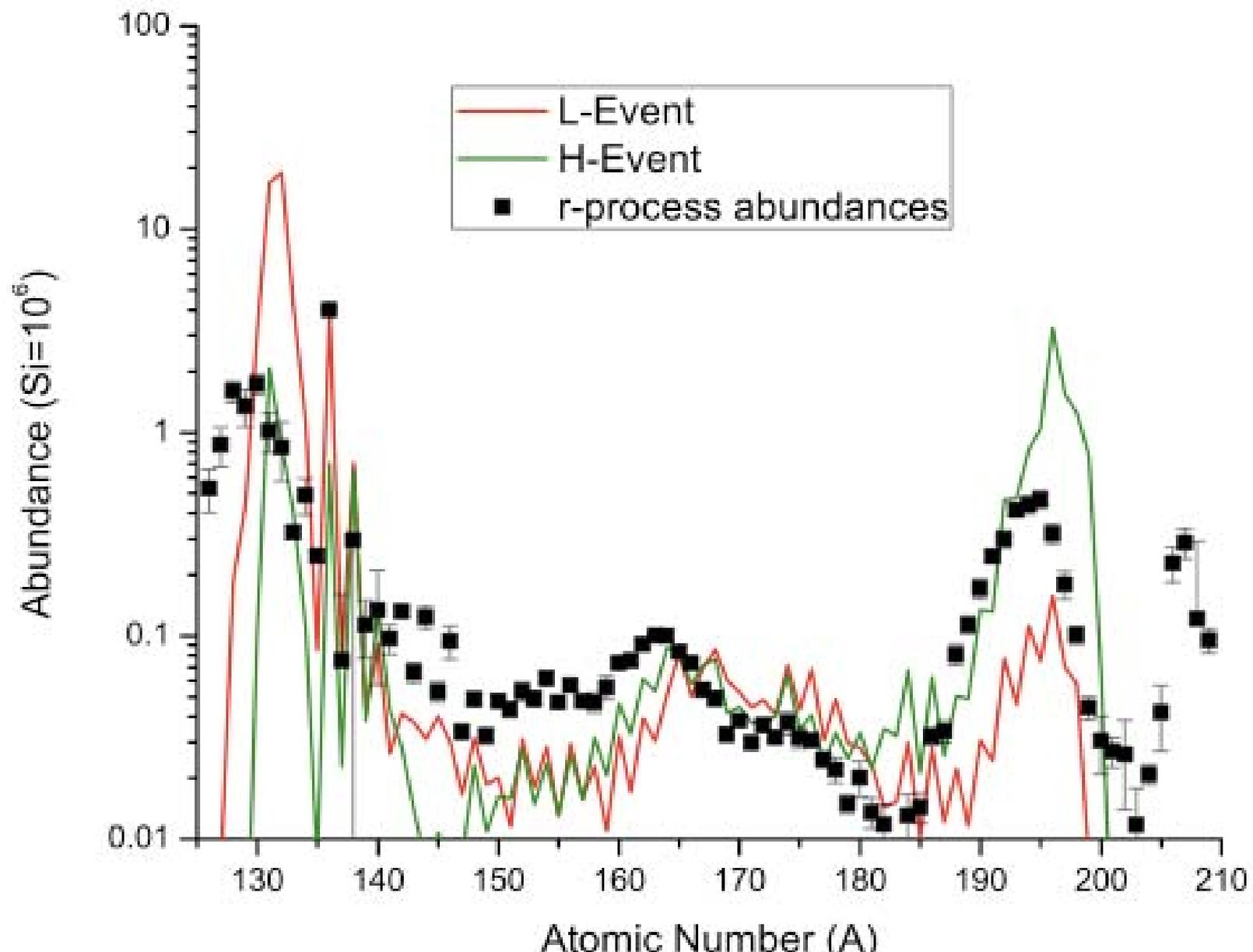
ΔY for DZ

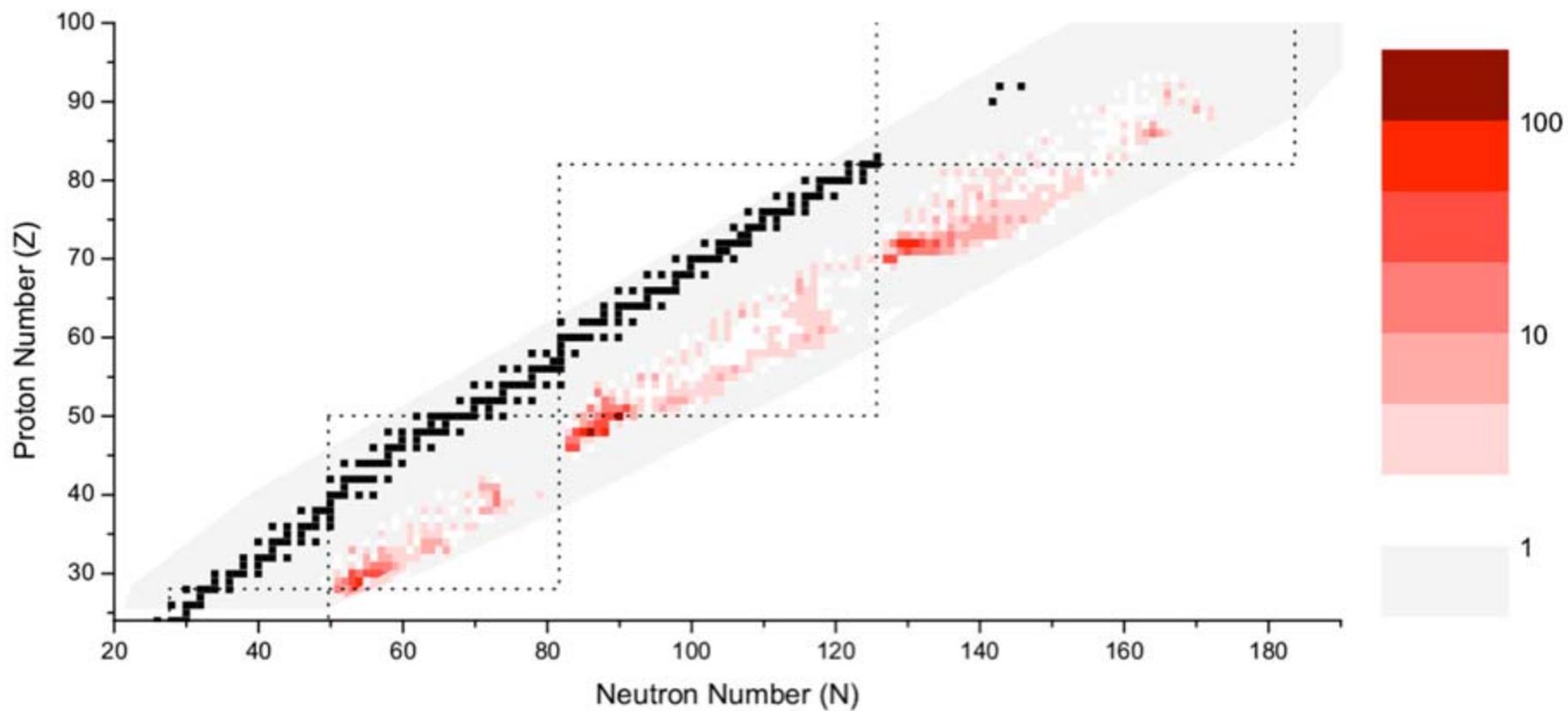
Nucleus	ΔY
⁸⁰ Ni	13.6
⁷⁹ Ni	9.96
¹³⁸ Cd	7.08
¹³⁷ Cd	5.49
⁸³ Cu	4.27
¹³¹ Pd	3.54
⁸² Cu	3.36
¹³² Pd	3.12
¹³⁶ Cd	3.00
¹³⁰ Pd	2.97
⁸⁶ Zn	2.84
¹²⁹ Pd	1.88
⁸⁵ Zn	1.81
¹³⁴ Ag	1.49
¹⁴² Sn	1.42
¹³⁵ Ag	1.39
¹³⁵ Cd	1.36
¹³³ Cd	1.10
¹⁴¹ Sn	1.08
¹⁴⁴ Sn	1.07

ΔY for HFB21

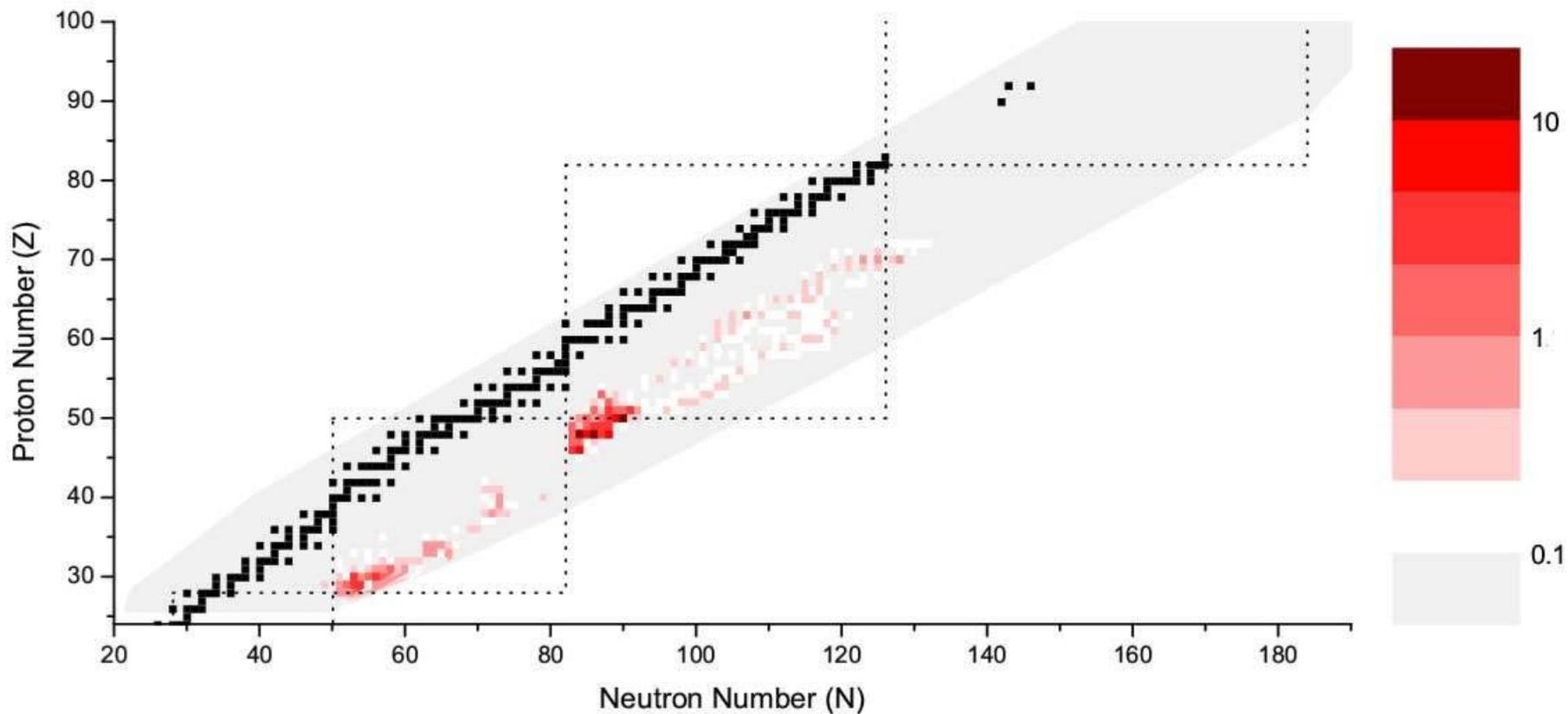
Nucleus	ΔY
¹³⁶ Cd	22.7
¹³⁷ Cd	10.8
¹³⁸ Cd	10.4
¹³⁵ Cd	6.97
¹⁴⁰ Sn	5.97
¹³⁰ Pd	5.46
⁸³ Cu	5.23
¹⁴² Sn	4.66
¹³⁴ Cd	4.57
¹⁴¹ Sn	4.21
⁸⁶ Zn	3.82
¹³³ Cd	3.52
¹³² Cd	3.04
¹³⁷ Sn	2.86
⁸² Cu	2.63
¹³⁸ In	2.47
¹³⁹ In	2.23
¹²⁹ Pd	1.95
¹³¹ Pd	1.81
¹³¹ Ag	1.69





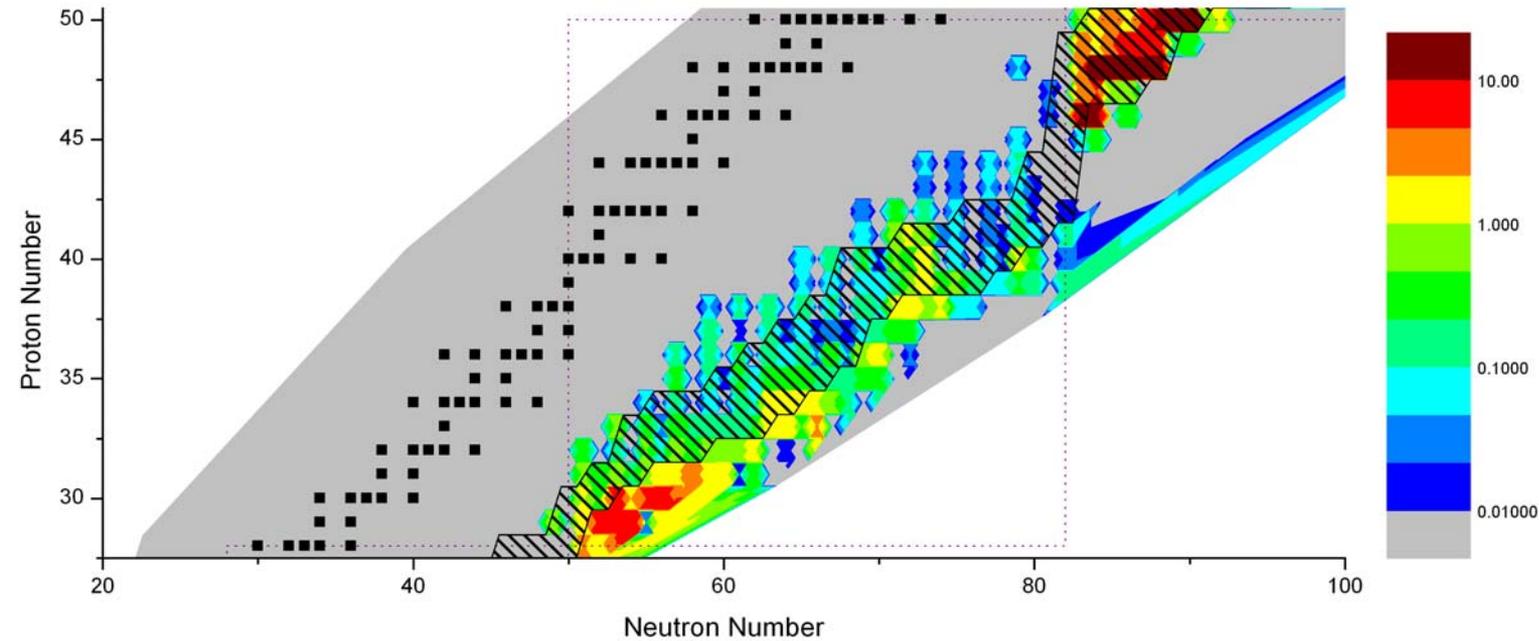


$$\Delta_{\pm 25\%}(N, Z) = \sum_A \frac{|Y(A) - Y(A, \pm \Delta S_n(N, Z))|}{Y(A)}$$



$$\Delta Y_{\pm 25\%}(N, Z) = \sum_A |Y(A) - Y(A, \pm \Delta S_n(N, Z))|.$$

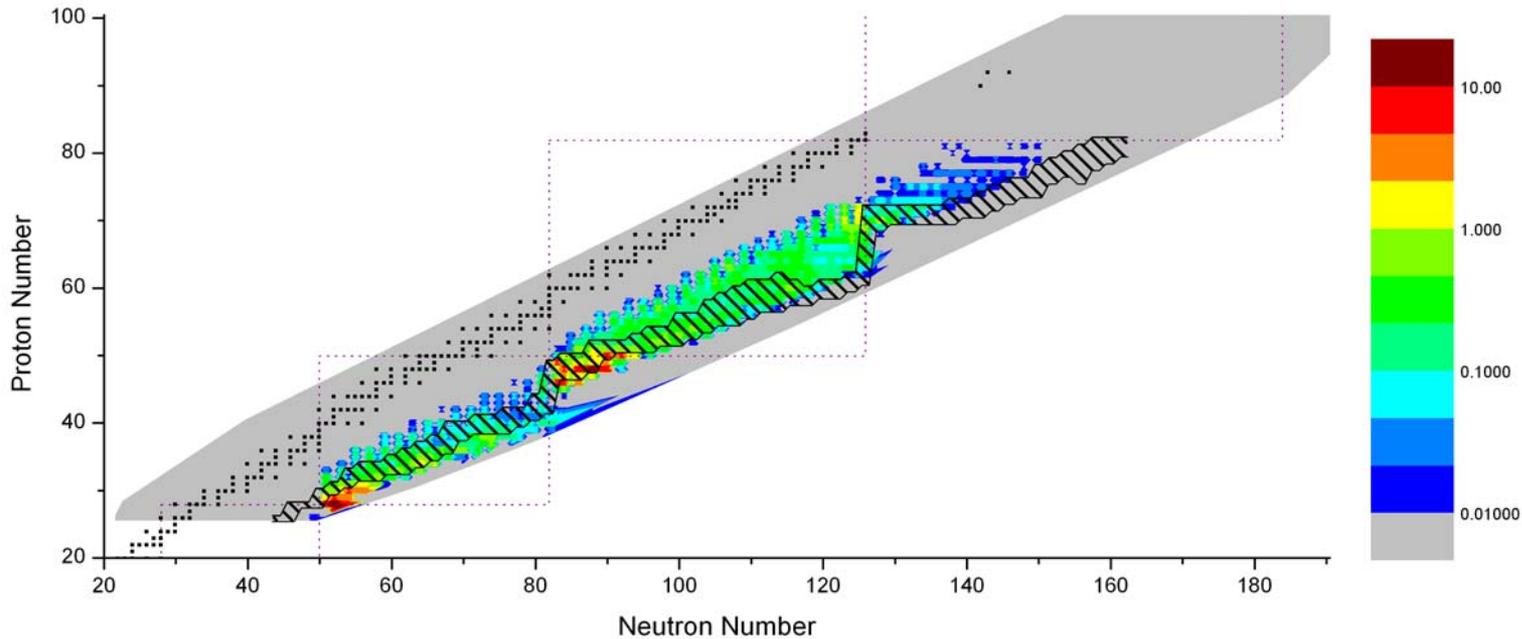
Run 23: H-Event with Iron-70 Seed ($Z \leq 50$)



Nucleus	$\Delta_{+25\%}$	$\Delta_{-25\%}$
140Sn	3.59E+00	6.55E+01
134Cd	2.25E+01	1.55E+01
132Cd	2.82E-01	3.09E+01
139Sn	3.71E+00	1.55E+01
136Cd	1.52E+01	1.84E+00
133Cd	5.21E+00	9.65E+00
130Pd	3.18E+00	9.76E+00
129Pd	3.63E+00	7.98E+00
135Cd	8.69E+00	1.68E+00
138Sn	1.71E-01	1.01E+01
83Cu	3.51E+00	4.27E+00
137In	1.22E+00	5.95E+00
135In	7.78E-01	6.39E+00
82Cu	3.01E+00	3.51E+00
83Zn	7.40E-01	5.73E+00
136In	1.55E+00	4.70E+00
86Zn	5.50E-01	5.58E+00
137Sn	8.48E-01	4.79E+00
81Cu	7.61E-02	5.32E+00
131Ag	2.06E+00	2.63E+00

Run #	Description	Seed	Nseed	Nn	T9	density [g/cm ³]	time [sec.]	Source
23	H Qian's neutrinoless model (Iron)	Fe70	0.511	0.489	1.5	3.4x10 ²	1.68	Qian et al. ApJ 494 (1998) with Fe70

Run 62: H-Event with Iron-70 Seed

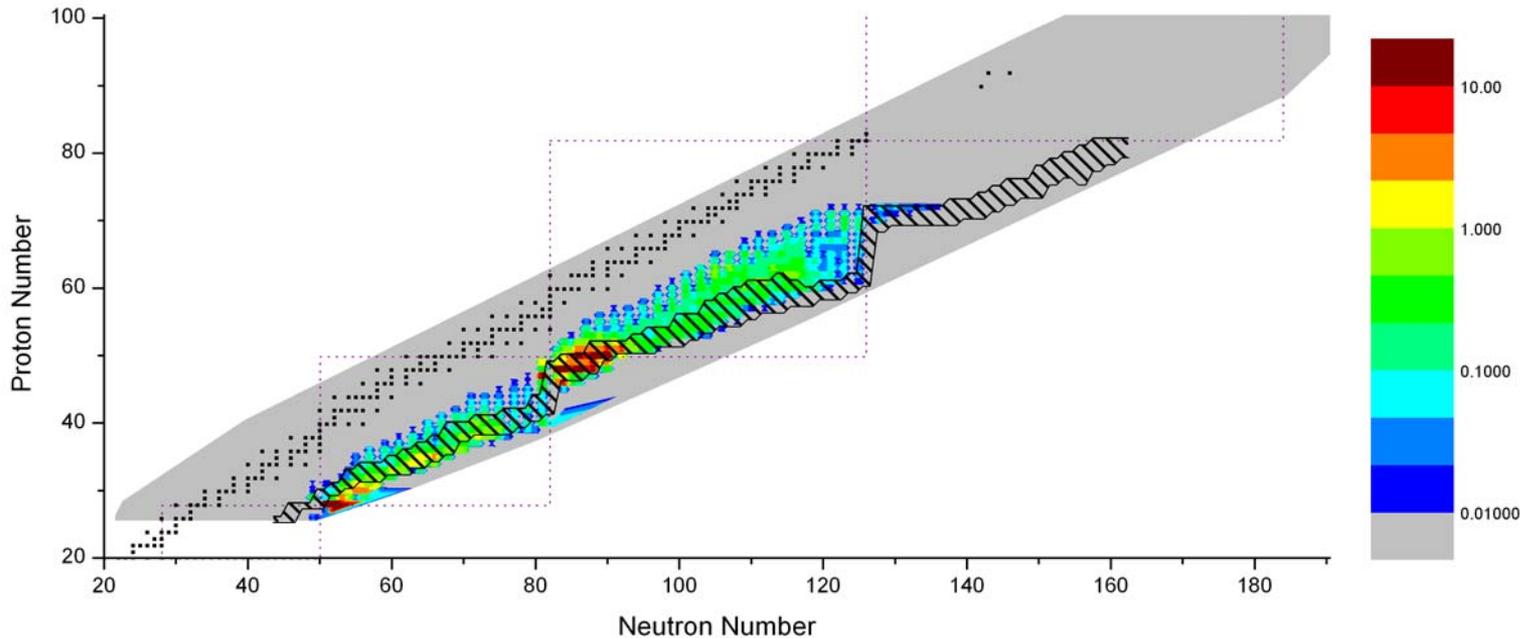


Nucleus	$\Delta_{+25\%}$	$\Delta_{-25\%}$
136Cd	6.79E+00	1.05E+01
80Ni	1.29E+01	2.90E+00
79Ni	7.00E+00	2.64E+00
135Cd	1.90E+00	7.16E+00
134Cd	1.47E+00	5.80E+00
138Cd	5.83E+00	1.26E+00
130Pd	2.92E+00	3.15E+00
140Sn	9.12E-01	4.92E+00
137Cd	4.48E+00	1.19E+00
142Sn	1.12E+00	4.17E+00
81Cu	1.05E+00	3.98E+00
129Pd	2.24E+00	2.78E+00
132In	3.77E+00	1.22E+00
84Zn	2.97E-02	4.93E+00
132Cd	1.76E-01	4.65E+00
132Pd	3.57E+00	4.52E-02
86Zn	2.73E+00	8.48E-01
83Cu	2.64E+00	8.16E-01
141Sn	9.33E-01	2.15E+00
82Cu	2.19E+00	8.38E-01

DUZU mass model

Run #	Description	Seed	Nseed	Nn	T9	density [g/cm ³]	time [sec.]	Source
62	H Qian's neutrinoless model (Iron)	Fe70	0.511	0.489	1.5	3.4x10 ²	1.68	Qian et al. ApJ 494 (1998) with Fe70

Run 63: H-Event with Iron-70 Seed

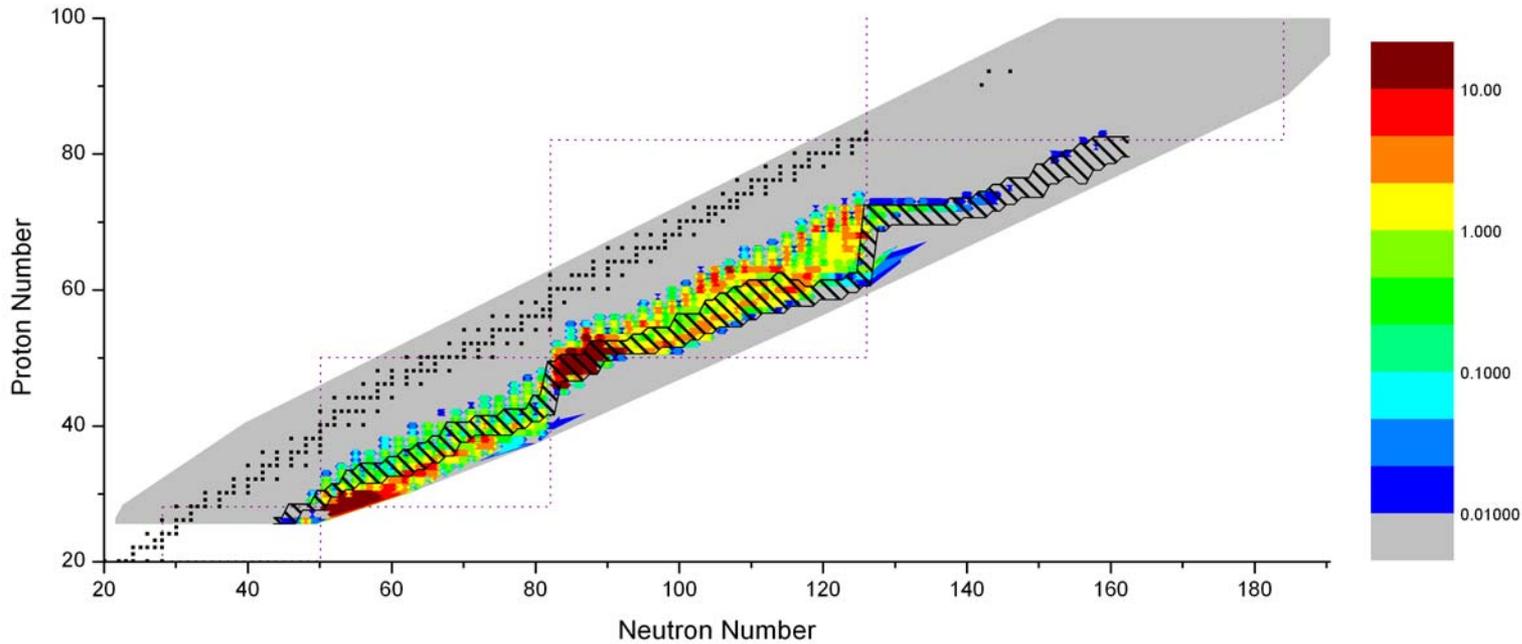


Nucleus	$\Delta_{+25\%}$	$\Delta_{-25\%}$
¹³⁴ Cd	3.45E+01	8.20E+00
¹⁴⁰ Sn	8.69E+00	2.11E+01
¹³² Cd	2.50E+01	4.61E+00
¹³⁹ Sn	5.41E+00	1.75E+01
⁸⁰ Ni	6.34E+00	1.28E+01
⁷⁹ Ni	6.13E+00	1.28E+01
¹³⁸ Sn	1.00E+01	7.06E+00
¹³⁶ Sn	5.17E-01	1.30E+01
¹³⁶ Cd	1.02E+01	1.35E+00
¹³¹ Cd	8.38E+00	2.92E+00
¹²⁸ Ag	9.23E-04	1.08E+01
¹³⁵ Cd	6.42E+00	1.32E+00
¹³³ Cd	3.73E+00	3.64E+00
¹³⁷ Sn	3.40E+00	2.46E+00
¹³⁰ Pd	5.07E+00	5.09E-01
¹³⁷ In	1.17E+00	4.31E+00
¹⁴¹ Sb	1.51E+00	3.82E+00
¹⁴³ Sb	1.26E+00	3.47E+00
¹³⁵ In	1.56E+00	2.87E+00
¹³⁶ In	9.28E-01	3.16E+00

ETFSI-12 mass model

Run #	Description	Seed	Nseed	Nn	T9	density [g/cm ³]	time [sec.]	Source
63	H Qian's neutrinoless model (Iron)	Fe70	0.511	0.489	1.5	3.4x10 ²	1.68	Qian et al. ApJ 494 (1998) with Fe70

Run 64: H-Event with Iron-70 Seed



Nucleus	$\Delta_{+25\%}$	$\Delta_{-25\%}$
¹³⁶ Sn	2.87E+00	7.00E+02
⁸⁰ Ni	3.09E+01	1.56E+02
¹³⁴ Cd	1.50E+02	3.33E+01
¹³² Cd	2.96E+00	1.75E+02
¹³⁸ Sn	1.39E+02	3.01E+01
⁷⁹ Ni	3.58E+01	1.13E+02
¹³⁷ Sn	8.82E+01	2.80E+01
¹³⁰ Pd	7.10E+01	2.56E+01
¹³⁵ In	6.17E+00	6.43E+01
¹³³ Cd	3.77E+01	3.06E+01
¹⁴⁰ Sb	1.35E+01	5.30E+01
¹²⁹ Pd	4.18E+01	2.45E+01
¹³⁶ Cd	5.60E+01	6.87E-01
¹³⁵ Sn	9.82E+00	4.63E+01
¹³⁶ In	2.99E+01	2.40E+01
¹³⁷ In	2.84E+01	2.52E+01
⁸³ Cu	1.86E+00	4.71E+01
¹⁴² Sb	2.12E+01	1.84E+01
¹⁴¹ Sb	2.18E-03	3.70E+01
¹³⁶ Sb	2.28E+01	1.24E+01

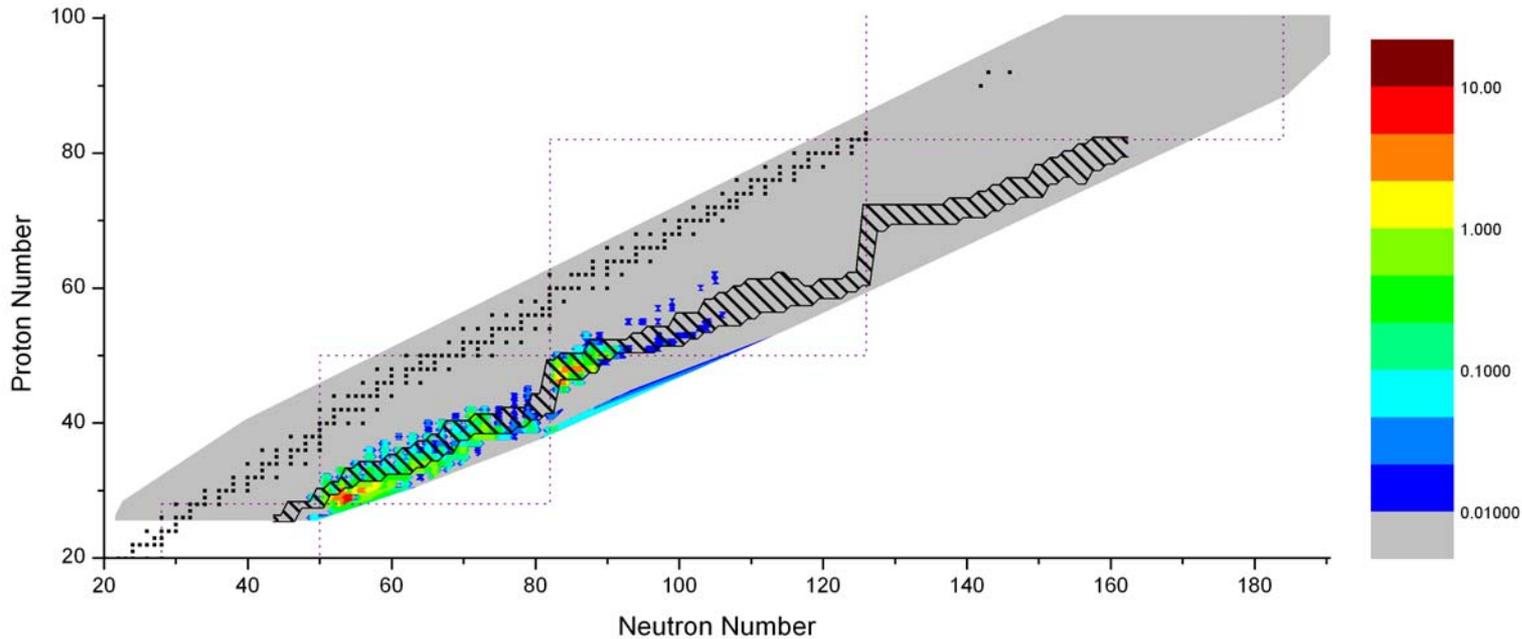
F-spin mass model

Run #	Description	Seed	Nseed	Nn	T9	density [g/cm ³]	time [sec.]	Source
64	H Qian's neutrinoless model (Iron)	Fe70	0.511	0.489	1.5	3.4x10 ²	1.68	Qian et al. ApJ 494 (1998) with Fe70

Runs 23, 63, 64

- These runs use the **same astrophysical parameters** (Qian's H-Event with a ^{70}Fe seed).
- **Varied mass models**
- The following nuclei are in all three top 20 tables:
 ^{130}Pd , ^{132}Cd , ^{134}Cd , ^{135}Cd , ^{136}Cd and ^{140}Sn .

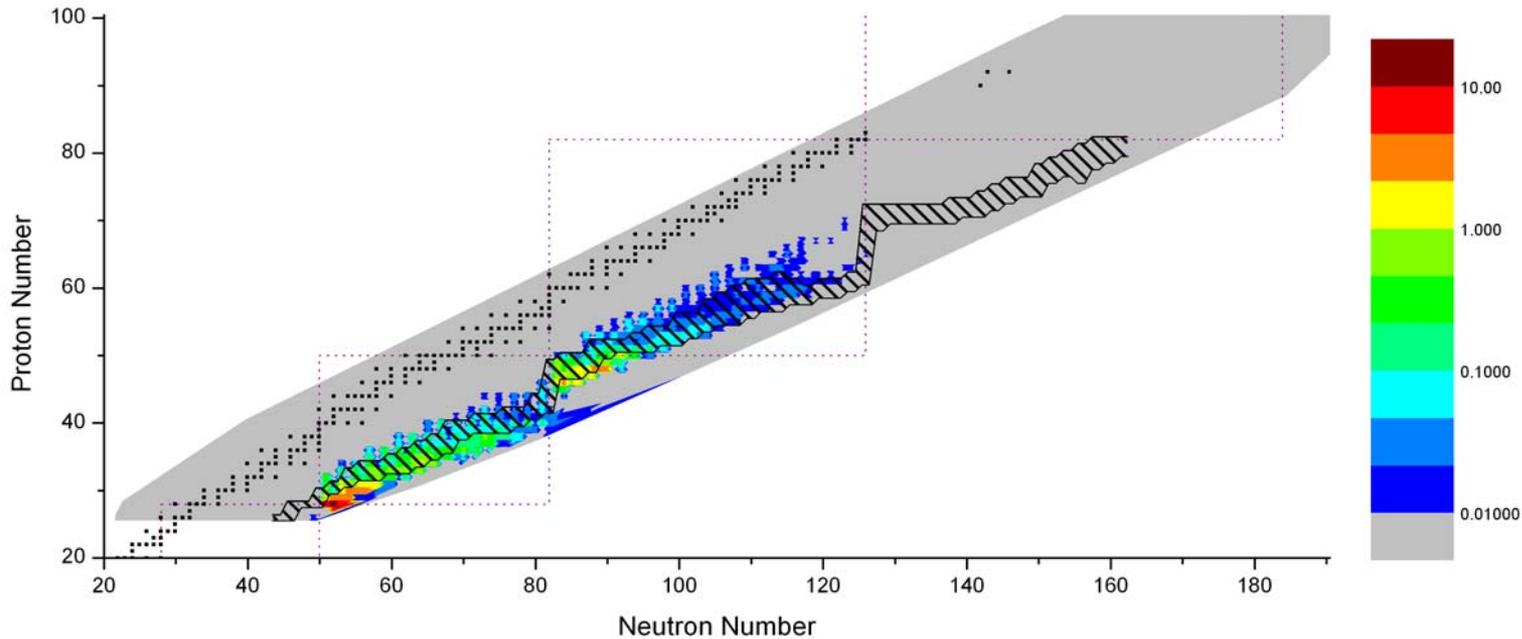
Run 24: L-Event with Iron-70 Seed



Nucleus	$\Delta_{+25\%}$	$\Delta_{-25\%}$
83Cu	1.92E+00	5.34E+00
82Cu	1.30E+00	3.13E+00
134Cd	1.55E+00	2.27E+00
130Pd	9.98E-01	2.28E+00
83Zn	4.02E-01	2.87E+00
132Cd	6.40E-03	3.06E+00
133Cd	1.26E+00	1.79E+00
129Pd	6.46E-01	1.74E+00
81Cu	1.65E-02	2.33E+00
86Zn	1.67E-01	2.13E+00
85Zn	8.50E-01	1.27E+00
131Ag	3.56E-01	1.67E+00
130Ag	4.13E-01	8.31E-01
89Ga	2.87E-01	9.39E-01
136Cd	9.91E-01	8.64E-02
110Sr	1.46E-02	9.36E-01
140Sn	5.69E-02	8.90E-01
132In	2.71E-02	8.76E-01
79Ni	6.57E-01	2.29E-01
99As	8.53E-01	1.29E-02

Run #	Description	Seed	Nseed	Nn	T9	density [g/cm ³]	time [sec.]	Source
24	L Qian's neutrinoless model (Iron)	Fe70	0.672	0.328	1.5	5.1x10 ²	0.78	Qian et al. ApJ 494 (1998) with Fe70

Run 67: L-Event with Iron-70 Seed

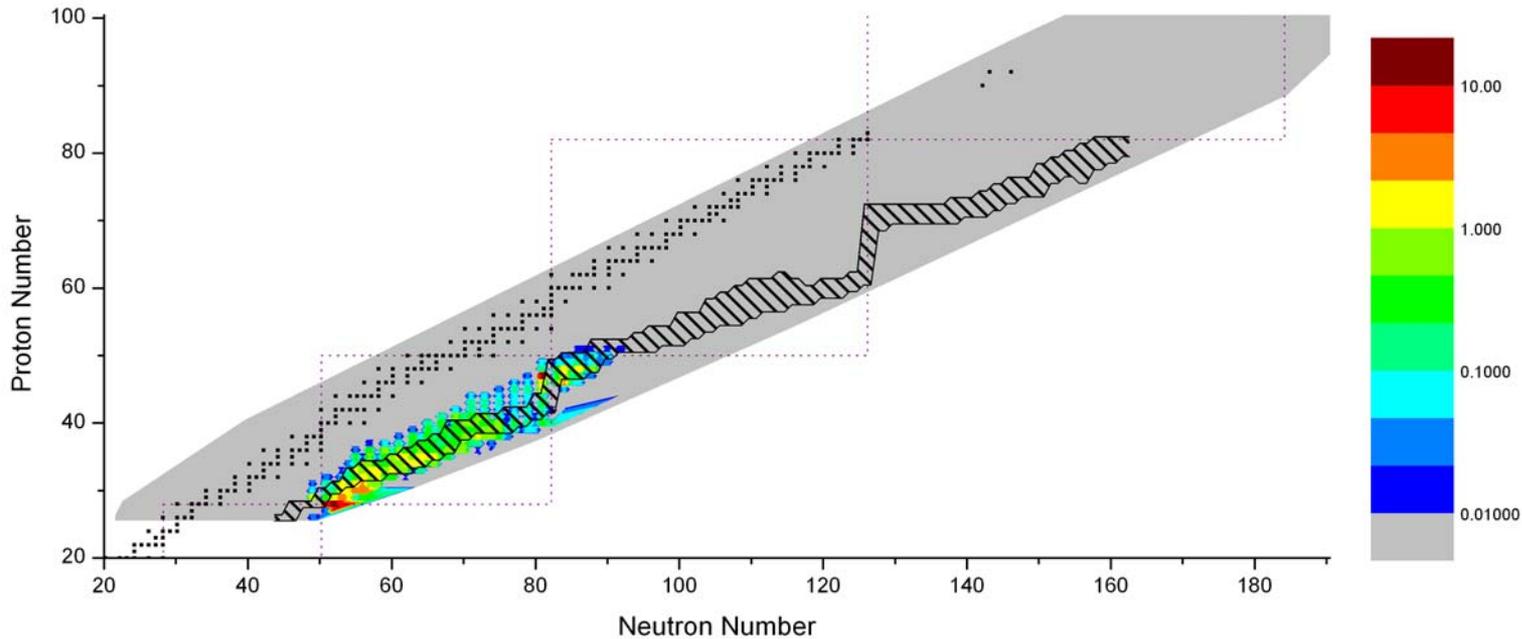


Nucleus	$\Delta_{+25\%}$	$\Delta_{-25\%}$
80Ni	6.56E+00	4.43E+00
79Ni	5.06E+00	3.95E+00
83Cu	2.59E+00	2.00E+00
82Cu	1.87E+00	2.02E+00
86Zn	1.75E+00	1.97E+00
81Cu	3.62E-01	2.93E+00
84Zn	1.13E-02	3.02E+00
85Zn	1.21E+00	1.64E+00
130Pd	1.72E+00	1.06E+00
137Cd	1.91E+00	7.41E-01
138Cd	1.75E+00	7.93E-01
136Cd	5.62E-01	1.84E+00
134Cd	3.66E-02	1.48E+00
83Zn	2.25E-01	1.26E+00
132Pd	1.31E+00	8.11E-02
89Ga	7.33E-01	6.47E-01
129Pd	6.34E-01	7.33E-01
135Cd	2.74E-01	1.04E+00
131Ag	6.44E-01	6.54E-01
87Ga	5.29E-01	7.25E-01

DUZU mass model

Run #	Description	Seed	Nseed	Nn	T9	density [g/cm ³]	time [sec.]	Source
67	L Qian's neutrinoless model (Iron)	Fe70	0.672	0.328	1.5	5.1x10 ²	0.78	Qian et al. ApJ 494 (1998) with Fe70

Run 68: L-Event with Iron-70 Seed

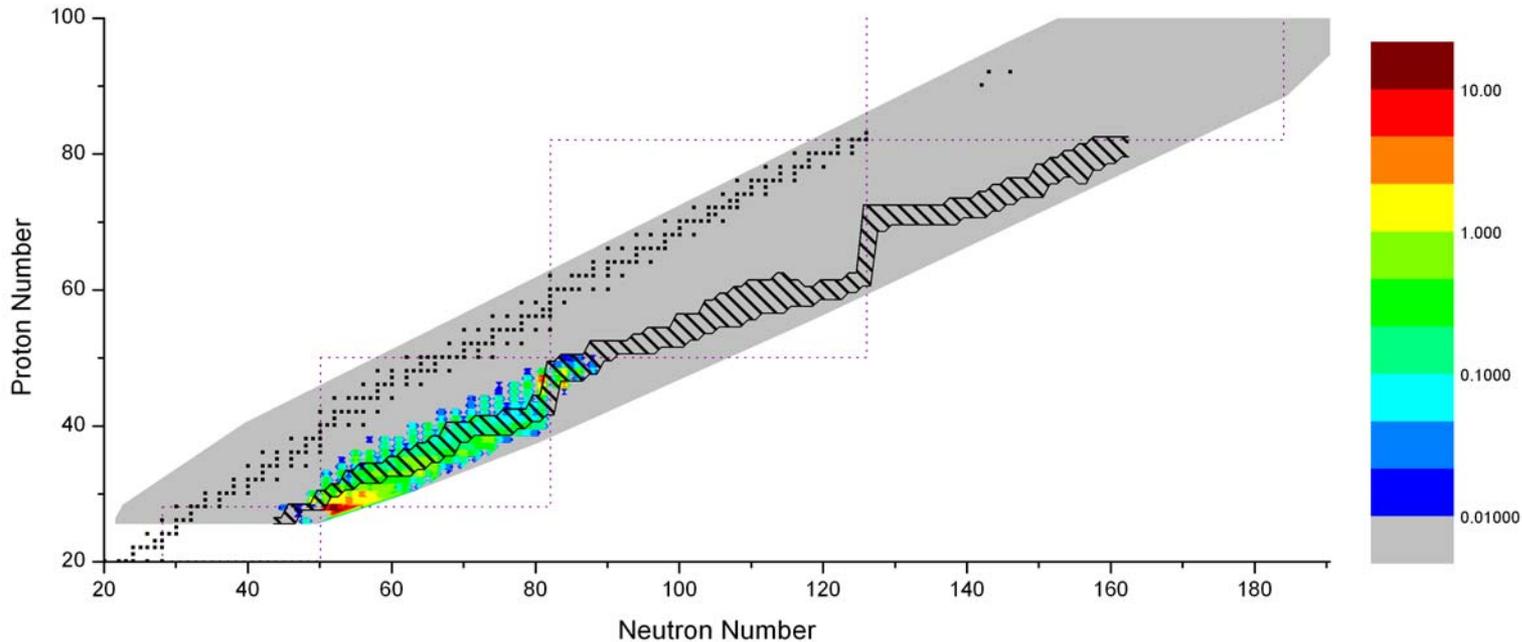


Nucleus	$\Delta_{+25\%}$	$\Delta_{-25\%}$
80Ni	3.47E+00	7.73E+00
128Ag	8.95E-04	1.02E+01
79Ni	1.41E+00	6.29E+00
82Cu	6.57E-01	3.39E+00
86Zn	1.28E+00	2.56E+00
85Zn	1.10E+00	2.46E+00
130Pd	2.23E+00	1.14E-01
87Ga	1.27E+00	1.05E+00
101Br	7.59E-01	1.30E+00
78Cu	2.60E-02	1.87E+00
99Br	6.76E-01	1.22E+00
134Cd	1.73E+00	1.39E-01
132Cd	1.63E+00	2.10E-01
84Zn	6.00E-01	1.23E+00
131Ag	1.53E+00	1.76E-01
98Se	6.51E-01	9.93E-01
91As	2.75E-01	1.33E+00
93As	7.53E-01	8.39E-01
84Ga	1.00E-02	1.53E+00
96Br	8.68E-01	6.06E-01

ETFSI-12 mass model

Run #	Description	Seed	Nseed	Nn	T9	density [g/cm ³]	time [sec.]	Source
68	L Qian's neutrinoless model (Iron)	Fe70	0.672	0.328	1.5	5.1x10 ²	0.78	Qian et al. ApJ 494 (1998) with Fe70

Run 69: L-Event with Iron-70 Seed



Nucleus	$\Delta_{+25\%}$	$\Delta_{-25\%}$
80Ni	4.00E-01	1.20E+01
79Ni	9.96E-01	7.12E+00
128Ag	2.53E-04	4.68E+00
83Cu	4.78E-01	2.44E+00
86Zn	2.62E-02	2.27E+00
127Pd	4.86E-03	2.18E+00
130Pd	2.06E+00	1.00E-01
83Zn	2.77E-01	1.76E+00
78Cu	1.82E-03	2.00E+00
85Zn	5.55E-01	1.39E+00
85Cu	8.06E-01	6.58E-01
82Cu	3.35E-01	1.12E+00
81Cu	5.13E-02	1.29E+00
132Cd	3.52E-01	9.82E-01
84Cu	6.86E-01	6.04E-01
97As	4.29E-01	6.13E-01
126Rh	3.18E-02	9.72E-01
131Ag	7.92E-01	1.19E-01
95As	4.32E-01	4.66E-01
91As	8.71E-03	8.89E-01

F-spin mass model

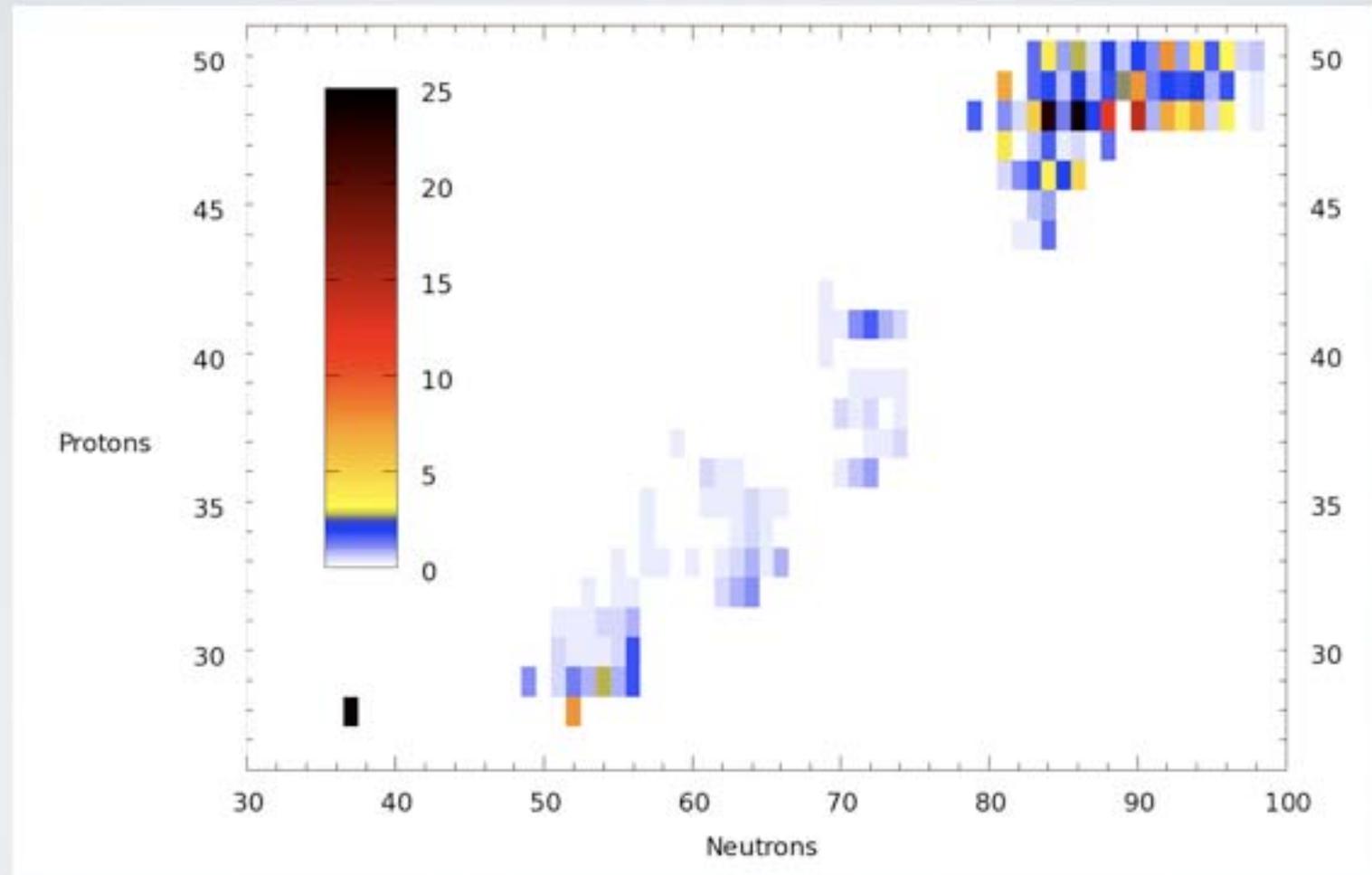
Run #	Description	Seed	Nseed	Nn	T9	density [g/cm ³]	time [sec.]	Source
69	L Qian's neutrinoless model (Iron)	Fe70	0.672	0.328	1.5	5.1x10 ²	0.78	Qian et al. ApJ 494 (1998) with Fe70

Runs 24, 67, 68

- same astrophysical parameters
- Varied mass models
- The following nuclei are in all three top 20

^{79}Ni , ^{82}Cu , ^{85}Zn , ^{86}Zn , ^{130}Pd , ^{131}Ag , and ^{134}Cd .

TESTING FOR SENSITIVITY



TESTING FOR SENSITIVITY

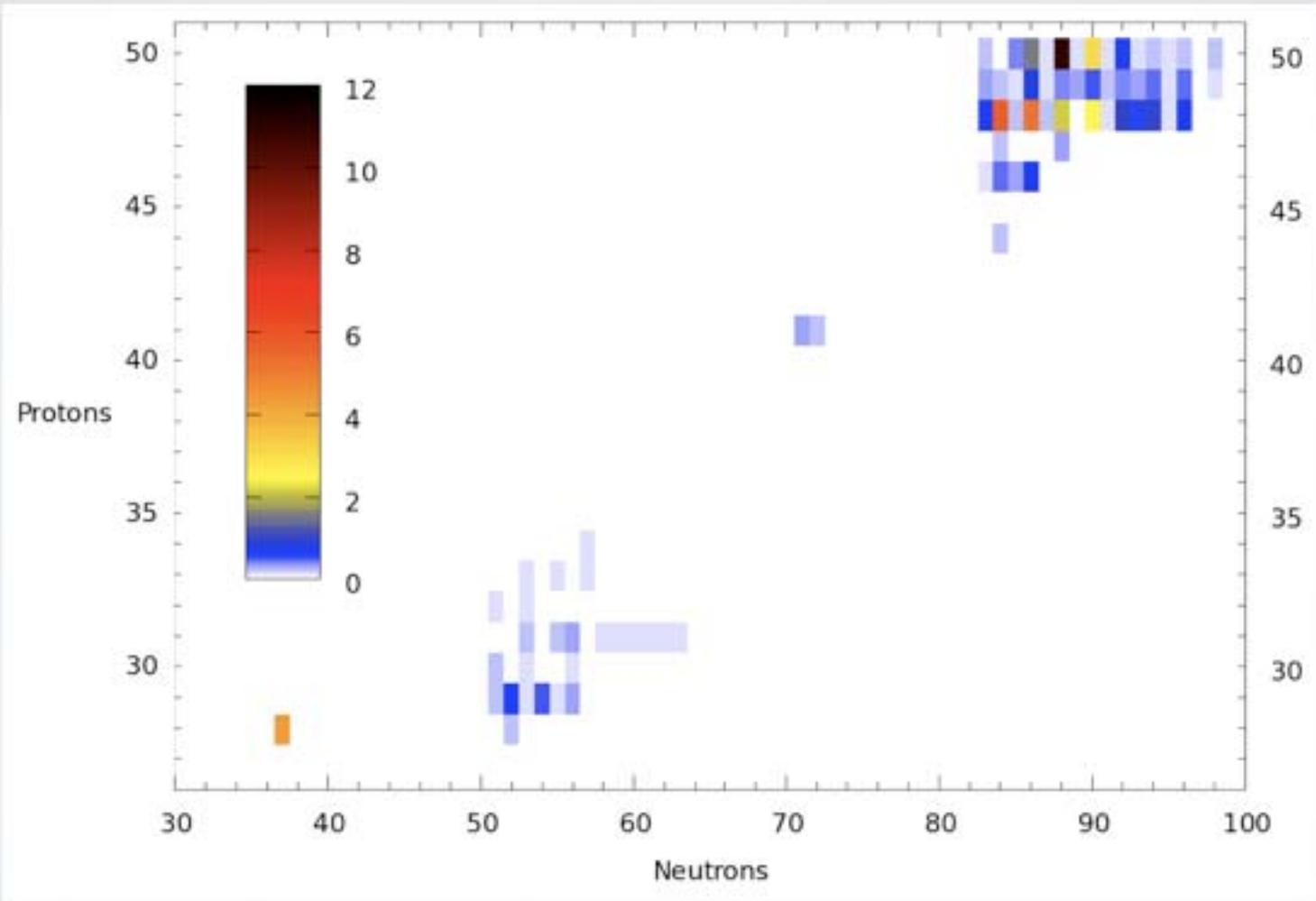


TABLE I: MOST IMPORTANT NUCLEAR MASSES FOR H-SCENARIO WITH ^{70}Fe SEED

^AX	Rank			Rank		
	$\sum \Delta_{\pm 25}$	Δ_{+25}	Δ_{-25}	$\sum \Delta Y_{\pm 25}$	ΔY_{+25}	ΔY_{-25}
^{140}Sn	1	6.77	262	1	1.34	24.4
^{134}Cd	2	15	119	2	8.39	5.78
^{202}Hf	3	36.4	42.5	165	0.07	0.12
^{201}Hf	4	43.9	34.2	179	0.08	0.09
^{203}Hf	5	39.4	33.9	187	0.07	0.09
^{133}Cd	6	8.62	62.7	6	1.94	3.6
^{136}Cd	7	46.6	8.03	5	5.67	0.69
^{82}Cu	8	17.5	27.8	16	1.12	1.31
^{83}Cu	8	13.6	37.6	12	1.31	1.59
^{204}Hf	10	1.96	41.3	256	0	0.11
^{139}Sn	11	8.21	33	4	1.38	5.78
^{135}Cd	12	32.8	7.31	9	3.24	0.63
^{201}Lu	13	37.2	1.81	273	0.1	0.01
^{132}Cd	14	0.29	38.2	3	0.11	11.5
^{142}Sb	15	11.7	24.9	15	0.92	1.58
^{86}Zn	16	2.04	21.5	10	0.01	0.00

ΔY

- Various mass model neutron separation energies ($S_{\downarrow n}$) were varied by $\pm 25\%$ for each nucleus individually.
- The change in the total abundance curve is then calculated using:

$$\Delta Y_{\downarrow \pm 25\%}(N, Z) = \sum A \uparrow \text{▒} Y(A) - Y(A, \pm \Delta S_{\downarrow n}(N, Z)).$$

^{78}Ni , ^{77}Ni first measurement of half-lives

$110^{+100/-60}$ ms; $128^{+27/-33}$ ms

^{76}Ni , ^{75}Ni more precise measurements

$238^{+15/-18}$ ms; $344^{+20/-24}$ ms

